W+3 jet production at the LHC

— signal or background —

Giulia Zanderighi

Oxford Theoretical Physics & STFC

LHC focus week, IPMU, Tokyo University, I 2th November 2009

Multiparticle final states

LHC's new regime in energy and luminosity implies that we will have a very large number of high-multiplicity events

- typical SM process is accompanied by radiation multi-jet events
- most signals involve pair-production and subsequent chain decays



More important than ever to describe high-multiplicity final states

Leading order

Status: fully automated, edge around outgoing 8 particles

Alpgen, CompHEP, CalcHEP, Helac, Madgraph, Helas, Sherpa, Whizard, ...

⇒ amazing progress in the last years [before only parton shower]

Leading order

Status: fully automated, edge around outgoing 8 particles

Alpgen, CompHEP, CalcHEP, Helac, Madgraph, Helas, Sherpa, Whizard, ...

⇒ amazing progress in the last years [before only parton shower]

Drawbacks of LO:

large scale dependences, sensitivity to cuts, poor modeling of jets, ...

<u>Example</u>: W+4 jet cross-section $\propto \alpha_s(Q)^4$

Vary $\alpha_s(Q)$ by ±10% via change of $Q \Rightarrow$ cross-section varies by ±40%

Leading order

Status: fully automated, edge around outgoing 8 particles

Alpgen, CompHEP, CalcHEP, Helac, Madgraph, Helas, Sherpa, Whizard, ...

⇒ amazing progress in the last years [before only parton shower]

Drawbacks of LO: large scale dependences, sensitivity to cuts, poor modeling of jets, ... Example: W+4 jet cross-section $\propto \alpha_s(Q)^4$ Vary $\alpha_s(Q)$ by ±10% via change of Q \Rightarrow cross-section varies by ±40%

When and why LO:

- always the fastest option, often the only one
- Lest quickly new ideas with fully exclusive description
- many working, well-tested approaches
- In highly automated, crucial to explore new ground, but no precision

Why NLO?

- Solutions only qualitative, due to poor convergence of perturbative expansion ($\alpha_s \sim 0.1$) \Rightarrow NLO can be 30-100%
- first prediction of normalization of cross-sections is at NLO
- Iess sensitivity to unphysical input scales (renormalization, factorization)
- more physics at NLO
 - parton merging to give structure in jets
 - more species of incoming partons enter at NLO
 - initial state radiation effects
- a prerequisite for more sophisticated calculations which match NLO with parton showers

Why NLO?

- Solution LO predictions only qualitative, due to poor convergence of perturbative expansion ($\alpha_s \sim 0.1$) \Rightarrow NLO can be 30-100%
- first prediction of normalization of cross-sections is at NLO
- Iess sensitivity to unphysical input scales (renormalization, factorization)
- more physics at NLO
 - parton merging to give structure in jets
 - more species of incoming partons enter at NLO
 - initial state radiation effects
- a prerequisite for more sophisticated calculations which match NLO with parton showers

⇒ Role of NLO for precision measurement uncontested What about for discoveries?

The 2007 Les Houches NLO wishlist

Process $(V \in \{Z, W, \gamma\})$ Calculations completed since Les Houches 20051. $pp \rightarrow VV$ jet2. $pp \rightarrow$ Higgs+2jets	Comments <i>WW</i> jet completed by Dittmaier/Kallweit/Uwer [3]; Campbell/Ellis/Zanderighi [4] and Binoth/Karg/Kauer/Sanguinetti (in progress) NLO QCD to the <i>gg</i> channel completed by Campbell/Ellis/Zanderighi [5]; NLO QCD+EW to the VBF channel completed by Ciccolini/Denner/Dittmaier [6,7]	based on Feynman diagrams;
3. $pp \rightarrow VVV$	ZZZ completed by Lazopoulos/Melnikov/Petriello [8] and WWZ by Hankele/Zeppenfeld [9]	J privace codes only
Calculations femalining from Les frouches 2005		
4. $pp \rightarrow t\bar{t} b\bar{b}$	relevant for $t\bar{t}H$	'09 with standard techniques
5. $pp \rightarrow t\bar{t}$ +2jets	relevant for $t\bar{t}H$	
6. $pp \rightarrow VV bb$,	relevant for VBF $\rightarrow H \rightarrow VV, ttH$	
7. $pp \rightarrow VV+2$ jets	relevant for VBF \rightarrow $H \rightarrow VV$	
	(Bozzi/) läger/Olegri/Zeppenfeld [10_12]	
8. $pp \rightarrow V$ +3jets	various new physics signatures	'09 with new techniques
NLO calculations added to list in 2007		
9. $pp \rightarrow b\bar{b}b\bar{b}$	Higgs and new physics signatures	
Calculations beyond NLO added in 2007		
10. $gg \rightarrow W^*W^* \mathcal{O}(\alpha^2 \alpha_s^3)$ 11. NNLO $pp \rightarrow t\bar{t}$ 12. NNLO to VBF and Z/γ +jet	backgrounds to Higgs normalization of a benchmark process Higgs couplings and SM benchmark	
Calculations including electroweak effects		
13. NNLO QCD+NLO EW for W/Z	precision calculation of a SM benchmark	

+ virtual amplitudes for all $2 \rightarrow 4$ at one point [van Hameren, Papadopoulos, Pittau]

NLO: current status

Status of NLO:

- $\boxed{12}$ 2 \rightarrow 2: all known (or easy) in SM and beyond
- $\boxed{12}$ 2 \rightarrow 3: very few processes left

[but: often do not include decays, newest codes mostly private]

- $\Box \quad 2 \rightarrow 4: the frontier$
 - NLO cross-sections available only for two processes at the LHC
 ✓ tt + bb [Bredenstein et al '08; Bevilacqua et al '09]
 ✓ W + 3jets [Berger et al '09; Ellis et al '09 (LC)]
 - Benchmark results for all 2 → 4 processes in the Les Houches list at one phase space point [van Hameren et al '09]

See talks of Lance Dixon and Zoltan Kunszt for recent progress on new techniques for NLO calculations

Generalized unitarity

I will not explain the method in detail, only remind of the main ideas (see talks of L. Dixon and Z. Kunszt).

I will concentrate on applications & recent results

References:

- Ellis, Giele, Kunszt '07
- Giele, Kunszt, Melnikov '08
- Giele & GZ '08
- Ellis, Giele, Melnikov, Kunszt '08
- Ellis, Giele, Melnikov, Kunszt, GZ '08
- Ellis, Melnikov, GZ '09, Melnikov & GZ '09

These papers heavily rely on previous work

- Bern, Dixon, Kosower '94
- Ossola, Pittau, Papadopoulos '06
- Britto, Cachazo, Feng '04

- [....]

[Unitarity in D=4] [Unitarity in D≠4] [All one-loop N-gluon amplitudes] [Massive fermions, ttggg amplitudes] [W+5p one-loop amplitudes] [W+3 jets]

[Unitarity, oneloop from trees] [OPP] [Generalized cuts]

One-loop virtual amplitudes

Cut constructible part can be obtained by taking residues in D=4

$$\mathcal{A}_{N} = \sum_{[i_{1}|i_{4}]} \left(d_{i_{1}i_{2}i_{3}i_{4}} \ I_{i_{1}i_{2}i_{3}i_{4}}^{(D)} \right) + \sum_{[i_{1}|i_{3}]} \left(c_{i_{1}i_{2}i_{3}} \ I_{i_{1}i_{2}i_{3}}^{(D)} \right) + \sum_{[i_{1}|i_{2}]} \left(b_{i_{1}i_{2}} \ I_{i_{1}i_{2}}^{(D)} \right) + \mathcal{R}$$

Rational part: can be obtained with $D \neq 4$

Generic D dependence

Two sources of D dependence





dimensionality of loop momentum D

of spin eigenstates/ polarization states D_s

Keep D and D_s distinct



Two key observations

I. External particles in D=4 \Rightarrow no preferred direction in the extra space

$$\mathcal{N}(l) = \mathcal{N}(l_4, \tilde{l}^2)$$
 $\tilde{l}^2 = -\sum_{i=5}^D l_i^2$ \mathcal{N} : numerator function

• in arbitrary D up to 5 constraints \Rightarrow get up to pentagon integrals

Two key observations

I. External particles in D=4 \Rightarrow no preferred direction in the extra space

$$\mathcal{N}(l) = \mathcal{N}(l_4, \tilde{l}^2)$$
 $\tilde{l}^2 = -\sum_{i=5}^D l_i^2$ \mathcal{N} : numerator function

• in arbitrary D up to 5 constraints \Rightarrow get up to pentagon integrals

2. Dependence of \mathcal{N} on D_s is linear (or almost)

$$\mathcal{N}^{D_s}(l) = \mathcal{N}_0(l) + (D_s - 4)\mathcal{N}_1(l)$$

■ evaluate at any D_{s1} , $D_{s2} \Rightarrow$ get \mathcal{N}_0 and \mathcal{N}_1 , i.e., full \mathcal{N}

Two key observations

I. External particles in D=4 \Rightarrow no preferred direction in the extra space

$$\mathcal{N}(l) = \mathcal{N}(l_4, \tilde{l}^2)$$
 $\tilde{l}^2 = -\sum_{i=5}^D l_i^2$ \mathcal{N} : numerator function

• in arbitrary D up to 5 constraints \Rightarrow get up to pentagon integrals

2. Dependence of \mathcal{N} on D_s is linear (or almost)

$$\mathcal{N}^{D_s}(l) = \mathcal{N}_0(l) + (D_s - 4)\mathcal{N}_1(l)$$

■ evaluate at any D_{s1} , $D_{s2} \Rightarrow$ get \mathcal{N}_0 and \mathcal{N}_1 , i.e., full \mathcal{N}

Choose D_{s1} , D_{s2} integer \Rightarrow suitable for numerical implementation

$$[D_s = 4 - 2\varepsilon$$
 't-Hooft-Veltman scheme, $D_s = 4$ FDH scheme]

In practice

Start from

$$\frac{\mathcal{N}^{(D_s)}(l)}{d_1 d_2 \cdots d_N} = \sum_{[i_1|i_5]} \frac{\overline{e}_{i_1 i_2 i_3 i_4 i_5}^{(D_s)}(l)}{d_{i_1} d_{i_2} d_{i_3} d_{i_4} d_{i_5}} + \sum_{[i_1|i_4]} \frac{\overline{d}_{i_1 i_2 i_3 i_4}^{(D_s)}(l)}{d_{i_1} d_{i_2} d_{i_3} d_{i_4}} + \sum_{[i_1|i_3]} \frac{\overline{c}_{i_1 i_2 i_3}^{(D_s)}(l)}{d_{i_1} d_{i_2} d_{i_3}} + \sum_{[i_1|i_2]} \frac{\overline{b}_{i_1 i_2}^{(D_s)}(l)}{d_{i_1} d_{i_2}} + \sum_{[i_1|i_1]} \frac{\overline{a}_{i_1}^{(D_s)}(l)}{d_{i_1} d_{i_2}} + \sum_{[i_1|i_2]} \frac{\overline{b}_{i_1 i_2}^{(D_s)}(l)}{d_{i_1} d_{i_2}} + \sum_{[i_1|i_1]} \frac{\overline{a}_{i_1}^{(D_s)}(l)}{d_{i_1} d_{i_2}} + \sum_{[i_1|i_2]} \frac{\overline{b}_{i_1 i_2}^{(D_s)}(l)}{d_{i_1} d_{i_2}} + \sum_{[i_1|i_1]} \frac{\overline{a}_{i_1}^{(D_s)}(l)}{d_{i_1} d_{i_2}} + \sum_{[i_1|i_2]} \frac{\overline{b}_{i_1 i_2}^{(D_s)}(l)}{d_{i_1} d_{i_2}} + \sum_{[i_1|i_1]} \frac{\overline{b}_{i_1}^{(D_s)}(l)}{d_{i_1} d_{i_2}} + \sum_{[i_1|i_2]} \frac{\overline{b}_{i_1 i_2}^{(D_s)}(l)}{d_{i_1} d_{i_2}} + \sum_{[i_1|i_1]} \frac{\overline{b}_{i_1}^{(D_s)}(l)}{d_{i_1} d_{i_2}} + \sum_{[i_1|i_2]} \frac{\overline{b}_{i_1}^{(D_s)}(l)}{d_{i_1} d_{i_2}} + \sum_{[i_1|i_1]} \frac{\overline{b}_{i_1}^{(D_s)}(l)}{d_{i_1} d_{i_2}} + \sum_{[i_1|i_2]} \frac{\overline{b}_{i_1}^{(D_s)}(l)}{d_{i_1} d_{i_2} d_{i_3}} + \sum_{[i_1|i_2]} \frac{\overline{b}_{i_1}^{(D_s)}(l)}{d_{i_1} d_{i_2}$$

- Use unitarity constraints to determine the coefficients, computed as products of tree-level amplitudes with complex momenta in higher dimensions
- Berends-Giele recursion relations are natural candidates to compute tree level amplitudes: they are very fast for large N and very general (spin, masses, complex momenta)

Berends, Giele '88

Generalized unitarity: very simple, efficient, general, transparent method, straightforward to implement/automate

Final result

$$\begin{aligned} \mathcal{A}_{(D)} &= \sum_{[i_1|i_5]} e_{i_1i_2i_3i_4i_5}^{(0)} I_{i_1i_2i_3i_4i_5}^{(D)} \\ &+ \sum_{[i_1|i_4]} \left(d_{i_1i_2i_3i_4}^{(0)} I_{i_1i_2i_3i_4}^{(D)} - \frac{D-4}{2} d_{i_1i_2i_3i_4}^{(2)} I_{i_1i_2i_3i_4}^{(D+2)} + \frac{(D-4)(D-2)}{4} d_{i_1i_2i_3i_4}^{(4)} I_{i_1i_2i_3i_4}^{(D+4)} \right) \\ &+ \sum_{[i_1|i_3]} \left(c_{i_1i_2i_3}^{(0)} I_{i_1i_2i_3}^{(D)} - \frac{D-4}{2} c_{i_1i_2i_3}^{(9)} I_{i_1i_2i_3}^{(D+2)} \right) + \sum_{[i_1|i_2]} \left(b_{i_1i_2}^{(0)} I_{i_1i_2}^{(D)} - \frac{D-4}{2} b_{i_1i_2}^{(9)} I_{i_1i_2}^{(D+2)} \right) \end{aligned}$$

Cut-constructible part:

$$\mathcal{A}_{N}^{CC} = \sum_{[i_{1}|i_{4}]} d_{i_{1}i_{2}i_{3}i_{4}}^{(0)} I_{i_{1}i_{2}i_{3}i_{4}}^{(4-2\epsilon)} + \sum_{[i_{1}|i_{3}]} c_{i_{1}i_{2}i_{3}}^{(0)} I_{i_{1}i_{2}i_{3}}^{(4-2\epsilon)} + \sum_{[i_{1}|i_{2}]} b_{i_{1}i_{2}}^{(0)} I_{i_{1}i_{2}}^{(4-2\epsilon)}$$

Rational part:

$$R_N = -\sum_{[i_1|i_4]} \frac{d_{i_1 i_2 i_3 i_4}^{(4)}}{6} + \sum_{[i_1|i_3]} \frac{c_{i_1 i_2 i_3}^{(9)}}{2} - \sum_{[i_1|i_2]} \left(\frac{(q_{i_1} - q_{i_2})^2}{6} - \frac{m_{i_1}^2 + m_{i_2}^2}{2}\right) b_{i_1 i_2}^{(9)}$$

<u>Vanishing contributions</u>: $\mathcal{A} = \mathcal{O}(\epsilon)$

Scalar integrals $I^{(4-2e)}_{iii2...}$ all known 't Hooft & Veltman '79; Bern, Dixon Kosower '93, Duplancic & Nizic '02; Ellis & GZ '08, public code \Rightarrow http://www.qcdloop.fnal.gov

The F90 Rocket program

Rocket science!

Eruca sativa =Rocket=roquette=arugula=rucola Recursive unitarity calculation of one-loop amplitudes



So far computed one-loop amplitudes:

 $\sqrt[]{ N-gluons } \\ \sqrt[]{ qq + N-gluons } \\ \sqrt[]{ qq + W + N-gluons } \\ \sqrt[]{ qq + QQ + W } \\ \sqrt[]{ tt + N-gluons } \\ \sqrt[]{ tt + qq + N-gluons } [Schulze]$

NB: N is a parameter in Rocket In perspective, for gluons: $N = 6 \implies 10860$ diags. $N = 7 \implies 168925$ diags. Successfully computed up to N=20

W + 3 jets

I. W + 3 jets measured at the Tevaton, but LO varies by more than a factor 2 for reasonable changes in scales

	W^{\pm}, TeV	W^+ , LHC	W^- , LHC
σ [pb], $\mu = 40$ GeV	74.0 ± 0.2	783.1 ± 2.7	481.6 ± 1.4
σ [pb], $\mu = 80 \text{ GeV}$	45.5 ± 0.1	515.1 ± 1.1	316.7 ± 0.7
σ [pb], $\mu = 160 \text{ GeV}$	29.5 ± 0.1	353.5 ± 0.8	217.5 ± 0.5

W + 3 jets

I. W + 3 jets measured at the Tevaton, but LO varies by more than a factor 2 for reasonable changes in scales

	W^{\pm}, TeV	W^+ , LHC	W^- , LHC
σ [pb], $\mu = 40 \text{ GeV}$	74.0 ± 0.2	783.1 ± 2.7	481.6 ± 1.4
σ [pb], $\mu = 80 \text{ GeV}$	45.5 ± 0.1	515.1 ± 1.1	316.7 ± 0.7
σ [pb], $\mu = 160~{\rm GeV}$	29.5 ± 0.1	353.5 ± 0.8	217.5 ± 0.5

- II. CDF data for W + n jets with n=1,2 is described exceptionally well by NLO QCD
 - \Rightarrow verify this for 3 and more jets



First application: W + 3 jets

III.W/Z + 3 jets of interest at the LHC, as one of the backgrounds to model-independent new physics searches using jets + MET

First application: W + 3 jets

III.W/Z + 3 jets of interest at the LHC, as one of the backgrounds to model-independent new physics searches using jets + MET

IV. Calculation highly non-trivial optimal testing ground

$$0 \to \bar{u} \, d \, g \, g \, g \, W^+ \quad \square$$

1203 +104 Feynman diagrams

 $0 \rightarrow \bar{u} \, d \, \bar{Q} \, Q \, g \, W^+$ 258 + 18 Feynman diagrams

Cross-section calculation

- Consider the NLO leading color approximation, keep n_f dependence exact (important for beta function) but neglect I/N_c^2 terms
- Real radiation part:
 - leading color tree level W+6 parton amplitudes computed recursively
 we use Catani-Seymour subtraction terms modified to deal with the minimal set of color structures needed at leading color
- Real + virtual implemented in the MCFM parton level integrator

Full-color NLO calculation done by Berger et al. '09 (see talk by Lance Dixon)

Define

$$\mathcal{R}_{\mathcal{O}} = \frac{\int \mathcal{O}(p) d\sigma_{LO}^{FC}(\mu, p)}{\int \mathcal{O}(p) d\sigma_{LO}^{LC}(\mu, p)}$$

Define

$$\mathcal{R}_{\mathcal{O}} = \frac{\int \mathcal{O}(p) d\sigma_{LO}^{FC}(\mu, p)}{\int \mathcal{O}(p) d\sigma_{LO}^{LC}(\mu, p)}$$

This turns out to be very stable, independent of factorization/renormalization and on the observable (e.g. bin of distribution)

$$\mathcal{R}_{\mathcal{O}}(\mu) \Rightarrow r$$

Define

$$\mathcal{R}_{\mathcal{O}} = \frac{\int \mathcal{O}(p) \mathrm{d}\sigma_{LO}^{\mathrm{FC}}(\mu, p)}{\int \mathcal{O}(p) \mathrm{d}\sigma_{LO}^{\mathrm{LC}}(\mu, p)}$$

This turns out to be very stable, independent of factorization/renormalization and on the observable (e.g. bin of distribution)

$$\mathcal{R}_{\mathcal{O}}(\mu) \Rightarrow r$$

Define our best approximation to the NLO result as

$$\mathcal{O}^{\mathrm{NLO}} = r \cdot \mathcal{O}^{\mathrm{NLO,LC}}$$

Leading color adjustment tested in W+1, W+2 jets and W+3 jets: always OK to 3 %

Define

$$\mathcal{R}_{\mathcal{O}} = \frac{\int \mathcal{O}(p) \mathrm{d}\sigma_{LO}^{\mathrm{FC}}(\mu, p)}{\int \mathcal{O}(p) \mathrm{d}\sigma_{LO}^{\mathrm{LC}}(\mu, p)}$$

This turns out to be very stable, independent of factorization/renormalization and on the observable (e.g. bin of distribution)

$$\mathcal{R}_{\mathcal{O}}(\mu) \Rightarrow r$$

Define our best approximation to the NLO result as

$$\mathcal{O}^{\mathrm{NLO}} = r \cdot \mathcal{O}^{\mathrm{NLO,LC}}$$

Leading color adjustment tested in W+1, W+2 jets and W+3 jets: always OK to 3 %

Other O(1%) effects neglected:

- CKM set to unity $\Rightarrow \sim -1\%$
- W treated onshell $\Rightarrow \sim +1\%$

CDF cuts

$$p_{\perp,j} > 20 \text{GeV} \qquad p_{\perp,e} > 20 \text{GeV} \qquad E_{\perp,\text{miss}} > 30 \text{GeV}$$
$$|\eta_e| < 1.1 \qquad M_{\perp,W} > 20 \text{GeV}$$
$$\mu_0 = \sqrt{p_{\perp,W}^2 + M_W^2} \qquad \mu = \mu_R = \mu_F = [\mu_0/2, 2\mu_0]$$

- PDFs: cteq6II and cteq6m
- CDF applies lepton-isolation cuts. This is a O(10%) effect. Leptonisolation has been corrected for (was not have been needed ...) No lepton isolation applied
- CDF uses JETCLU with R = 0.4, but this is not infrared safe, use a different jet-algorithm

Jet-algorithms

- CDF uses JETCLU which is not infrared safe
- NLO calculation with JETCLU not possible
- use e.g. SISCone and anti-kt algorithm which are IR safe
- can compare Leading order results for these algorithm (even if meaning of LO for JETCLU is questionable ...)

Leading order:

Algorithm	R	$E_{\perp}^{\rm jet} > 20 {\rm ~GeV}$	$E_{\perp}^{3 \mathrm{rdjet}} > 25 \mathrm{~GeV}$
JETCLU	0.4	$1.845(2)^{+1.101(3)}_{-0.634(2)}$	$1.008(1)^{+0.614(2)}_{-0.352(1)}$
SIScone	0.4	$1.470(1)^{+0.765(1)}_{-0.560(1)}$	$0.805(1)^{+0.493(1)}_{-0.281(1)}$
anti- k_{\perp}	0.4	$1.850(1)^{+1.105(1)}_{-0.638(1)}$	$1.010(1)^{+0.619(1)}_{-0.351(1)}$

SIScone: Salam & Soyez '07; anti-kt: Cacciari, Salam, Soyez '08

At LO anti-kt R =0.4 is closer to JETCLU

<u>Moral:</u>

precision comparison with theory require that experiments use IR-safe algorithms



$$\sigma_{W+3j}(p_{\perp,j} > 25 \,\text{GeV}) = (0.84 \pm 0.24) \,\text{pb}$$

CDF



$$\sigma_{W+3j}(p_{\perp,j} > 25 \,\text{GeV}) = (0.84 \pm 0.24) \,\text{pb}$$

CDF

	LO ^{LC}	LO ^{FC}			
SIS.	$0.89^{+0.55}_{-0.31}$	$0.81\substack{+0.50 \\ -0.28}$			
a-k _t	$1.12_{-0.39}^{+0.68}$	$1.01_{-0.35}^{+0.62}$			

 $\sigma_{W+3j}(p_{\perp,j} > 25 \,\text{GeV}) = (0.84 \pm 0.24) \,\text{pb}$

	LO ^{LC}	LO ^{FC}	$r = \frac{\mathrm{LO}^{\mathrm{FC}}}{\mathrm{LO}^{\mathrm{LC}}}$		
SIS.	$0.89^{+0.55}_{-0.31}$	$0.81_{-0.28}^{+0.50}$	0.91		
a-k _t	$1.12_{-0.39}^{+0.68}$	$1.01\substack{+0.62\\-0.35}$	0.91		

 $\sigma_{W+3j}(p_{\perp,j} > 25 \,\text{GeV}) = (0.84 \pm 0.24) \,\text{pb}$

	LO ^{LC}	LO ^{FC}	$r = \frac{\mathrm{LO}^{\mathrm{FC}}}{\mathrm{LO}^{\mathrm{LC}}}$	NLO ^{LC}		
SIS.	$0.89^{+0.55}_{-0.31}$	$0.81_{-0.28}^{+0.50}$	0.91	$1.01\substack{+0.05 \\ -0.17}$		
a-k _t	$1.12_{-0.39}^{+0.68}$	$1.01\substack{+0.62\\-0.35}$	0.91	$1.10^{+0.01}_{-0.13}$		

 $\sigma_{W+3j}(p_{\perp,j} > 25 \,\text{GeV}) = (0.84 \pm 0.24) \,\text{pb}$

	LO ^{LC}	LO ^{FC}	$r = \frac{\mathrm{LO}^{\mathrm{FC}}}{\mathrm{LO}^{\mathrm{LC}}}$	NLO ^{LC}	r · NLO ^{LC}	
SIS.	$0.89^{+0.55}_{-0.31}$	$0.81_{-0.28}^{+0.50}$	0.91	$1.01\substack{+0.05 \\ -0.17}$	$0.91\substack{+0.05 \\ -0.12}$	
a-k _t	$1.12_{-0.39}^{+0.68}$	$1.01\substack{+0.62\\-0.35}$	0.91	$1.10^{+0.01}_{-0.13}$	$1.00\substack{+0.01\\-0.12}$	

 $\sigma_{W+3j}(p_{\perp,j} > 25 \,\text{GeV}) = (0.84 \pm 0.24) \,\text{pb}$

	LO ^{LC}	LO ^{FC}	$r = \frac{\mathrm{LO}^{\mathrm{FC}}}{\mathrm{LO}^{\mathrm{LC}}}$	NLO ^{LC}	r · NLO ^{LC}	Berger et al. (LC)	
SIS.	$0.89^{+0.55}_{-0.31}$	$0.81_{-0.28}^{+0.50}$	0.91	$1.01\substack{+0.05 \\ -0.17}$	$0.91\substack{+0.05 \\ -0.12}$	$0.908^{+0.044}_{-0.142}$	
a-k _t	$1.12_{-0.39}^{+0.68}$	$1.01\substack{+0.62\\-0.35}$	0.91	$1.10^{+0.01}_{-0.13}$	$1.00\substack{+0.01 \\ -0.12}$		
$\sigma_{W+3j}(p_{\perp,j} > 25 \,\text{GeV}) = (0.84 \pm 0.24) \,\text{pb}$

	LO ^{LC}	LO ^{FC}	$r = \frac{\mathrm{LO}^{\mathrm{FC}}}{\mathrm{LO}^{\mathrm{LC}}}$	NLO ^{LC}	r · NLO ^{LC}	Berger et al. (LC)	Berger et al. (FC)
SIS.	$0.89^{+0.55}_{-0.31}$	$0.81\substack{+0.50 \\ -0.28}$	0.91	$1.01\substack{+0.05 \\ -0.17}$	$0.91\substack{+0.05 \\ -0.12}$	$0.908^{+0.044}_{-0.142}$	$0.882^{+0.057}_{-0.138}$
a-k _t	$1.12_{-0.39}^{+0.68}$	$1.01\substack{+0.62\\-0.35}$	0.91	$1.10^{+0.01}_{-0.13}$	$1.00^{+0.01}_{-0.12}$		

$$\sigma_{W+3j}(p_{\perp,j} > 25 \,\text{GeV}) = (0.84 \pm 0.24) \,\text{pb}$$

CDF

	LO ^{LC}	LO ^{FC}	$r = \frac{\mathrm{LO}^{\mathrm{FC}}}{\mathrm{LO}^{\mathrm{LC}}}$	NLO ^{LC}	r · NLO ^{LC}	Berger et al. (LC)	Berger et al. (FC)
SIS.	$0.89^{+0.55}_{-0.31}$	$0.81_{-0.28}^{+0.50}$	0.91	$1.01\substack{+0.05 \\ -0.17}$	$0.91\substack{+0.05 \\ -0.12}$	$0.908^{+0.044}_{-0.142}$	$0.882^{+0.057}_{-0.138}$
a-k _t	$1.12^{+0.68}_{-0.39}$	$1.01\substack{+0.62\\-0.35}$	0.91	$1.10_{-0.13}^{+0.01}$	$1.00^{+0.01}_{-0.12}$		

NB: errors are standard scale variation errors, statistical errors smaller

$$\sigma_{W+3j}(p_{\perp,j} > 25 \,\text{GeV}) = (0.84 \pm 0.24) \,\text{pb}$$

CDF

	LO ^{LC}	LO ^{FC}	$r = \frac{\mathrm{LO}^{\mathrm{FC}}}{\mathrm{LO}^{\mathrm{LC}}}$	NLO ^{LC}	r · NLO ^{LC}	Berger et al. (LC)	Berger et al. (FC)
SIS.	$0.89^{+0.55}_{-0.31}$	$0.81\substack{+0.50 \\ -0.28}$	0.91	$1.01\substack{+0.05 \\ -0.17}$	$0.91\substack{+0.05 \\ -0.12}$	$0.908^{+0.044}_{-0.142}$	$0.882^{+0.057}_{-0.138}$
a-k _t	$1.12_{-0.39}^{+0.68}$	$1.01\substack{+0.62\\-0.35}$	0.91	$1.10_{-0.13}^{+0.01}$	$1.00^{+0.01}_{-0.12}$		

NB: errors are standard scale variation errors, statistical errors smaller

 \Rightarrow agreement between independent calculations to within 3%

$$\sigma_{W+3j}(p_{\perp,j} > 25 \,\text{GeV}) = (0.84 \pm 0.24) \,\text{pb}$$

CDF

	LO ^{LC}	LO ^{FC}	$r = \frac{\mathrm{LO}^{\mathrm{FC}}}{\mathrm{LO}^{\mathrm{LC}}}$	NLO ^{LC}	r · NLO ^{LC}	Berger et al. (LC)	Berger et al. (FC)
SIS.	$0.89^{+0.55}_{-0.31}$	$0.81\substack{+0.50 \\ -0.28}$	0.91	$1.01\substack{+0.05 \\ -0.17}$	$0.91\substack{+0.05 \\ -0.12}$	$0.908^{+0.044}_{-0.142}$	$0.882^{+0.057}_{-0.138}$
a-k _t	$1.12_{-0.39}^{+0.68}$	$1.01\substack{+0.62\\-0.35}$	0.91	$1.10^{+0.01}_{-0.13}$	$1.00\substack{+0.01 \\ -0.12}$		

NB: errors are standard scale variation errors, statistical errors smaller

- \Rightarrow agreement between independent calculations to within 3%
- \Rightarrow leading color approximation works very well. After leading color adjustment procedure it is good to 3%

$$\sigma_{W+3j}(p_{\perp,j} > 25 \,\text{GeV}) = (0.84 \pm 0.24) \,\text{pb}$$

CDF

	LO ^{LC}	LO ^{FC}	$r = \frac{\mathrm{LO}^{\mathrm{FC}}}{\mathrm{LO}^{\mathrm{LC}}}$	NLO ^{LC}	r · NLO ^{LC}	Berger et al. (LC)	Berger et al. (FC)
SIS.	$0.89^{+0.55}_{-0.31}$	$0.81\substack{+0.50 \\ -0.28}$	0.91	$1.01\substack{+0.05 \\ -0.17}$	$0.91\substack{+0.05 \\ -0.12}$	$0.908^{+0.044}_{-0.142}$	$0.882^{+0.057}_{-0.138}$
a-k _t	$1.12_{-0.39}^{+0.68}$	$1.01\substack{+0.62\\-0.35}$	0.91	$1.10^{+0.01}_{-0.13}$	$1.00\substack{+0.01 \\ -0.12}$		

NB: errors are standard scale variation errors, statistical errors smaller

- \Rightarrow agreement between independent calculations to within 3%
- \Rightarrow leading color approximation works very well. After leading color adjustment procedure it is good to 3%
- \Rightarrow important (10% or more) differences due to different jet-algorithms. High precision comparison impossible if using different algorithms

Tevatron: sample distribution: E_{t,j3}

<u>NB</u>: CDF \Rightarrow JetCLU VERSUS NLO Theory \Rightarrow SISCone



- © agreement with CDF data (within currently large errors)
- \odot small K=1.0-1.1, reduced uncertainty: 50% (LO) \rightarrow 10% (NLO)
- \bigcirc first applications of new techniques to $2 \rightarrow 4$ LHC processes

Dual role of SM processes

Dual role of SM processes at colliders

- primary signals (apply signal cuts)
- unwanted background (apply background cuts)

Dual role of SM processes

Dual role of SM processes at colliders

- primary signals (apply signal cuts)
- unwanted background (apply background cuts)

Standard procedure

- study a given process with signal cuts \Rightarrow refine theoretical tools
- once good understanding of the process is achieved with signal cuts (e.g. low pt region) extrapolate to background cuts region (e.g. high pt)

Dual role of SM processes

Dual role of SM processes at colliders

- primary signals (apply signal cuts)
- unwanted background (apply background cuts)

Standard procedure

- study a given process with signal cuts \Rightarrow refine theoretical tools
- once good understanding of the process is achieved with signal cuts (e.g. low pt region) extrapolate to background cuts region (e.g. high pt)

How reliable is this procedure ?

Purpose of background cuts: push into corners of phase-space the SM process, therefore the robustness of the procedure is not assured. NLO QCD predictions for non-trivial processes can shed light on this.

W⁺ + 3 jets at the LHC

In the following: use highly non-trivial NLO calculation of W^++3 jets to illustrate/study this issue

<u>Signal-cuts setup (inspired by CMS studies):</u>

$$\begin{split} E_{\rm CM} &= 10 \,{\rm TeV} & E_{\perp,{\rm jet}} = 30 \,{\rm GeV} & E_{\perp,e} = 20 \,{\rm GeV} \\ E_{\perp,{\rm miss}} &= 15 \,{\rm GeV} & M_{\perp,W} = 30 \,{\rm GeV} & |\eta_e| < 2.4 & |\eta_{\rm jet}| < 3 \\ \mu_0 &= \sqrt{p_{\perp,W}^2 + M_W^2} & \mu = \mu_R = \mu_F = [\mu_0/2, 2\mu_0] \\ \end{split}$$
Jets: SIScone with R = 0.5; PDFs: cteq6II/cteq6m

Scale dependence



- scale dependence considerably reduced at NLO (both inclusive and exclusive)
- NLO tends to reduce crosssection
- because of very large scale dependence of LO, quoting a K-factor not very meaningful

Sample transverse energy distribution



Renormalization and factorization scale set to

$$\mu_0 = \sqrt{p_{T,W}^2 + m_{W^2}^2}$$

- with scale μ_0 : considerable change in shape between LO and NLO (extrapolation of LO from low p_t to high p_t would fail badly)
- but origin of the change in shape well understood: at high E_T , μ_0 is smaller than typical scales of the QCD branching \Rightarrow LO overshoots the result

Can one do a more sophisticated LO calculation?

Scale choice in V + jets

In a slightly different context, Bauer & Lange ('09) suggest that using a dynamical scale LO results do reproduce the NLO shapes

For W+2 jets they suggest $\mu^2 = M_W^2 + (m_{\rm hadr}/2)^2$

Similarly Berger et al ('09) suggest

$$\mu = \hat{H}_T = \sum_i p_{ti}$$
 (i = any parton)



Scale choice in V + jets

In a slightly different context, Bauer & Lange ('09) suggest that using a dynamical scale LO results do reproduce the NLO shapes



The idea of using dynamical scales is not new, it is implemented in all matrix element generators (CKKW local scales). Useful to compare NLO to those state-of-the art LO calculations.

Same transverse energy distribution

Local scale choice (CKKW):

- given a partonic event reconstruct a branching history: cluster partons into jets using k_t-algorithm
- at each branching the scale in the coupling to set to the relative k_t of the daughter partons
- local scale = CKKW scale choice, but no Sudakov reweighting, no parton shower

Same transverse energy distribution

Local scale choice (CKKW):

- given a partonic event reconstruct a branching history: cluster partons into jets using k_t-algorithm
- at each branching the scale in the coupling to set to the relative k_t of the daughter partons
- local scale = CKKW scale choice, but no Sudakov reweighting, no parton shower



Same transverse energy distribution

Local scale choice (CKKW):

- given a partonic event reconstruct a branching history: cluster partons into jets using k_t-algorithm
- at each branching the scale in the coupling to set to the relative kt of the daughter partons
- local scale = CKKW scale choice, but no Sudakov reweighting, no parton shower



- difference between "LO, local scale" and full Alpgen+Herwig indicative of importance of parton shower
- Iocal scale choice very close to Alpgen+Herwig which reproduces the NLO shape reasonably well

Other hadronic distributions



LO with local scale does a very reasonable job in reproducing shapes

<u>NB:</u> normalization of LO remains out of control. LO is normalized to NLO in above plots

Leptonic distributions



same conclusion holds for leptonic distributions

Leptonic distributions



Melnikov GZ '09

same conclusion holds for leptonic distributions

How solid (cut-independent) is this statement ? See what happens with different cuts. Consider two sets of cuts where W+3jet plays the role of unwanted background

<u>SUSY with R-parity</u>: e.g. gluino pair production, each decays into 2 jets and neutralino Typical signature: 4 jets and MET (no lepton)



<u>SUSY with R-parity</u>: e.g. gluino pair production, each decays into 2 jets and neutralino Typical signature: 4 jets and MET (no lepton)

Primary, irreducible background: $Z \rightarrow vv$ + 4 jets



<u>SUSY with R-parity</u>: e.g. gluino pair production, each decays into 2 jets and neutralino Typical signature: 4 jets and MET (no lepton)



Primary, irreducible background: $Z \rightarrow vv$ + 4 jets

Other SM background is W ($\rightarrow v \tau$ ($\rightarrow \overline{v}$ hadr.)) + 3 jets

<u>SUSY with R-parity</u>: e.g. gluino pair production, each decays into 2 jets and neutralino Typical signature: 4 jets and MET (no lepton)



Primary, irreducible background: $Z \rightarrow vv$ + 4 jets

Other SM background is W ($\rightarrow v \tau$ ($\rightarrow \overline{v}$ hadr.)) + 3 jets

Use peculiar properties of τ -jet to reject W+3jet background but

- I) limited efficiency for identifying τ -decays
- 2) $\sigma(W + 3 j) \sim 100 \sigma(Z + 4j)$

<u>SUSY with R-parity</u>: e.g. gluino pair production, each decays into 2 jets and neutralino Typical signature: 4 jets and MET (no lepton)



Primary, irreducible background: $Z \rightarrow vv$ + 4 jets

Other SM background is W ($\rightarrow v \tau$ ($\rightarrow \overline{v}$ hadr.)) + 3 jets

Use peculiar properties of τ -jet to reject W+3jet background but

- I) limited efficiency for identifying τ -decays
- 2) $\sigma(W + 3 j) \sim 100 \sigma(Z + 4j)$

 \Rightarrow important to consider this source of background as well

Atlas setup

Cuts designed by ATLAS to suppress W+3j background

$$\begin{split} p_{T,j} &> 50 \, \text{GeV} \qquad p_{T,j1} > 100 \, \text{GeV} \qquad p_{tl} < 20 \, \text{GeV} \\ E_{\text{T,miss}} &> \max(100 \, \text{GeV}, 0.2 \, H_T) \qquad H_T = \sum_j p_{T,j} + E_{\text{T,miss}} \\ S_T &> 0.2 \qquad |\eta_j| < 3 \end{split}$$

Yamazaki [ATLAS and CMS Col.] 0805.3883 Yamamoto [ATLAS Col.] 0710.3953

Atlas setup

Cuts designed by ATLAS to suppress W+3j background

 $p_{T,j} > 50 \,\text{GeV} \qquad p_{T,j1} > 100 \,\text{GeV} \qquad p_{tl} < 20 \,\text{GeV}$ $E_{T,\text{miss}} > \max(100 \,\text{GeV}, 0.2 H_T) \qquad H_T = \sum_j p_{T,j} + E_{T,\text{miss}}$ $S_T > 0.2 \qquad |\eta_j| < 3$



Yamazaki [ATLAS and CMS Col.] 0805.3883 Yamamoto [ATLAS Col.] 0710.3953

- each cut suppresses
 background by factor ~ 3
 without modifying the shape
- cut on collinear unsafe sphericity S_T not applied in the following study

Our calculation includes only the leptonic decay of the W (in e, μ or τ) but not the hadronic subsequent decay of τ . However

Our calculation includes only the leptonic decay of the W (in e, μ or τ) but not the hadronic subsequent decay of τ . However

- → kinematic cuts force τ to be highly boosted $\Rightarrow \tau$ -decay highly collimated
- $\Rightarrow \tau^+$ essentially decays only into $\pi^+(2/3 \text{ of energy})$ and ν (1/3 of energy)

Our calculation includes only the leptonic decay of the W (in e, μ or τ) but not the hadronic subsequent decay of τ . However

- → kinematic cuts force τ to be highly boosted $\Rightarrow \tau$ -decay highly collimated
- $\Rightarrow \tau^+$ essentially decays only into $\pi^+(2/3 \text{ of energy})$ and ν (1/3 of energy)



Theoretical robust approximation:

simulate the W decay as a perfect collinear branching with momentum fractions 2/3 (π^+) and 1/3 (v)

Primary observable is H_T (previously called M_{eff}) which 'measures' the SUSY scale:



Primary observable is H_T (previously called M_{eff}) which 'measures' the SUSY scale:



 universal enhancement (K-factor ~3) of LO without distorting the shape NB: same observable with cuts as shown before had K-factor ~ I

NLO effect similar to that of cuts but works in opposite direction

CMS style indirect lepton veto cut

How robust is the situation discussed in connection with ATLAS cuts ? Take a different set of cuts, which *targets the same physics*

CMS style indirect lepton veto cut

How robust is the situation discussed in connection with ATLAS cuts ? Take a different set of cuts, which *targets the same physics*

Indirect lepton veto = no explicit lepton veto, but other cuts force contribution from W+jets to become naturally small

 $p_{\rm T,j} > 30 {\rm GeV} \quad p_{\rm T,j1} > 180 {\rm GeV} \quad p_{\rm T,j2} > 110 {\rm GeV} \quad E_{\rm T,miss} > 200 {\rm GeV}$ $|\eta_{\rm lead \; jet}| < 1.7 \quad |\eta_{\rm other \; jets}| < 3 \qquad H_{\rm T,24} = \sum_{j=2}^{4} p_{\rm T,j} + E_{\rm T,miss} > 500 {\rm GeV}$

CMS Collaboration Journal Phys. G: Nucl. Part. Phys. 34 (2007) 995

CMS style indirect lepton veto cut

Primary search observables

distribution in transverse missing energy and total effective mass $H_{T,24}$



- NLO correction to cross-section small, K-factor ~ I
- shapes of LO mostly OK, but moderate shape distortion at high $H_{T,24}$

Lessons from W+3j study
NLO leads to reduction of scale uncertainties, residual uncertainty to total cross-section ~5% (~50% at LO)

- NLO leads to reduction of scale uncertainties, residual uncertainty to total cross-section ~5% (~50% at LO)
- but small corrections to total cross-section do not imply that corrections to distributions are small

- NLO leads to reduction of scale uncertainties, residual uncertainty to total cross-section ~5% (~50% at LO)
- In the section with the section of the section o
- this statement very much depends on the choice of scale at LO. Need to make good choice (e.g. CKKW procedure or other dynamical scale)

- NLO leads to reduction of scale uncertainties, residual uncertainty to total cross-section ~5% (~50% at LO)
- but small corrections to total cross-section do not imply that corrections to distributions are small
- this statement very much depends on the choice of scale at LO. Need to make good choice (e.g. CKKW procedure or other dynamical scale)
- Iarge (~100%) corrections for ATLAS setup, small corrections (~10%) for CMS cuts despite the fact that the cuts are designed for the same purpose

- NLO leads to reduction of scale uncertainties, residual uncertainty to total cross-section ~5% (~50% at LO)
- but small corrections to total cross-section do not imply that corrections to distributions are small
- this statement very much depends on the choice of scale at LO. Need to make good choice (e.g. CKKW procedure or other dynamical scale)
- Iarge (~100%) corrections for ATLAS setup, small corrections (~10%) for CMS cuts despite the fact that the cuts are designed for the same purpose
- these corrections are not correlated to the total cross-section

- NLO leads to reduction of scale uncertainties, residual uncertainty to total cross-section ~5% (~50% at LO)
- but small corrections to total cross-section do not imply that corrections to distributions are small
- this statement very much depends on the choice of scale at LO. Need to make good choice (e.g. CKKW procedure or other dynamical scale)
- Iarge (~100%) corrections for ATLAS setup, small corrections (~10%) for CMS cuts despite the fact that the cuts are designed for the same purpose
- these corrections are not correlated to the total cross-section
- Ill this emphasized the need to extend NLO corrections to other processes (Z+3j,W+4j ...)

Conclusions

A lot of physics to be learned from NLO QCD. Very fast evolving field, impressive progress in the last years, mainly driven by

- various inspiring/enlightening ideas
- In the second second
- many competitive groups (cross-checks/tuned comparisons) & more efficient computers

Conclusions

A lot of physics to be learned from NLO QCD. Very fast evolving field, impressive progress in the last years, mainly driven by

- various inspiring/enlightening ideas
- In the second second
- many competitive groups (cross-checks/tuned comparisons) & more efficient computers
- ⇒ development of practical tools for LHC phenomenology (BlackHat, CutTools, Rocket). Hopefully, we will soon have
- full automatization of codes (amplitudes, subtraction, phase space)
- public codes, as for leading order

Conclusions

A lot of physics to be learned from NLO QCD. Very fast evolving field, impressive progress in the last years, mainly driven by

- various inspiring/enlightening ideas
- In the second second
- many competitive groups (cross-checks/tuned comparisons) & more efficient computers
- ⇒ development of practical tools for LHC phenomenology (BlackHat, CutTools, Rocket). Hopefully, we will soon have
- full automatization of codes (amplitudes, subtraction, phase space)
- public codes, as for leading order

NLO QCD will provide solid basis for a successful program at the LHC