

Testing Lorentz invariance of Dark Matter

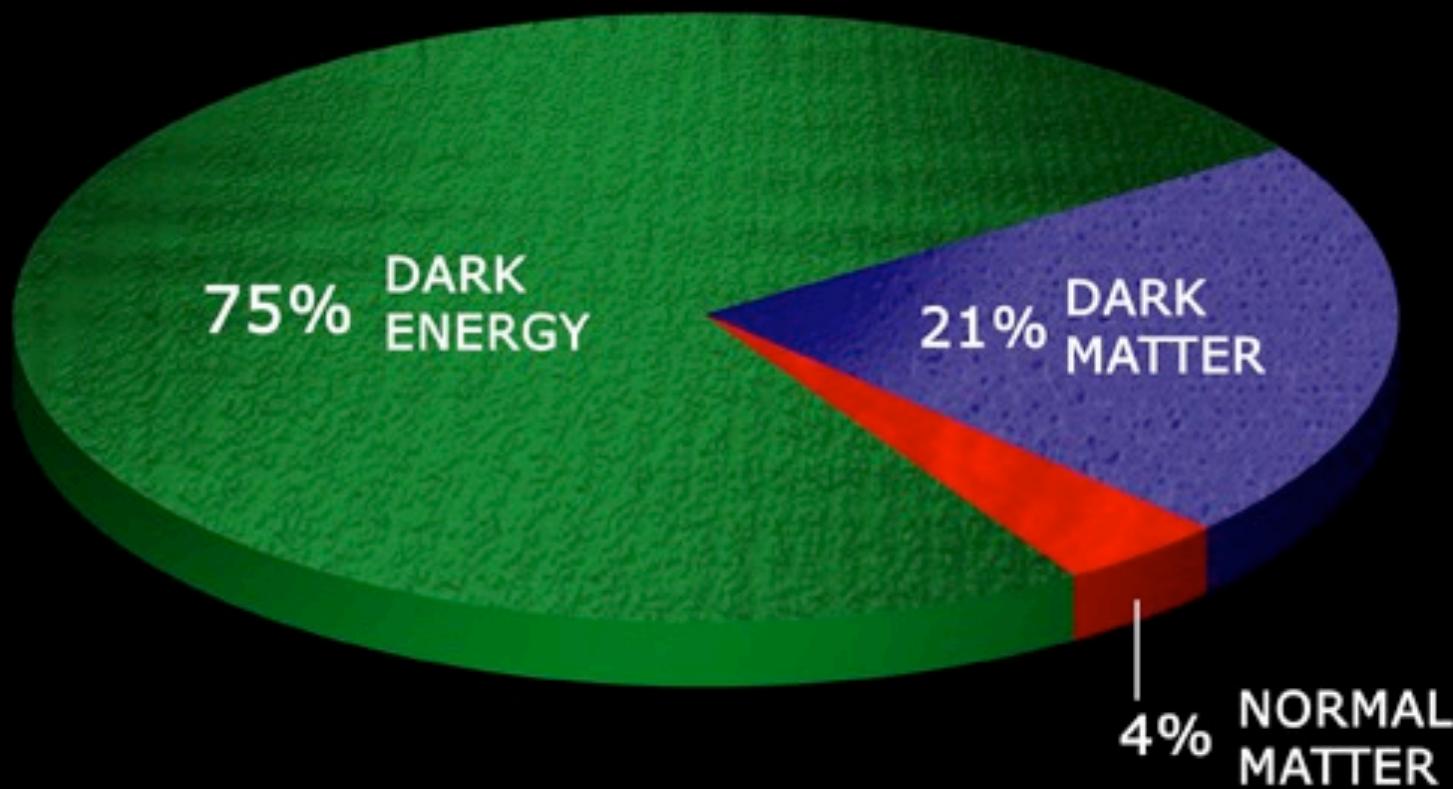
Sergey Sibiryakov
(INR RAS, Moscow)



with Diego Blas, Mikhail Ivanov, Benjamin Audren,
Julien Lesgourgues

Kavli IPMU, 2013

Our Universe is dark



Dark matter: present status

Theory

Plenty of candidates: neutralinos, gravitinos, sterile neutrinos, axions, wimps, wimpzillas, ...

Experiment

Nothing: no direct / indirect detection

Only information from gravitational interactions:
DM clusters as non-relativistic dust

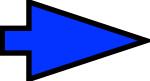
Can we learn more ?

The key principle since 1905:

Lorentz invariance

Consider dispersion relation of a particle

$$E^2 = m^2 + c^2 p^2 + \sum_{n>1} a_n p^{2n}$$

LI 

$$c = 1, a_n = 0$$

Experimental bounds on deviations from LI (δc)

Standard Model

$$10^{-15} \div 10^{-22}$$

gravity

$$10^{-4} \div 10^{-7}$$

dark matter

???

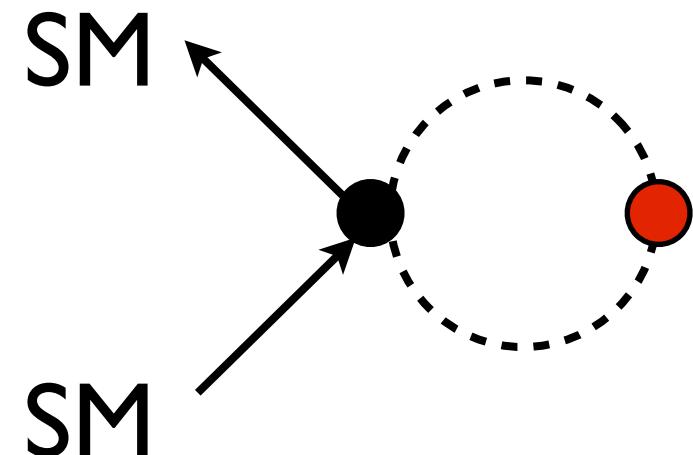
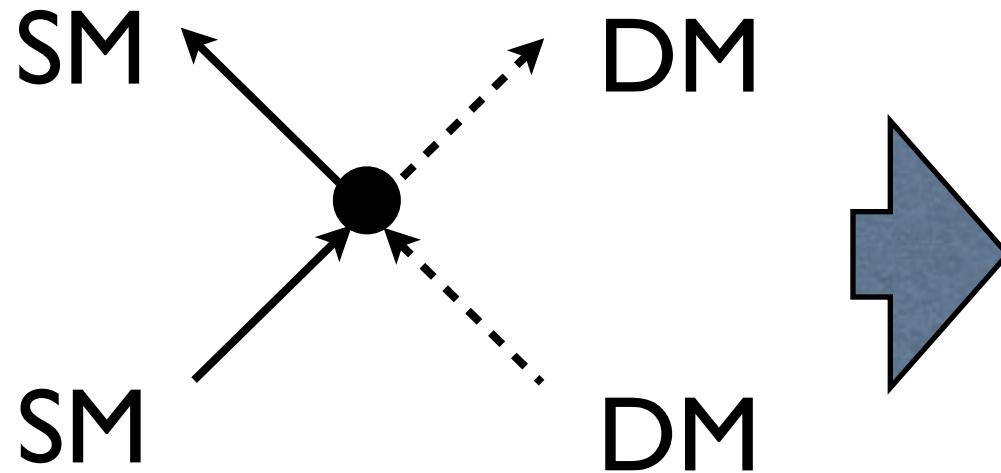
Digression I

Theoretical motivations for deviation from LI

- May be a consequence of quantum gravity
(emergent geometry, Horava-Lifshitz gravity, ...)
- Infrared modifications (e.g. massive gravity,
ghost condensation, ...)

Digression II

If DM is directly detected
→ very strong bounds on LV

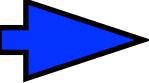


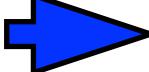
*cf. Bovy, Farrar 2009
Carroll et al. 2009*

NB. These bounds are model-dependent

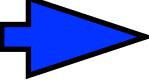
Dark matter is non-relativistic. Impossible to probe whether it is Lorentz invariant or not ?

Yes, it is possible !

Violation of LI  new gravitational degrees of freedom

 additional attraction between DM particles

 violation of the equivalence principle

 enhanced growth of structures

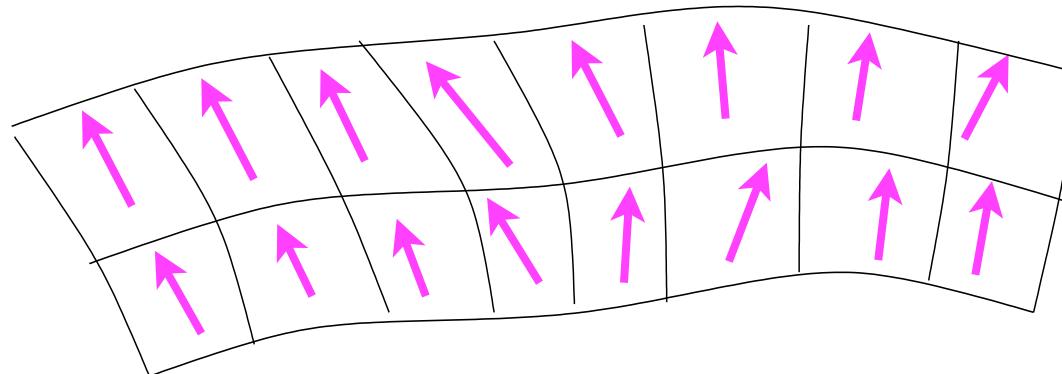
Consider the following pattern of Lorentz symmetry breaking

$$SO(3, 1) \rightarrow SO(3)_{rotations}$$

→ Einstein - aether model

Jacobson, Mattingly, 2000

At each point of the space-time there is a preferred frame set by a dynamical unit vector u^μ - aether



$$S = -\frac{M_P^2}{2} \int d^4x \sqrt{-g} [R + K_{\sigma\rho}^{\mu\nu} \nabla_\mu u^\sigma \nabla_\nu u^\rho + l(u_\mu u^\mu - 1)]$$

Lagrange multiplier:
enforces unit norm

$$K_{\sigma\rho}^{\mu\nu} \equiv c_1 g^{\mu\nu} g_{\sigma\rho} + c_2 \delta_\sigma^\mu \delta_\rho^\nu + c_3 \delta_\rho^\mu \delta_\sigma^\nu + c_4 u^\mu u^\nu g_{\sigma\rho}$$

Variation: khrono-metric model

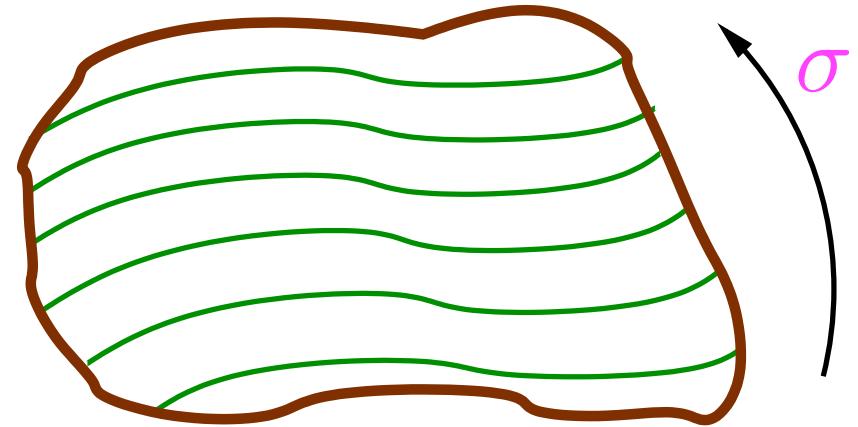
Blas, Pujolas, S.S., 2010

Aether restricted to be hypersurface-orthogonal:

$$u_\mu = \frac{\partial_\mu \sigma}{\sqrt{(\partial\sigma)^2}}$$

Scalar $\sigma(x)$ - *khronon* - defines preferred foliation of the space-time

↔ preferred time



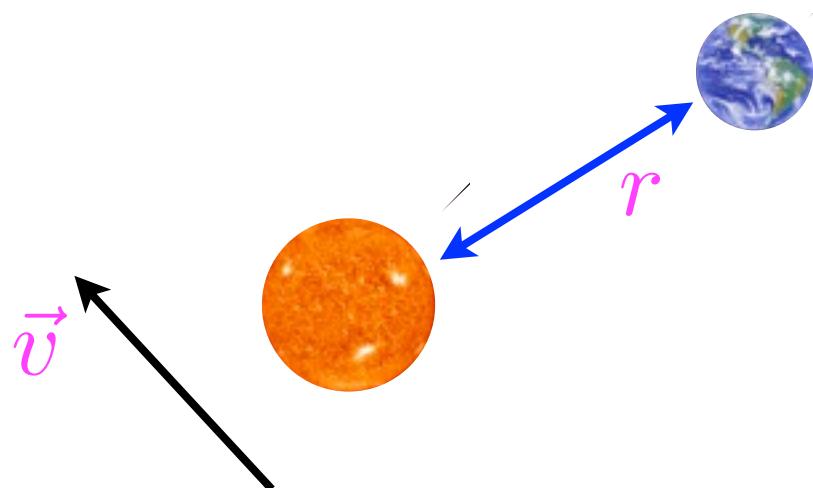
Number of couplings reduced:

$$\alpha = c_1 + c_4, \quad \beta = c_1 + c_3, \quad \lambda' = c_2$$

NB. Can be embedded into Horava-Lifshitz gravity (candidate for quantum gravity)

Constraints from the visible sector

- LI of the Standard Model
 - no direct coupling of aether to visible matter, interaction only through gravity
- Post-Newtonian corrections in the Solar System



$$h_{00} = -2G_N \frac{m}{r} \left(1 - \frac{\alpha_2^{PPN}}{2} \frac{(x^i v^i)^2}{r^2} \right)$$

$$h_{0i} = \frac{\alpha_1^{PPN}}{2} G_N \frac{m}{r} v^i$$

observations: $|\alpha_1^{PPN}| \lesssim 10^{-4}$, $|\alpha_2^{PPN}| \lesssim 10^{-7}$

$$\alpha_1^{PPN} = -4(\alpha - 2\beta)$$

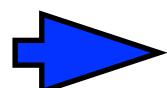
$$\alpha_2^{PPN} = \frac{(\alpha - 2\beta)(\alpha - \lambda' - 3\beta)}{2(\lambda' + \beta)}$$

- no cancellations



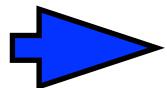
$$\alpha, \beta, \lambda' \lesssim 10^{-7} \div 10^{-6}$$

- α_2^{PPN} vanishes when $\beta = 0, \lambda' = \alpha$



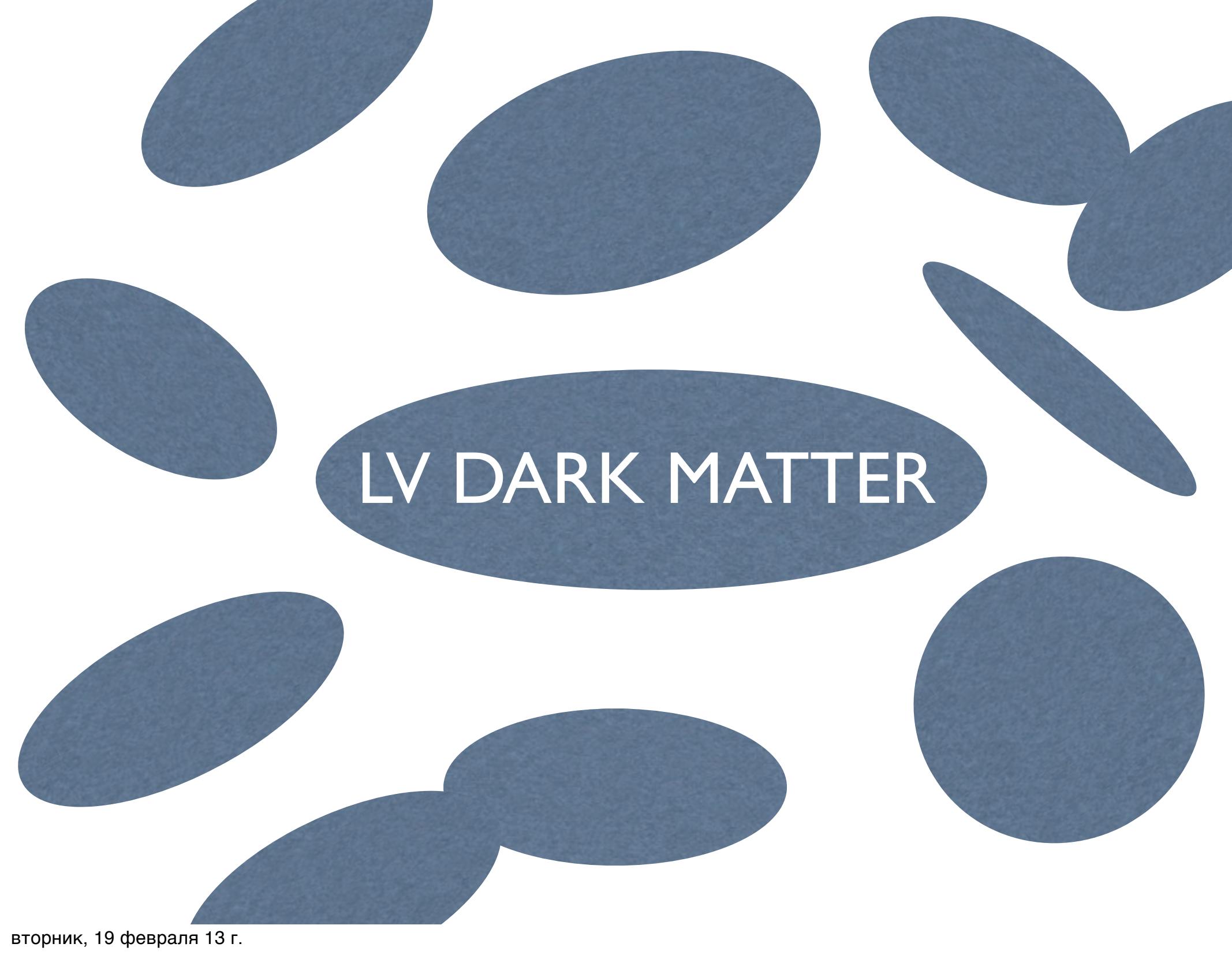
$$\alpha, \beta, \lambda' \lesssim 10^{-4}$$

- both vanish if $\alpha = 2\beta$



from gravitational wave emission and BBN

$$\alpha, \beta, \lambda' \lesssim 0.01$$



LV DARK MATTER

Generalized point particle action

$$S_{pp} = -m \int ds \quad \Longrightarrow \quad -m \int ds f(u_\mu v^\mu)$$

$\frac{dx^\mu}{ds}$

Connection to the dispersion relation:

$$p_i = \frac{\partial L}{\partial V^i} \qquad E = p_i V^i - L$$

$$E^2 = m^2 + (1 + \xi)p^2$$

→ $f = \sqrt{\frac{1 + \xi(u_\mu v^\mu)^2}{1 + \xi}} \approx 1 + \xi \frac{(u_\mu v^\mu)^2 - 1}{2}$

Generalized point particle action

$$S_{pp} = -m \int ds \quad \Longrightarrow \quad -m \int ds f(u_\mu v^\mu)$$

$\frac{dx^\mu}{ds}$

Newtonian limit: v^i , u^i -- small, $g_{00} = 1 + 2\phi$

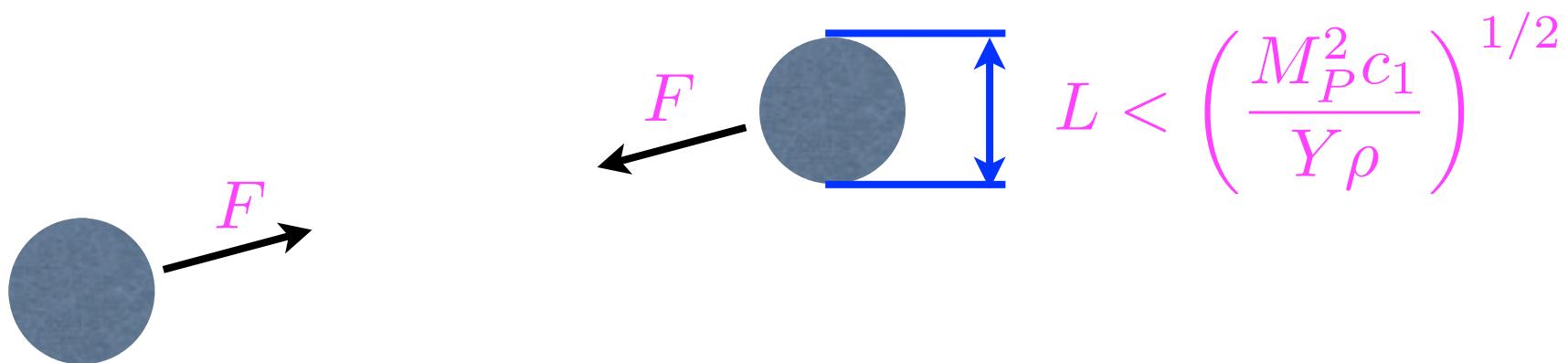
$$S = \int d^4x \left[M_P^2 \phi \Delta \phi + \frac{M_P^2 c_1}{2} u^i \Delta u^i \right] + \int d^4x \rho \left[\frac{(v^i)^2}{2} - \phi - Y \frac{(u^i - v^i)^2}{2} \right]$$

DM density

$f'(1)$

- modified inertial mass = violation of the equivalence principle
- effective potential for aether in matter

$$m_{eff}^2 \sim \frac{Y \rho}{M_P^2 c_1}$$

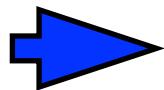
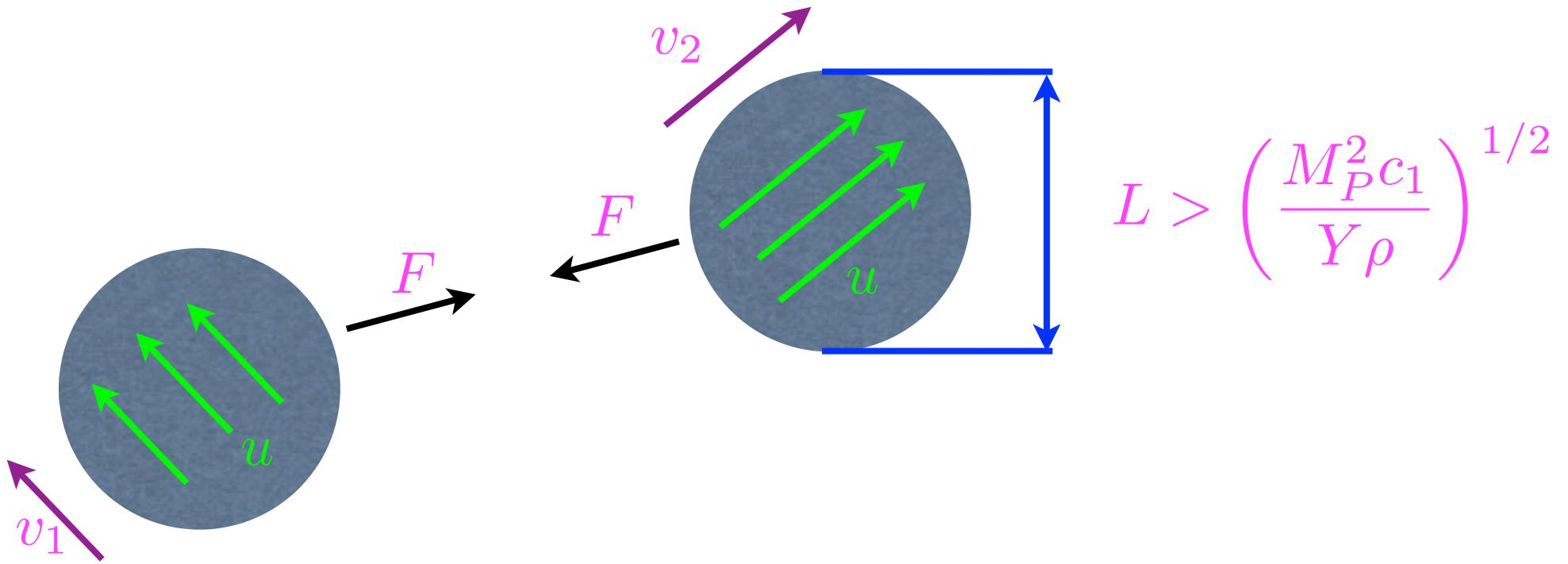


→ $F = \frac{F_N}{(1 - Y)}$

Accelerated Jeans instability

$$\delta \propto \tau^\gamma, \quad \gamma = \frac{1}{6} \left[-1 + \sqrt{\frac{25 - Y}{1 - Y}} \right]$$

density contrast



$$F = F_N$$

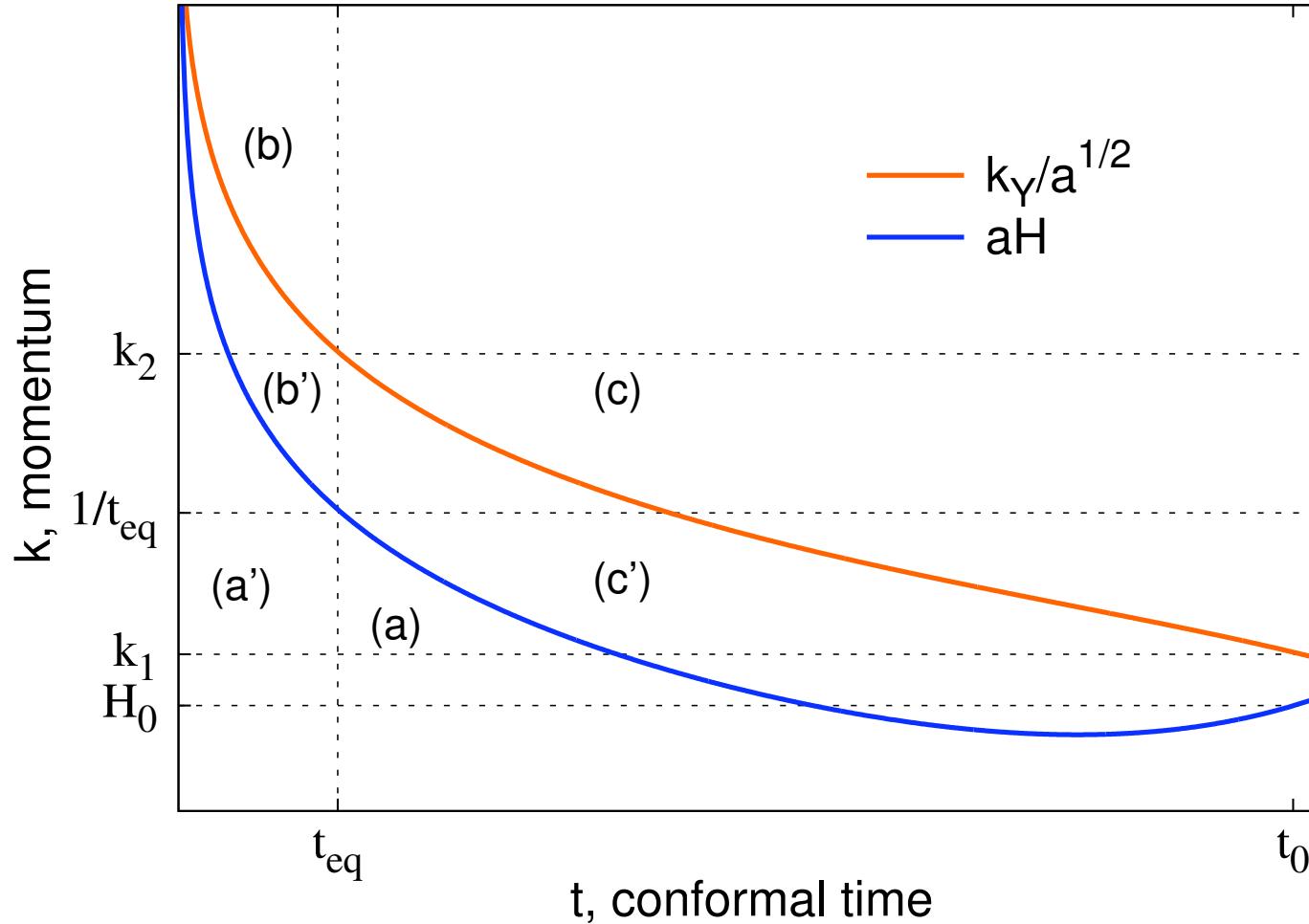
screening of the additional force
 \approx chameleon-type mechanism

Standard Jeans instability $\delta \propto \tau^{2/3}$

NB. Standard homogeneous cosmology

$$L > \left(\frac{M_P^2 c_1}{Y \rho} \right)^{1/2}$$

Screening scale vs. Hubble



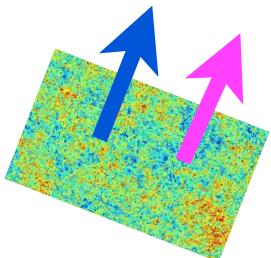
$$k_Y^2 \equiv \frac{3H_0^2\Omega_{dm}Y}{(\beta + \lambda')(1 - Y)}$$

Relativistic cosmology

$$G_{\mu\nu} = \frac{1}{M_P^2} T_{\mu\nu}^m + \frac{1}{M_P^2} T_{\mu\nu}^{fluid} + \frac{1}{M_P^2} T_{\mu\nu}^{aether} + \Lambda g_{\mu\nu}$$

baryonic matter minimally coupled to gravity

Background: Homogeneous and isotropic
(preferred foliation aligned with CMB frame)



$$ds^2 = g_{\mu\nu} dx^\mu dx^\nu = dt^2 - a(t)^2 dx^i dx^i$$
$$u_\mu = (u_0(t), 0, 0, 0) = v_\mu , \rho(t)$$

Friedmann equations almost not modified!

$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G_c}{3} \rho_m$$

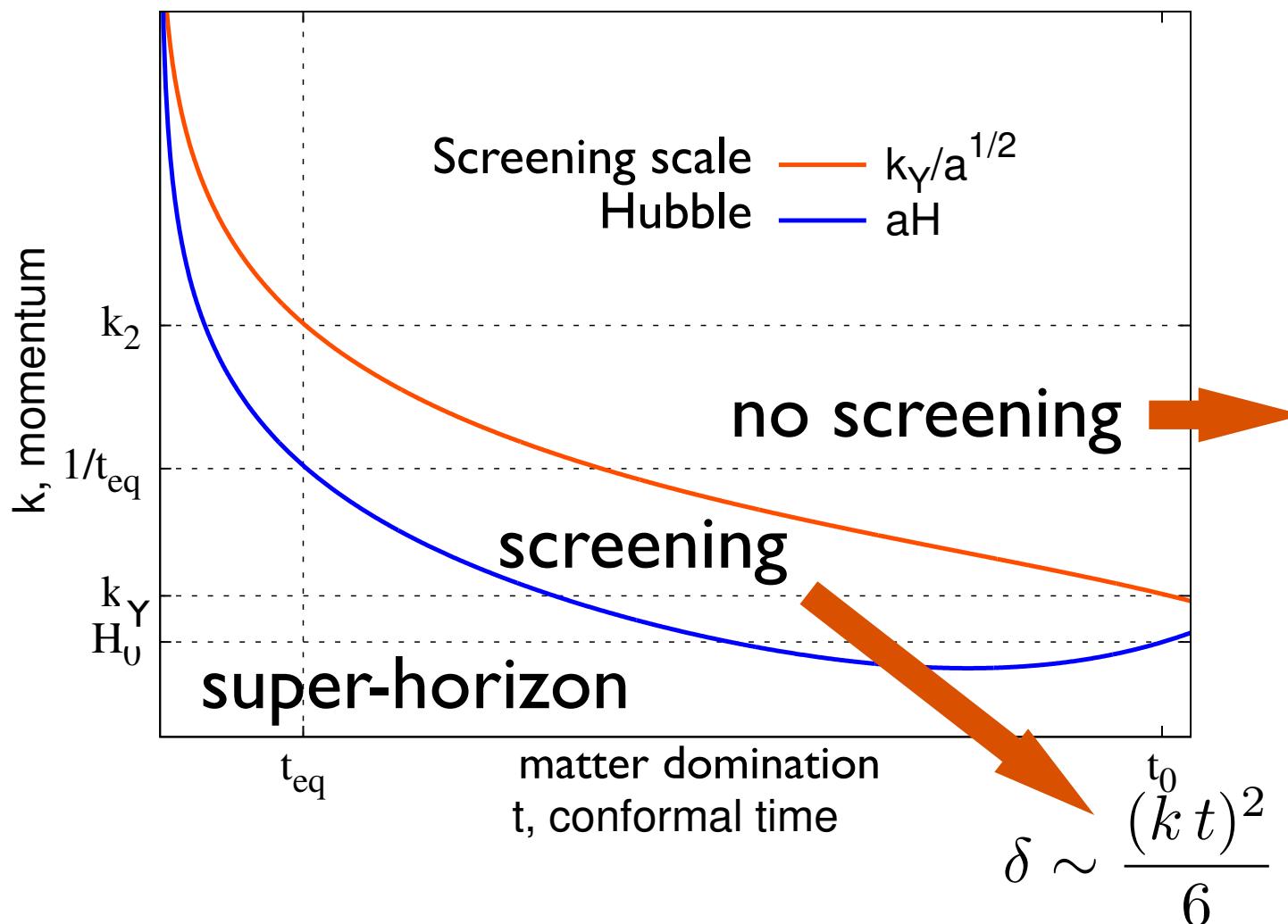
$$G_c = \frac{1}{8\pi M_P^2 [1 + 3\lambda/2 + \beta/2]}$$

From BBN $G_c = G_N + O(.01)$

Cosmological perturbations

$$\rho(x, t) \equiv \rho(t)(1 + \delta(x, t))$$

Scalars: All effects summarized in $Y \equiv \tilde{f}'(1)$



$$k_Y^2 \equiv \frac{3H_0^2\Omega_{dm}Y}{(\beta + \lambda)(1 - Y)}$$

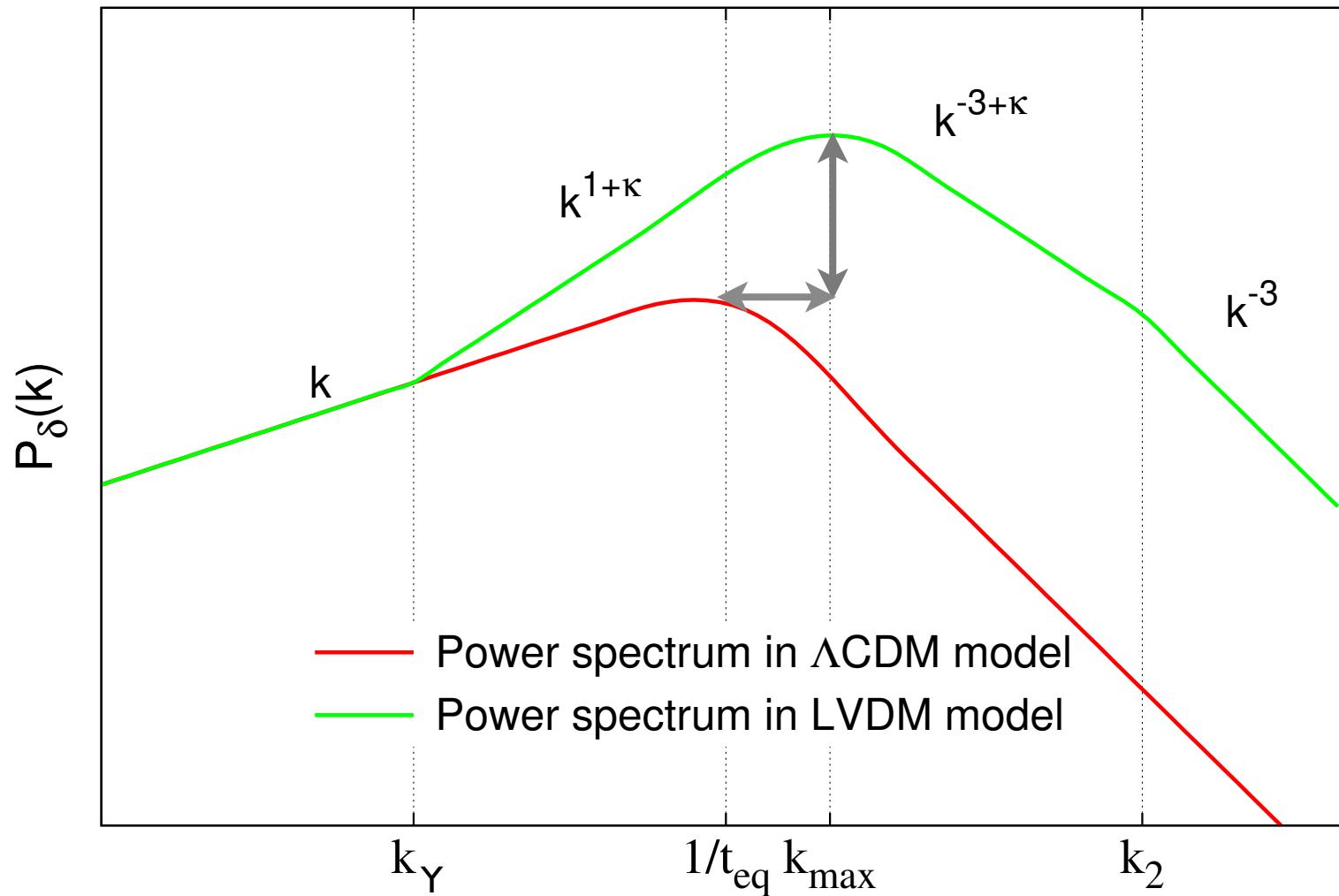
$$\delta \sim \frac{(k t)^2}{6(1 - Y)} t^\kappa$$

$$\kappa = \sqrt{25 + \frac{24\Omega_{dm}Y}{\Omega_{cm}(1 - Y)}} - 5$$

$$\delta \sim \frac{(k t)^2}{6}$$

Matter power spectrum: qualitative

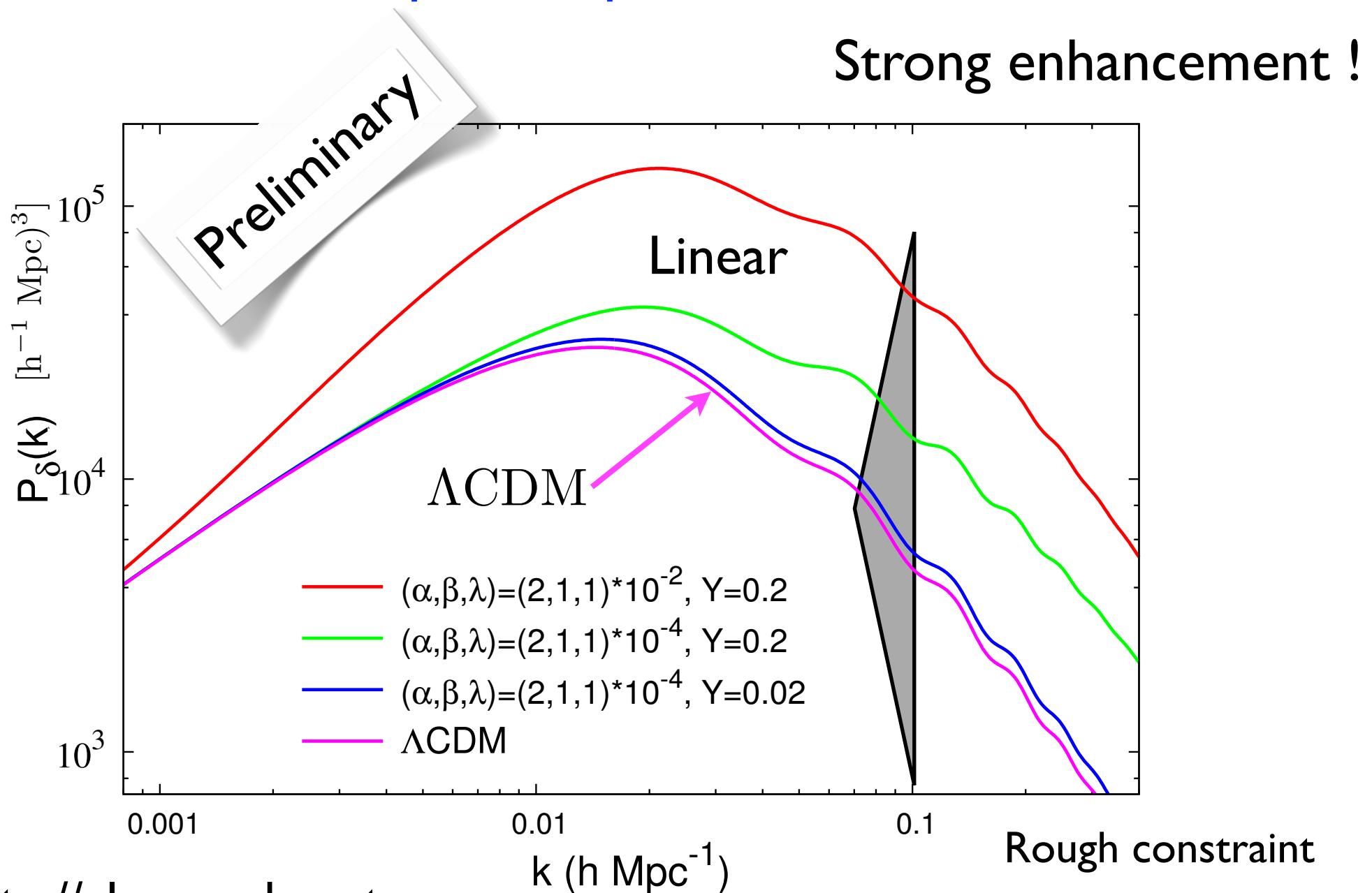
$$\langle \delta(k) \delta(k') \rangle \equiv \delta^{(3)}(k + k') P(k) k^3$$



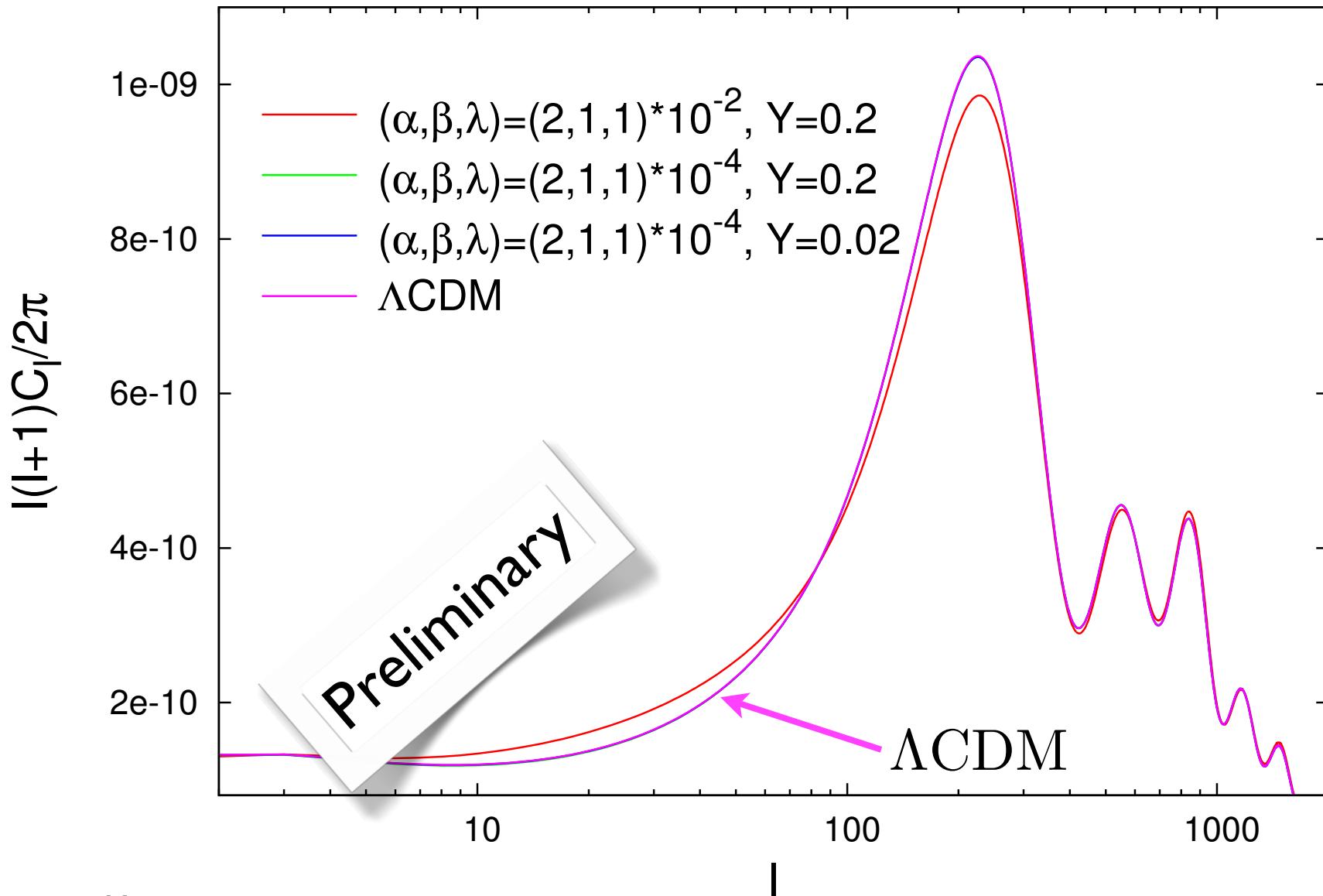
$$k_Y^2 \equiv \frac{3H_0^2 \Omega_{dm} Y}{(\beta + \lambda)(1 - Y)}$$

$$k_2 = k_Y \sqrt{\frac{\Omega_{dm} + \Omega_b}{\Omega_\gamma}}$$

Matter power spectrum: numerical



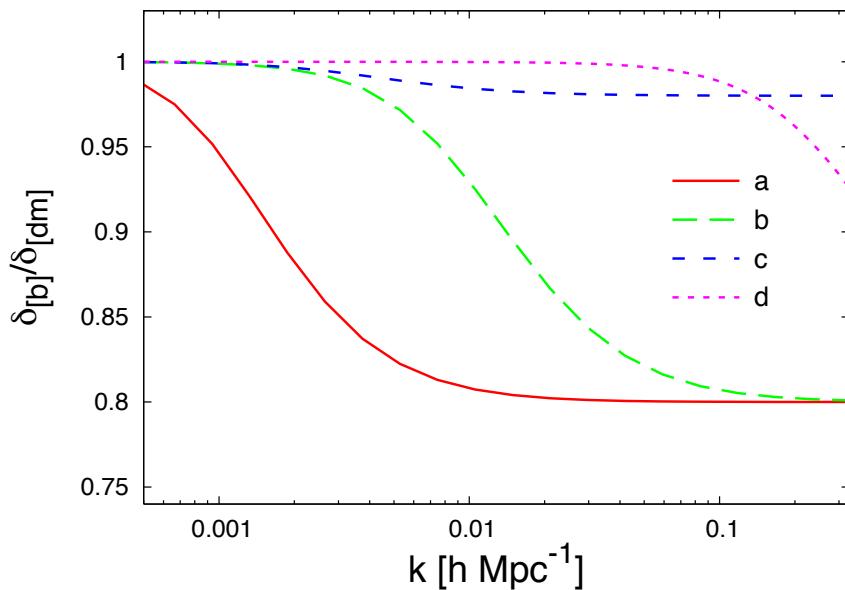
Cosmic microwave background



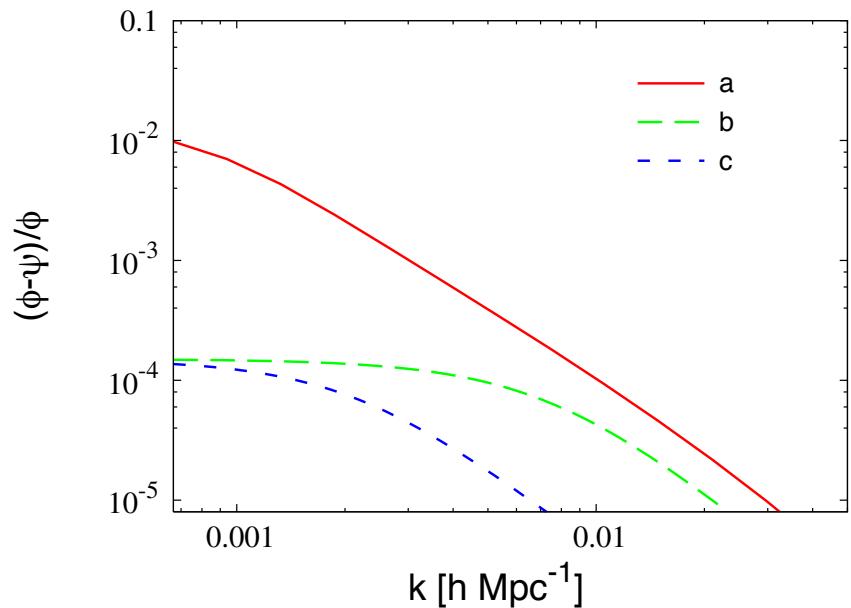
<http://class-code.net>

Other effects

Baryons bias



Anisotropic stress



	α	β	λ	Y	$k_{Y,0} \ (\mathrm{h \ Mpc^{-1}})$	$k_{Y,eq} \ (\mathrm{h \ Mpc^{-1}})$
a	$2 \cdot 10^{-2}$	10^{-2}	10^{-2}	0.2	$9.2 \cdot 10^{-4}$	$6.5 \cdot 10^{-2}$
b	$2 \cdot 10^{-4}$	10^{-4}	10^{-4}	0.2	$9.1 \cdot 10^{-3}$	0.65
c	$2 \cdot 10^{-4}$	10^{-4}	10^{-4}	0.02	$2.6 \cdot 10^{-3}$	0.18
d	10^{-7}	0	10^{-7}	0.2	0.41	29

Rough constraint on LV in dark matter:

$$Y < 10^{-2}$$

Summary

- Developing theoretical frameworks for deviations from LI is important to better understand our Universe
- Effects of LV in **dark matter** on cosmology: same background evolution, but distinct signals for (linear) perturbations.
- Cosmological observations allow to constrain deviations from LI in **dark matter** at the level 10^{-2} or better

OUTLOOK

- * Study of the parameter space, comparison with data, effects at non-linear scales