

*Atmospheric neutrinos  
(mostly results from Super-K)*

Takaaki Kajita

ICRR and IPMU, Univ. of Tokyo

# Outline

- Introduction
- Flux calculation
- Recent atmospheric neutrino data and ( $\Delta m_{23}^2$ ,  $\sin^2 2\theta_{23}$ )
- 3 flavor oscillation analyses and the future prospects
- Summary

# Introduction

Super-K @Neutrino 98

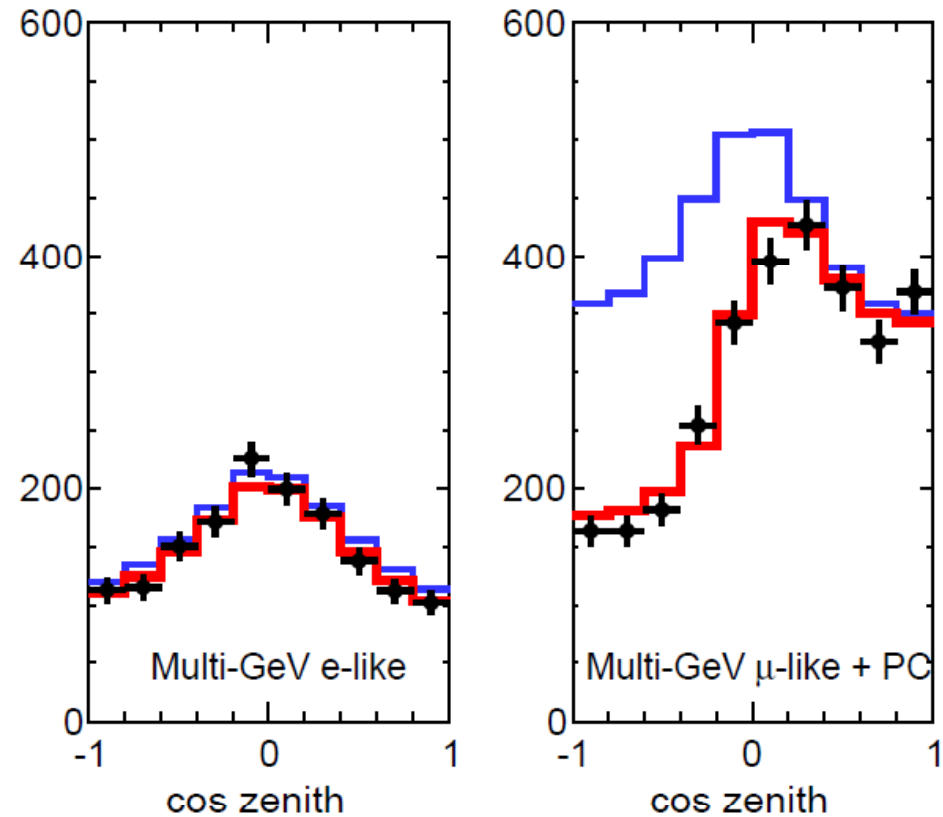
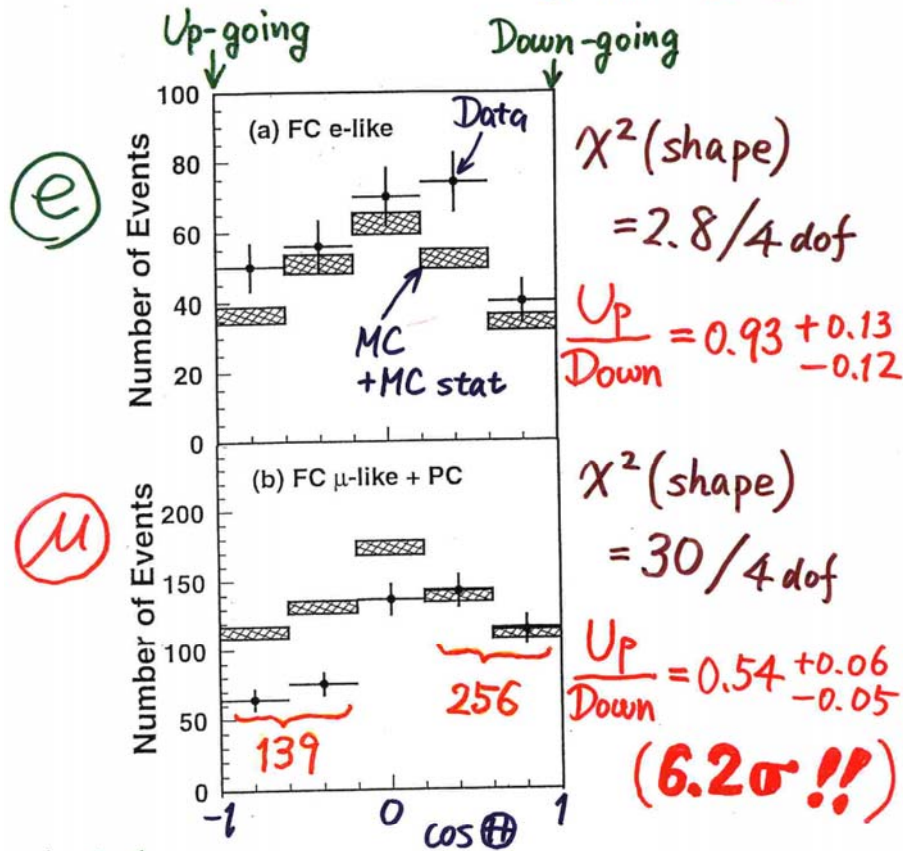
Super-K 2010

Zenith angle dependence  
(Multi-GeV)

535 day data

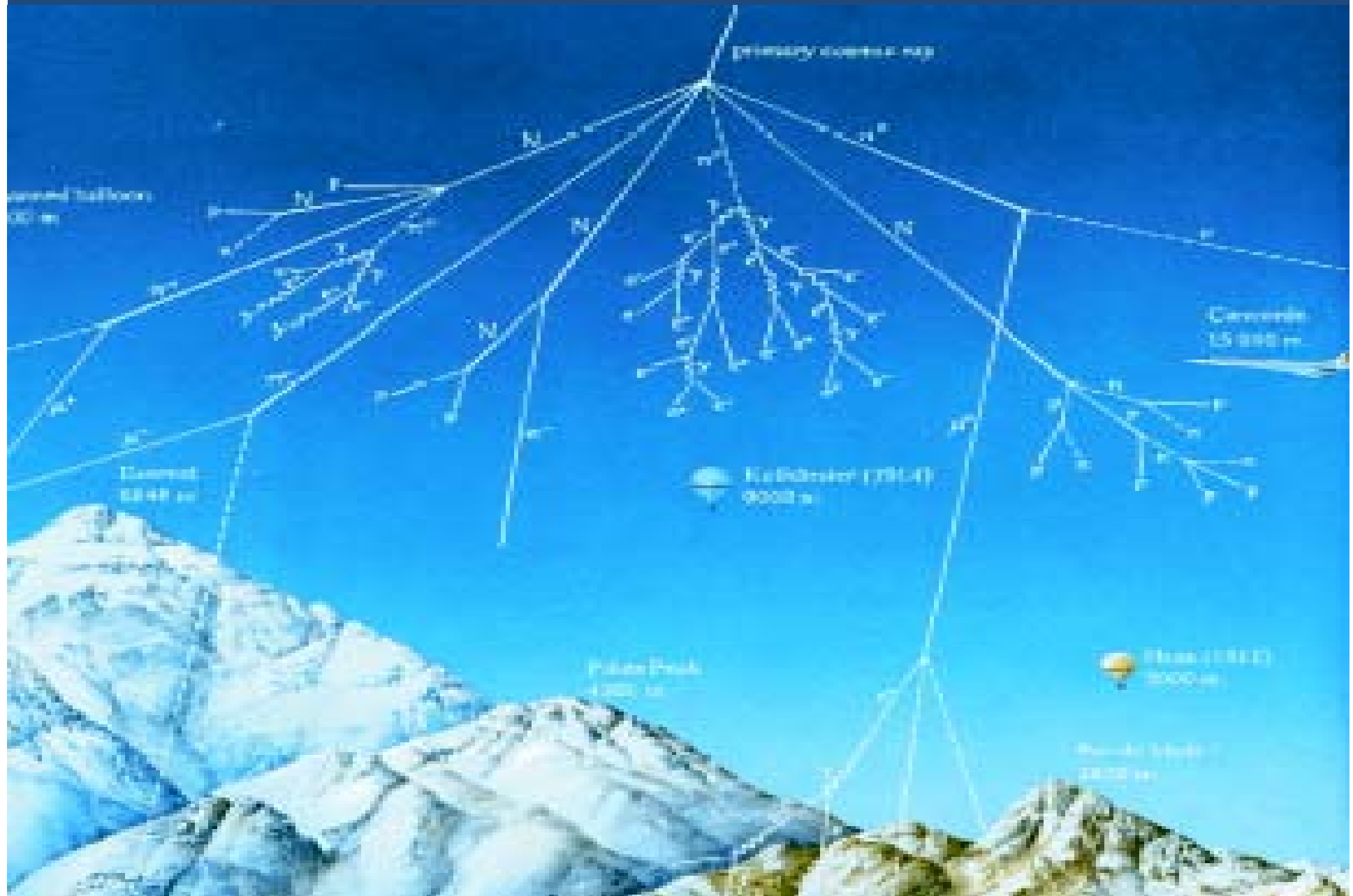
2806 day data

More than factor of 5 higher stat.



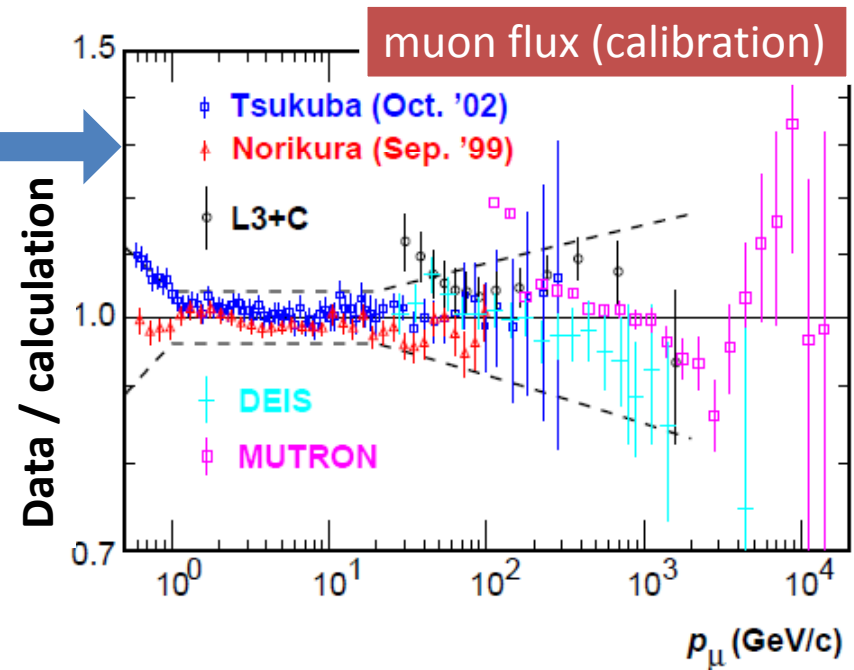
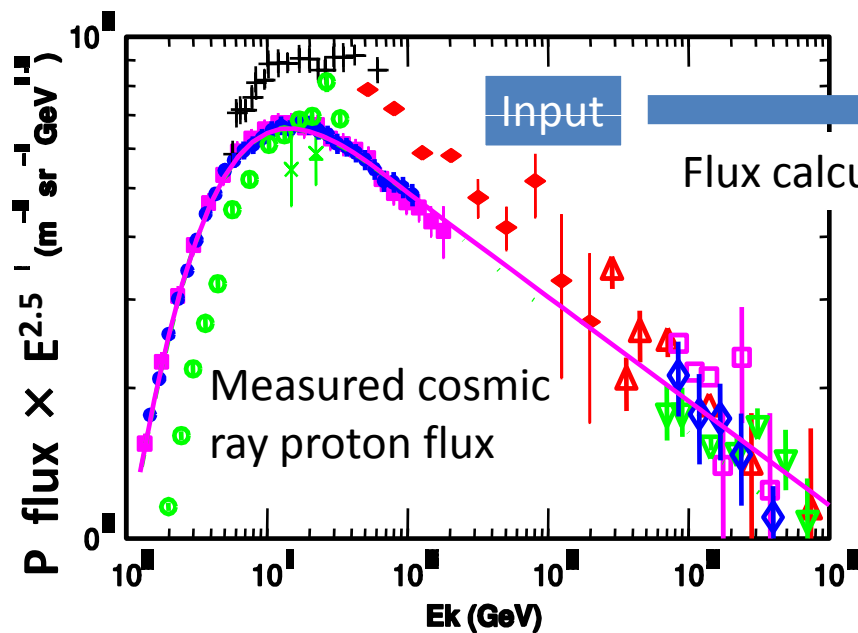
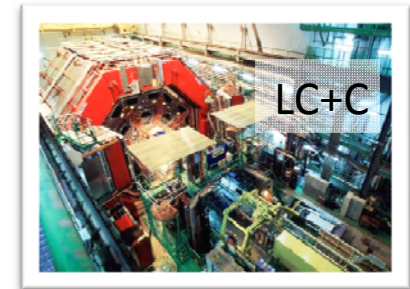
Would like to discuss most updated atmospheric neutrino analysis from Super-K.

# Flux calculation



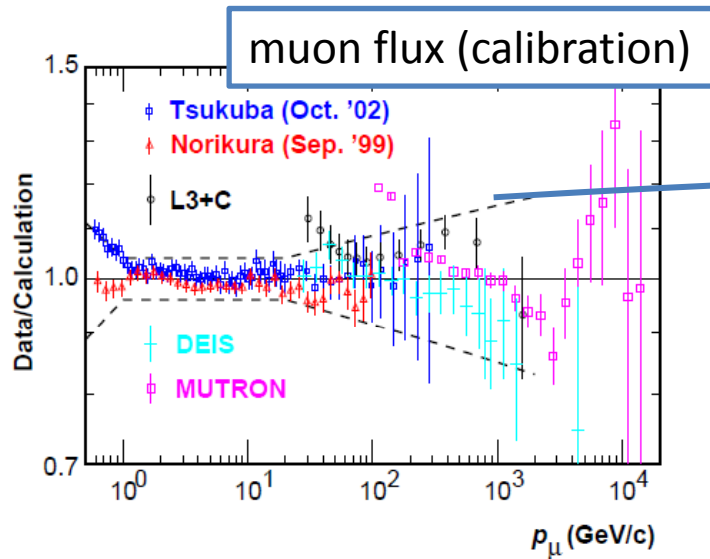
# Precise cosmic ray flux measurements and flux calculation

After the discovery of oscillations, experiments have been carried out to accurately measure the cosmic ray flux, which are essential inputs to the flux calculation.

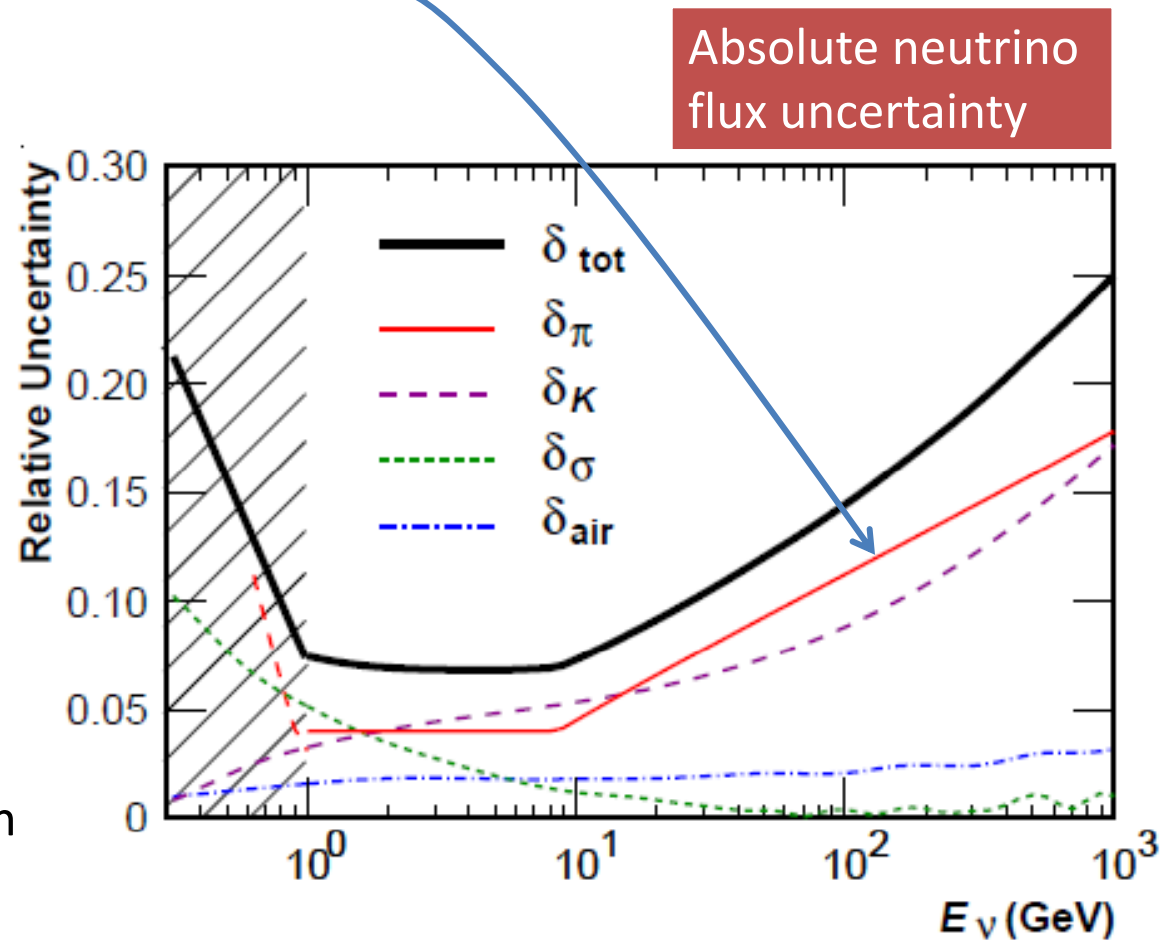


# Systematic errors in the absolute flux

Honda et al., astro-ph/0611418

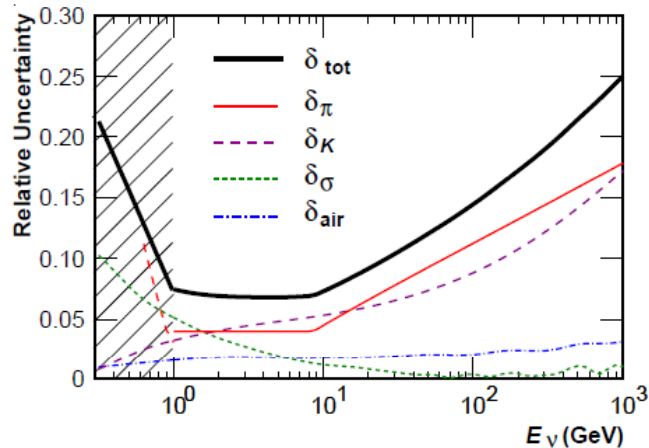


Better than 10% between 1 and 10 GeV.



# Flux calculation update: Motivation

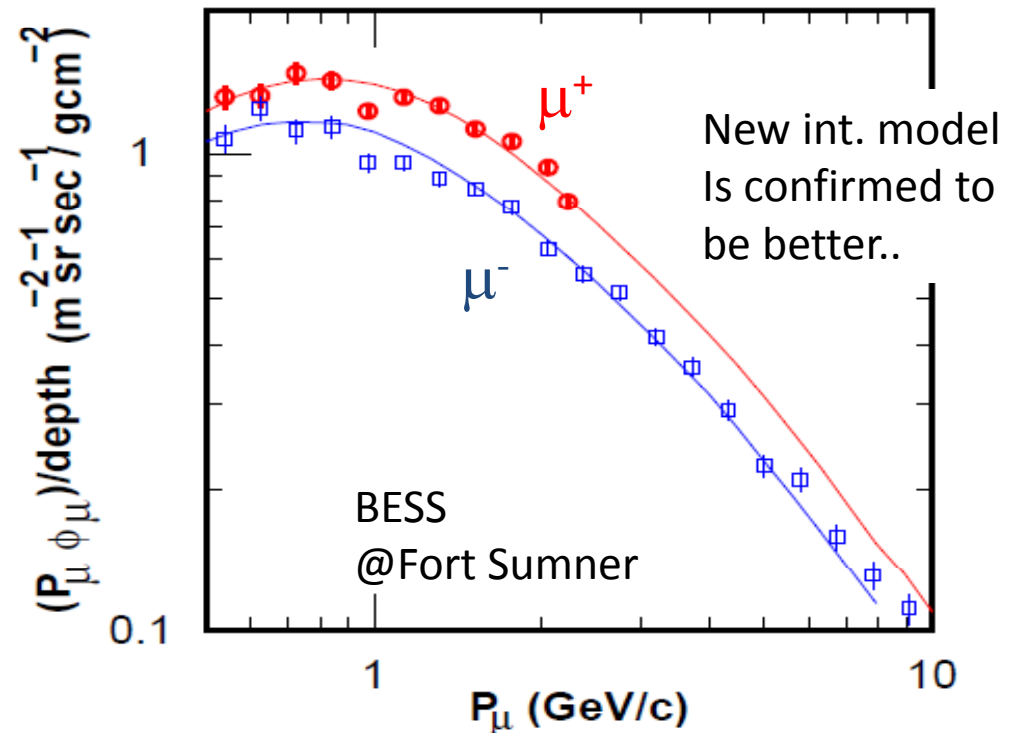
M. Honda et al., work in progress



In the previous calculation,  $\mu$  flux measurements at ground level and mountain altitude (2770 meters) were used. However, these  $\mu$ 's are not very useful to calibrate the sub-GeV neutrino flux due to the  $\mu$  energy loss (2GeV) before reaching the ground.

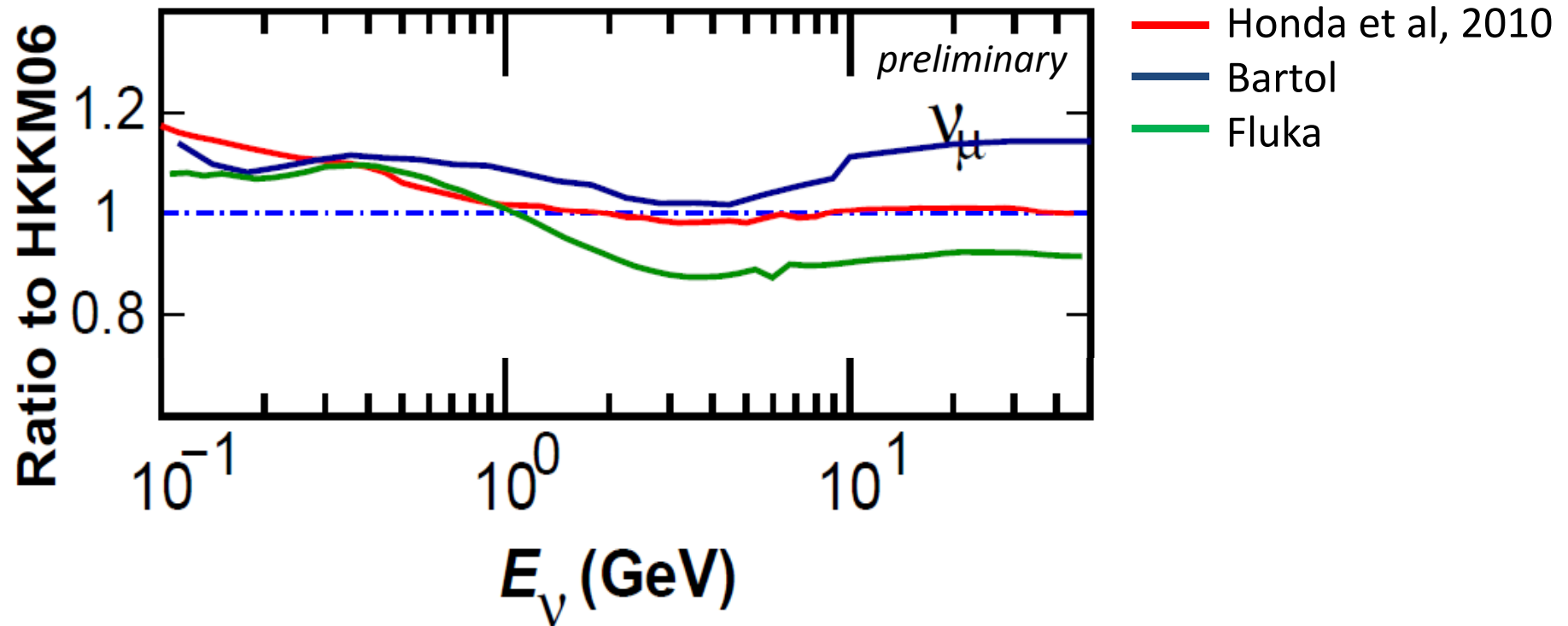
Update 1: Adopting recent hadronic interaction code (JAM) dedicated to the GeV energy range

Update 2: Calibration with balloon altitude muon flux data (5 – 26 g/cm<sup>2</sup>)



# Flux calculation update

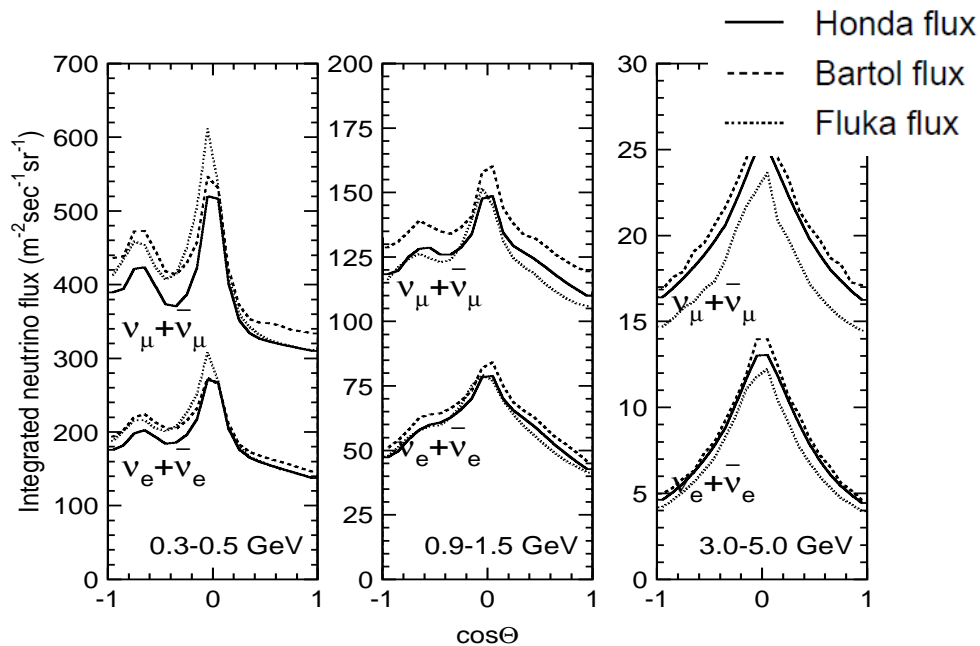
M. Honda et al., work in progress



The new flux by Honda et al. is essentially identical to the previous one (as should be).  
However, below 1 GeV the new calculation predicts a slightly higher flux.  
New syst. error still to be evaluated

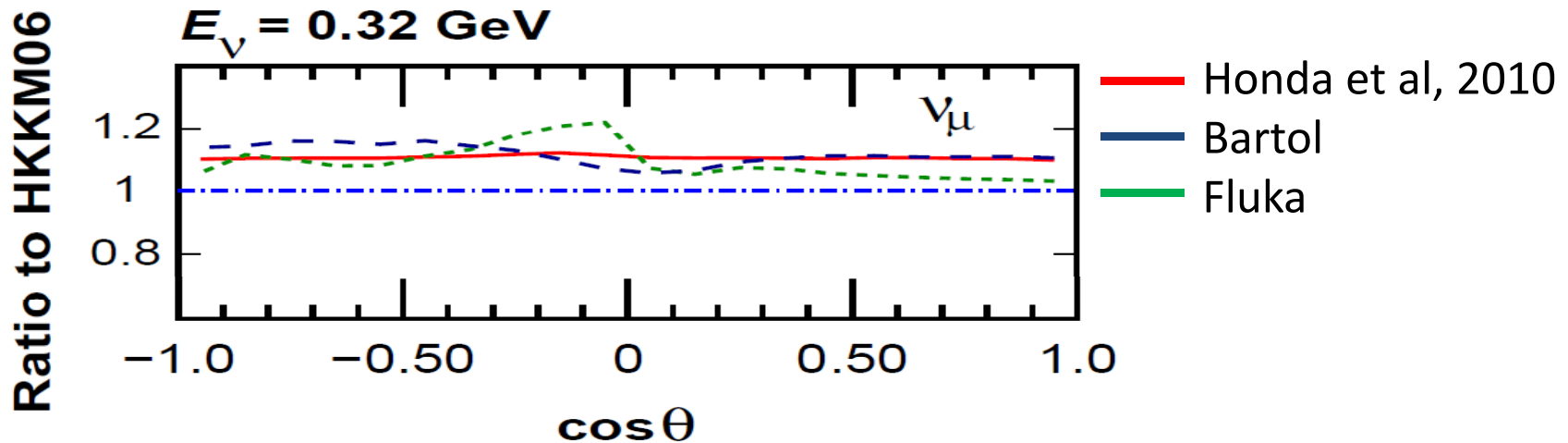


# Other and more important systematic errors in the flux: zenith angle

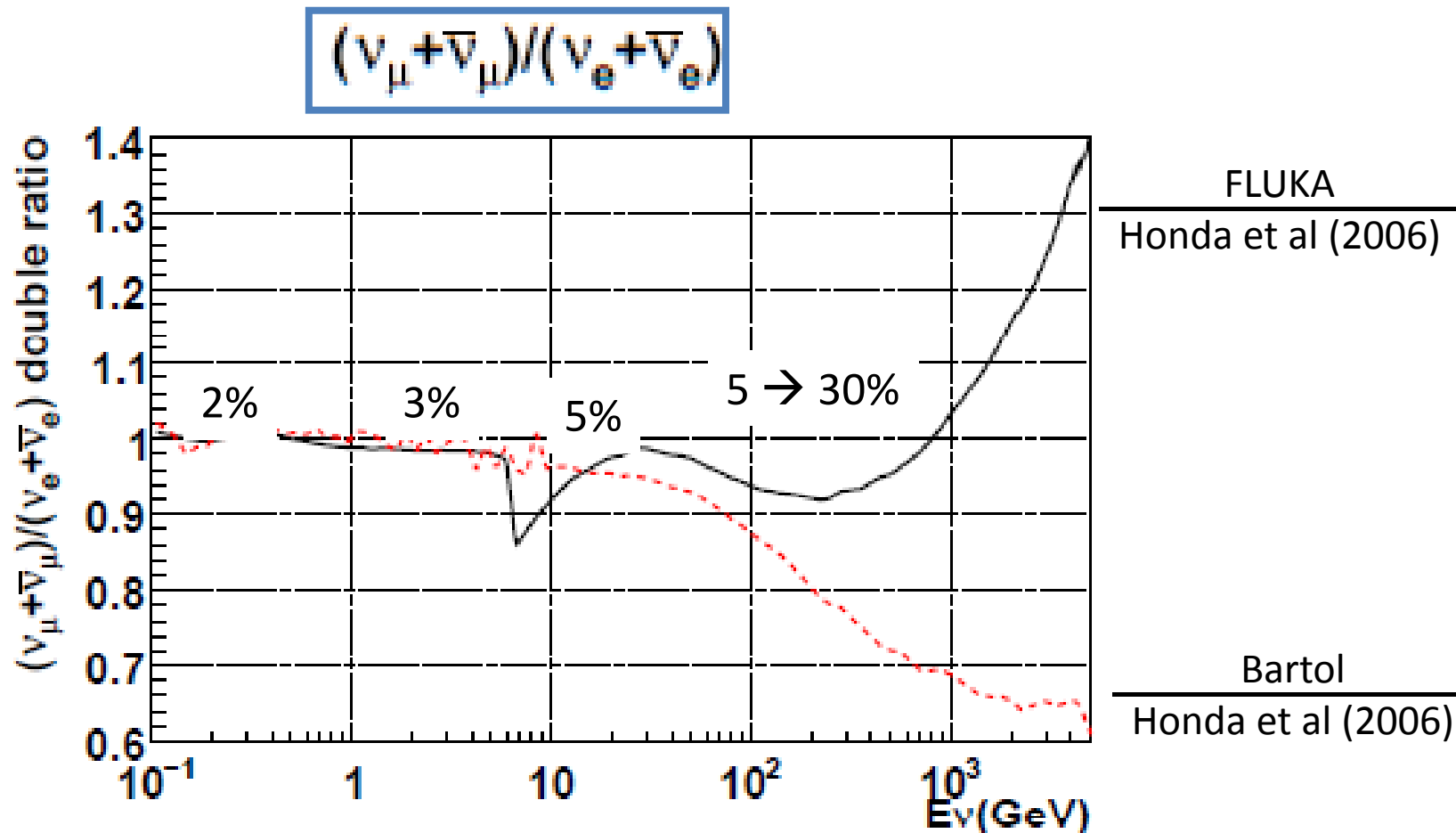


Up/Down uncertainty in the **lepton (muon)** zenith angle distribution (due to the flux uncertainty):

Energy range ( $\mu$ -like)	Uncertainty
< 0.4 GeV/c	0.3 %
0.4 – 1.33 GeV	0.5%
> 1.33 GeV (fully contained)	0.2%



# Other and more important systematic errors in the flux: flavor ratio

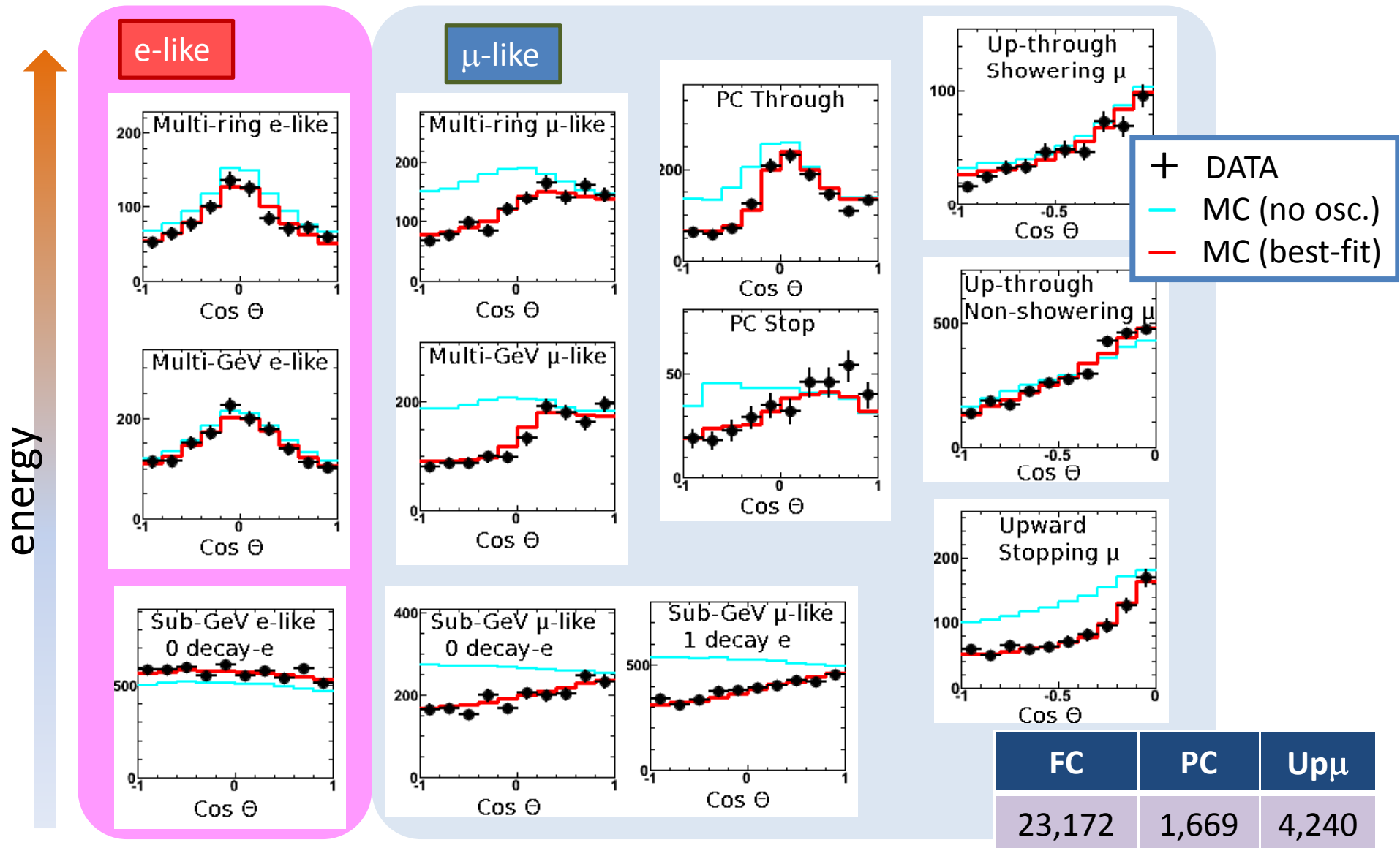


# Recent atmospheric neutrino data and $(\Delta m_{23}^2, \sin^2 2\theta_{23})$

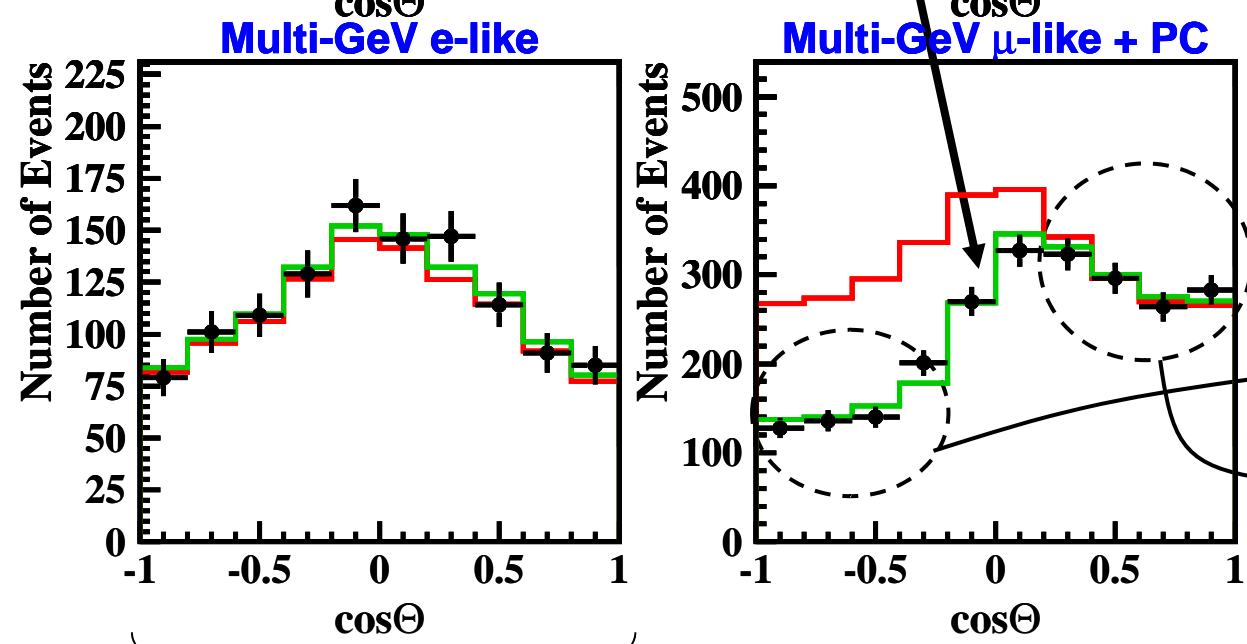
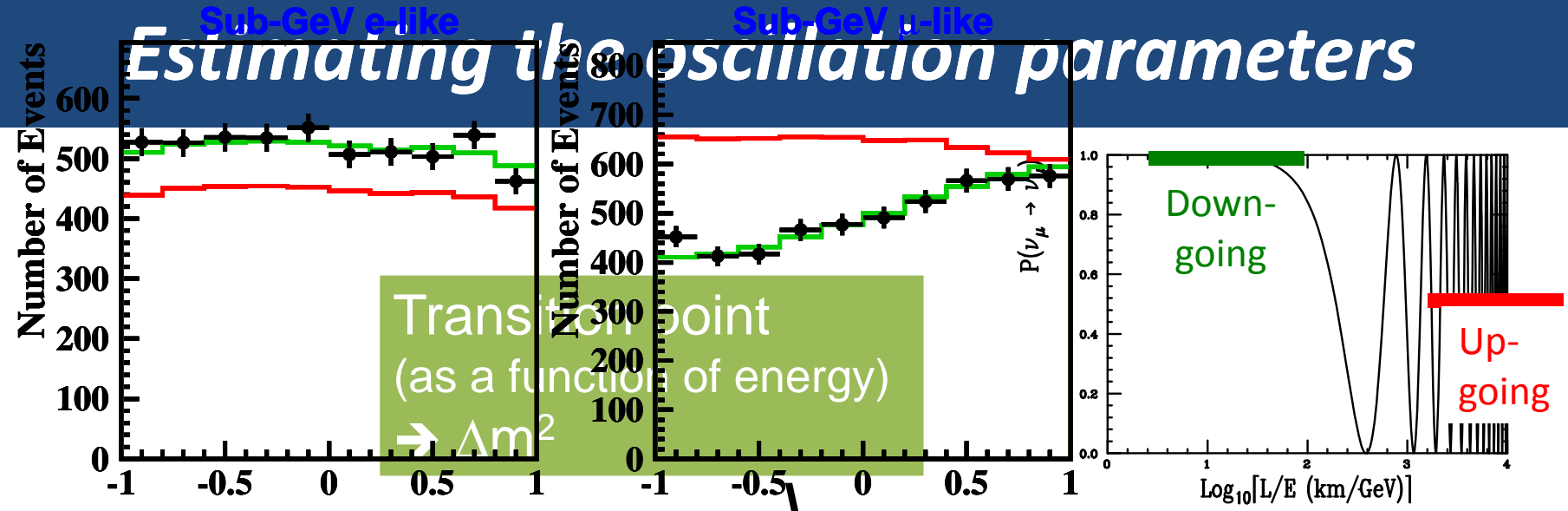


# Present Super-K atmospheric neutrino data

Super-K-I+II+III (2806 days (173kton·yr) for FC+PC, 3109 days for up- $\mu$ )



# Estimating the oscillation parameters



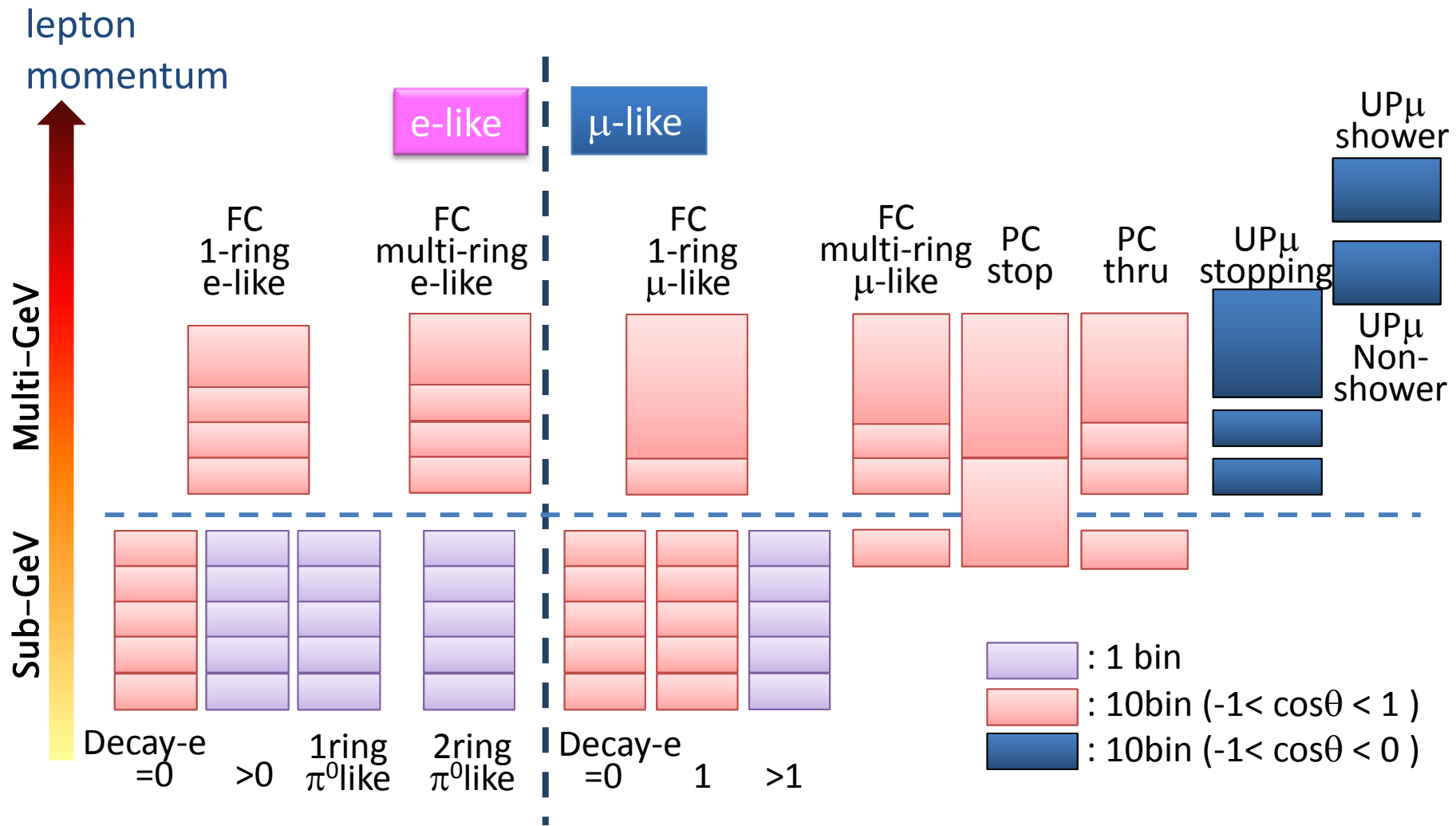
$$\frac{Up}{Down} = 1 - \sin^2 2\theta$$

Accurate measurement possible due to small syst. in up/down ( $\sim 1\%$ )

Confirmation of non-oscillated flux

# Oscillation analysis

(SK-I+II+III combined analysis)



Total Number of bins: 420 x 3 (SK1~3)

# Definition of $\chi^2$

$$L(N_{\text{exp}}, N_{\text{obs}}) = \prod_{n=1}^{1260} \frac{\exp(-N_{\text{exp}}^n) (N_{\text{exp}}^n)^{N_{\text{obs}}^n}}{N_{\text{obs}}^n!} \times \prod_{i=1}^{123} \exp\left(\frac{-\varepsilon_i^2}{2\sigma_i^2}\right)$$

Number of data bins (in the final anal., → 420)
Number of syst error terms

Poisson with systematic errors

$$\chi^2 \equiv -2 \ln \left( \frac{L(N_{\text{exp}}, N_{\text{obs}})}{L(N_{\text{obs}}, N_{\text{obs}})} \right) = \sum_{n=1}^{1260} \left[ 2(N_{\text{exp}}^n - N_{\text{obs}}^n) + 2N_{\text{obs}}^n \ln \left( \frac{N_{\text{obs}}^n}{N_{\text{exp}}^n} \right) \right] + \sum_{i=1}^{123} \left( \frac{\varepsilon_i}{\sigma_i} \right)^2$$

$$N_{\text{exp}} = N_{\text{MC}} \cdot P(\nu_{\mu} \rightarrow \nu_{\mu} \text{ (for CC } \nu_{\mu})) \cdot \left( 1 + \sum_{j=1}^{70} f_j \cdot \varepsilon_j \right)$$

$N_{\text{obs}}$  : observed number of events

$N_{\text{exp}}$  : expectation from MC

$\varepsilon_i$  : systematic error term

$\sigma_i$  : sigma of systematic error

$\chi^2$  minimization at each parameter point ( $\Delta m^2$ ,  $\sin^2 2\theta$ , ...).

Method ( $\chi^2$  version): G.L.Fogli et al., PRD 66, 053010 (2002).

# Syst. error terms

$\nu_{\text{atm}}$  flux

$\nu$  interaction

Reconstruction

Others

# 33~61

parameters are  
evaluated for  
each SK period.

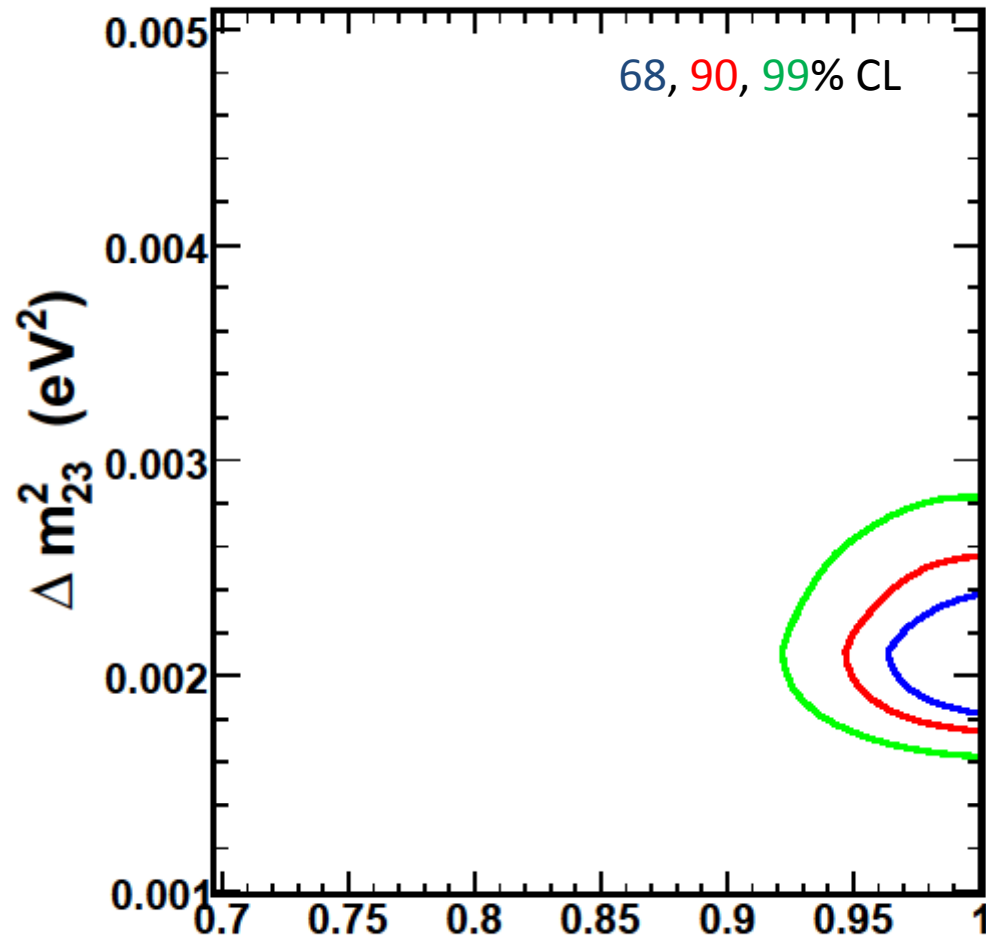
Total = 123 terms

1. absolute normalization ( $<1\text{GeV}$ )
2. absolute normalization ( $>1\text{GeV}$ )
3.  $(\nu_{\mu}+\text{anti-}\nu_{\mu})/(\nu_e+\text{anti-}\nu_e)$  ( $E_{\nu}<1\text{GeV}$ )
4.  $(\nu_{\mu}+\text{anti-}\nu_{\mu})/(\nu_e+\text{anti-}\nu_e)$  ( $1<E_{\nu}<10\text{GeV}$ )
5.  $(\nu_{\mu}+\text{anti-}\nu_{\mu})/(\nu_e+\text{anti-}\nu_e)$  ( $E_{\nu}>10\text{GeV}$ )
6.  $\nu_e/\text{anti-}\nu_e$  ( $E_{\nu}<1\text{GeV}$ )
7.  $\nu_e/\text{anti-}\nu_e$  ( $1<E_{\nu}<10\text{GeV}$ )
8.  $\nu_e/\text{anti-}\nu_e$  ( $E_{\nu}>10\text{GeV}$ )
9.  $\nu_{\mu}/\text{anti-}\nu_{\mu}$  ( $E_{\nu}<1\text{GeV}$ )
10.  $\nu_{\mu}/\text{anti-}\nu_{\mu}$  ( $1<E_{\nu}<10\text{GeV}$ )
11.  $\nu_{\mu}/\text{anti-}\nu_{\mu}$  ( $E_{\nu}>10\text{GeV}$ )
12. up/down
13. horizontal/vertical
14.  $K/\pi$
15.  $L_{\nu}$  (production height)
16. sample-by-sample FC Multi-GeV
17. sample-by-sample PC + UPstop
18.  $M_A$  in CCQE, single- $\pi$
19. CCQE (model dependence)
20. CCQE (anti- $\nu/\nu$ )
21. CCQE ( $\mu/e$ )
22. single- $\pi$  (cross section)
23. single- $\pi$  (anti- $\nu/\nu$ )
24. single- $\pi(\pi^0/\pi^{\pm})$
25. DIS(model dependence)
26. DIS (cross section)
27. coherent  $\pi$  (cross section)
28. NC/CC
29. nuclear effect in  $^{16}\text{O}$
30. nuclear effect (pion spectrum)
31. CC $\nu$  interaction cross section
32. hadron sim. (NC contami. in FC)
33. Solar activity
34. FC reduction
35. PC reduction
36. UP $\mu$  reduction
37. FC/PC separation
38. Normalization of PC stop/thru(top)
39. Normalization of PC stop/thru(barrel)
40. Normalization of PC stop/thru(bottom)
41. non- $\nu$  BG (flasher)
42. non- $\nu$  BG (cosmic-ray  $\mu$ )
43. BG subtraction of Upthru (shower)  $\mu$
44. BG subtraction of Upthru (non-shower)  $\mu$
45. BG subtraction of UPstop  $\mu$
46. UP $\mu$  stop/thru separation
47. UP $\mu$  non-shower/shower separation
48. ring separation
49. PID for single-ring
50. PID for multi-ring
51. energy calibration
52. energy cut for UPstop  $\mu$
53. up/down symmetry of energy calib.
54. non- $\nu_e$  BG in Multi-GeV 1-ring electron
55. non- $\nu_e$  BG in Multi-GeV m-ring electron
56. Likelihood of Multi-GeV m-ring e-like
57. Efficiency for 2-ring  $\pi^0$
58. number of event for 1-ring  $\pi^0$
59. Decay electron tagging
60. Fiducial volume
61. Up thru  $\uparrow$  length cut
62. Decay electron tagging from  $\pi^+$
63. Matter effect
64. Low- $q^2$  for DIS  $W<2\text{GeV}$
65. Low- $q^2$  for DIS  $W>2\text{GeV}$



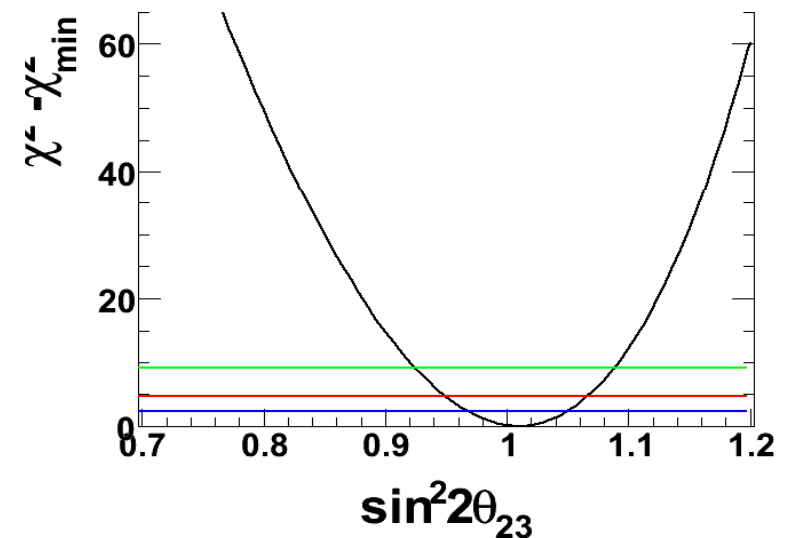
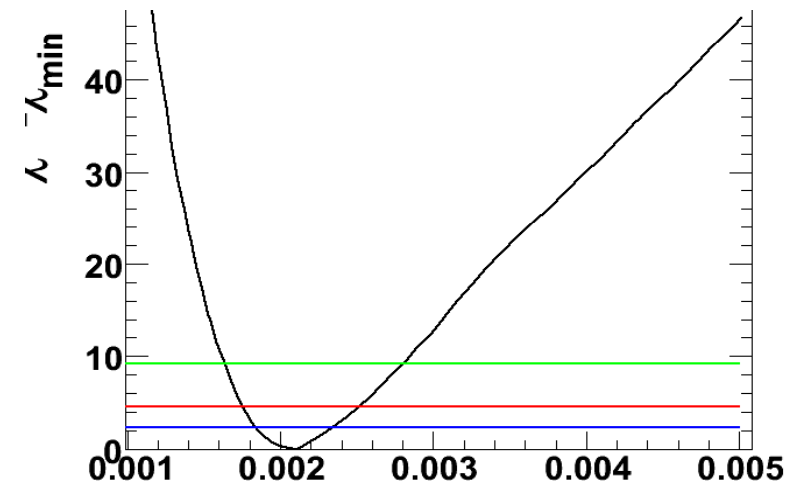
# $\nu_\mu \rightarrow \nu_\tau$ 2 flavor analysis (zenith angle)

SK-I+II+III



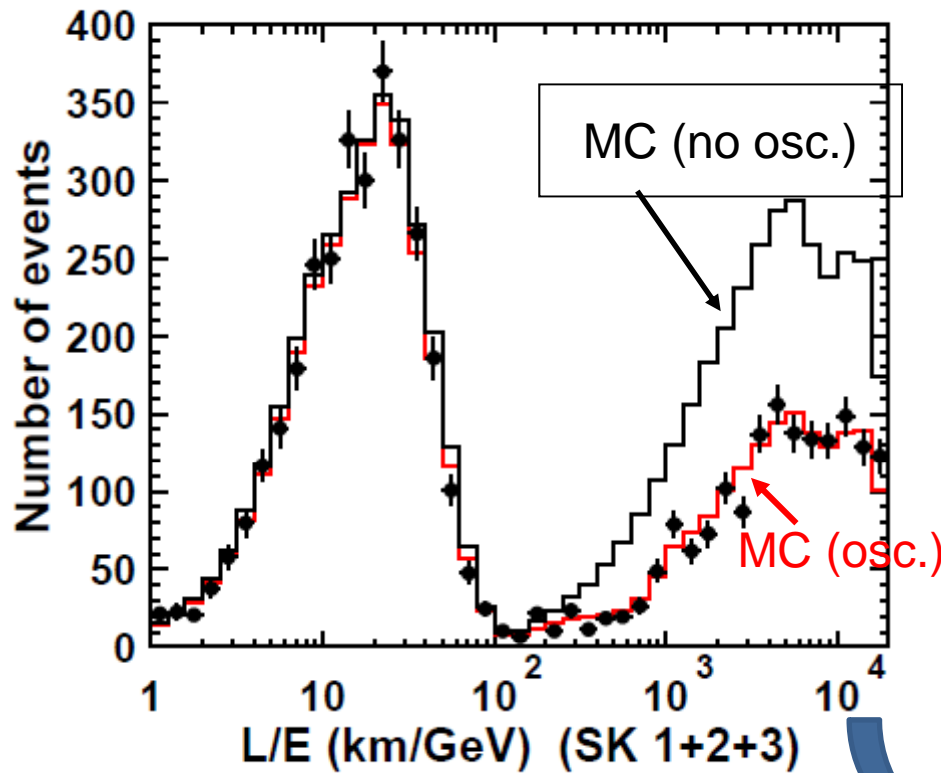
$1.7 \times 10^{-3} \text{ eV}^2 < \Delta m^2 < 2.6 \times 10^{-3} \text{ eV}^2$   
 $\sin^2 2\theta > 0.94$  at 90% CL

$\Delta\chi^2$  distributions



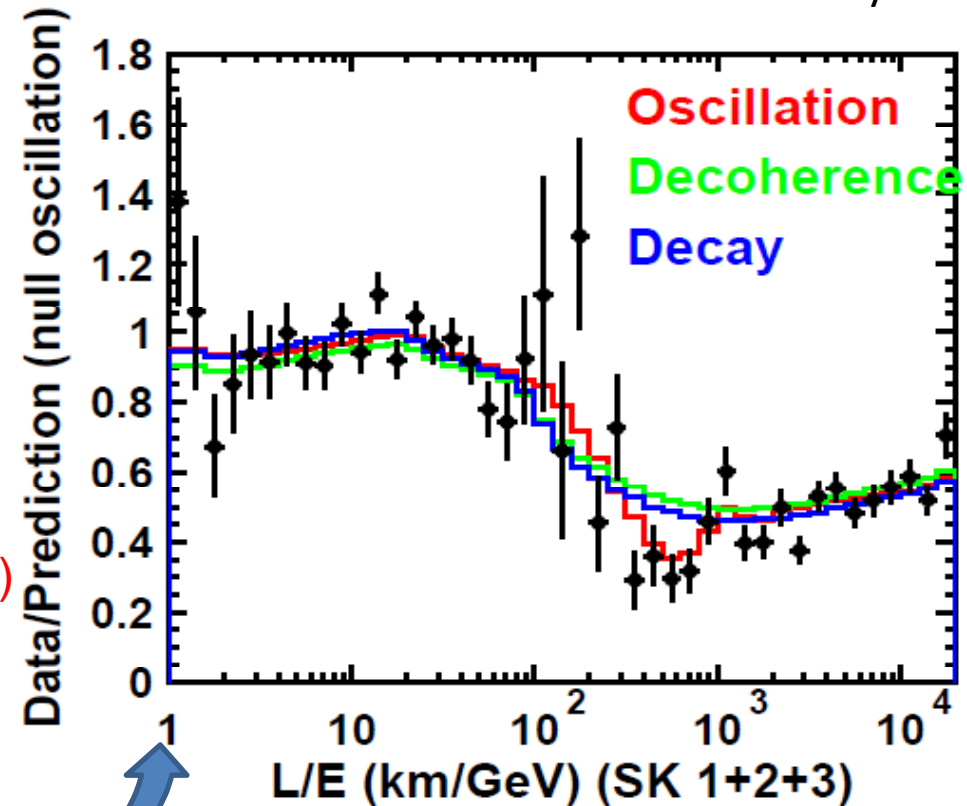
# *L/E distribution update with SK-I+II+III*

Preliminary



Mostly down-going

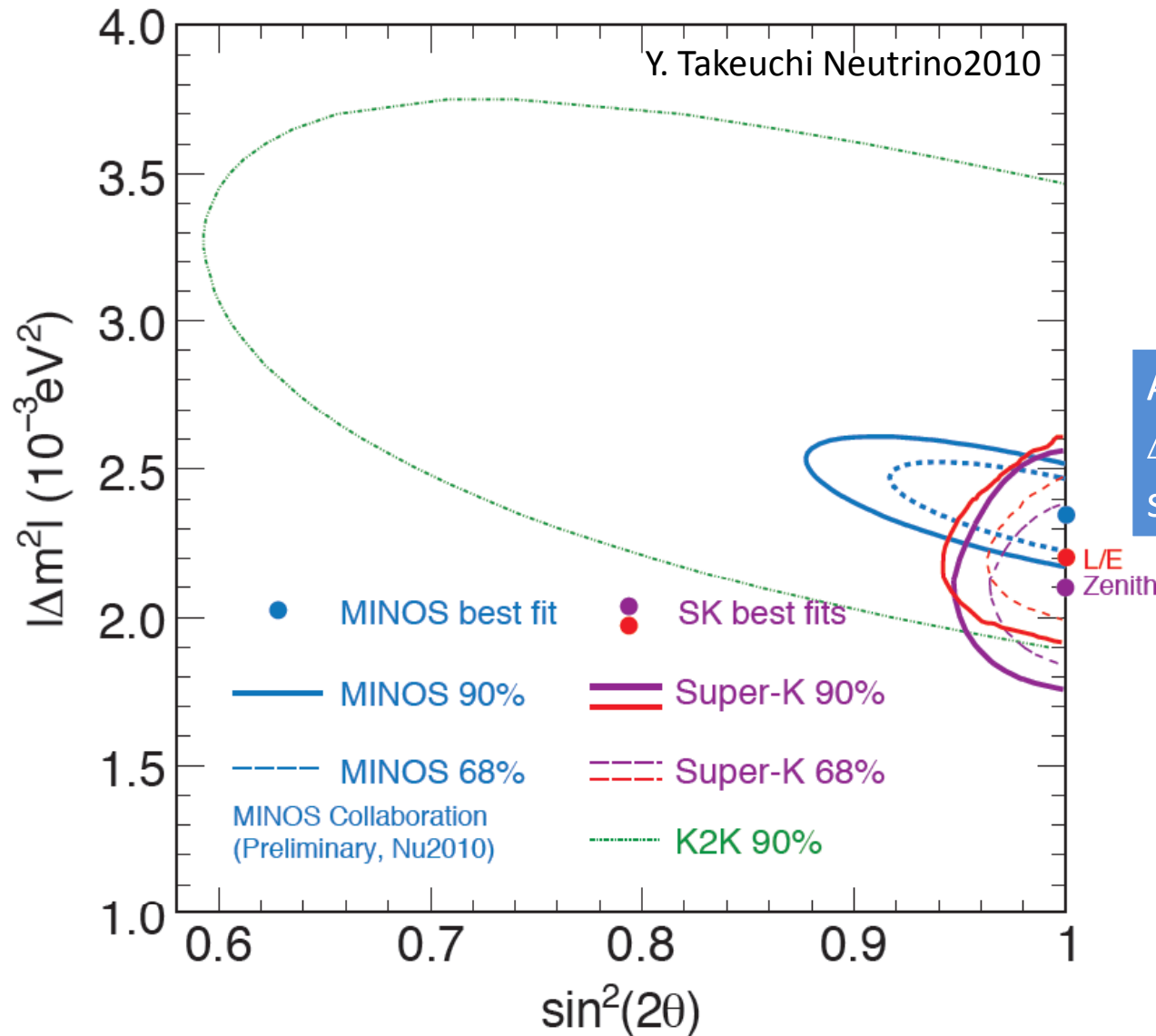
Mostly up-going



Neutrino decay disfavored ( $4.4\sigma$ )

Neutrino decoherence disfavored ( $5.4\sigma$ )

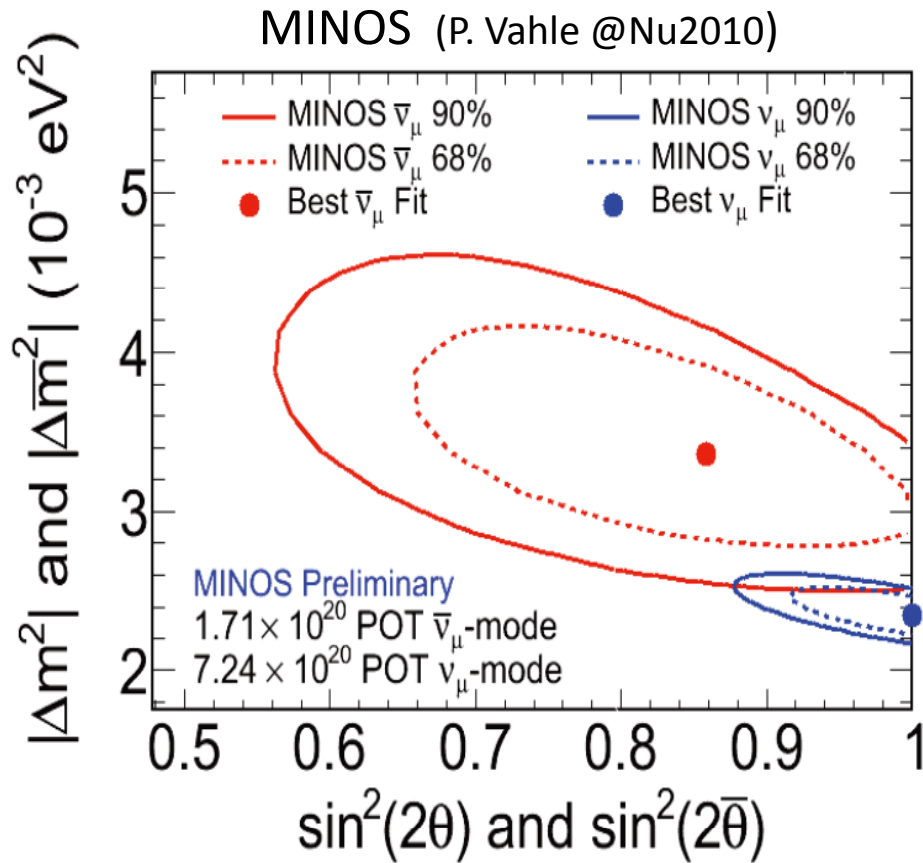
# Allowed parameter regions from atmospheric and long baseline experiments



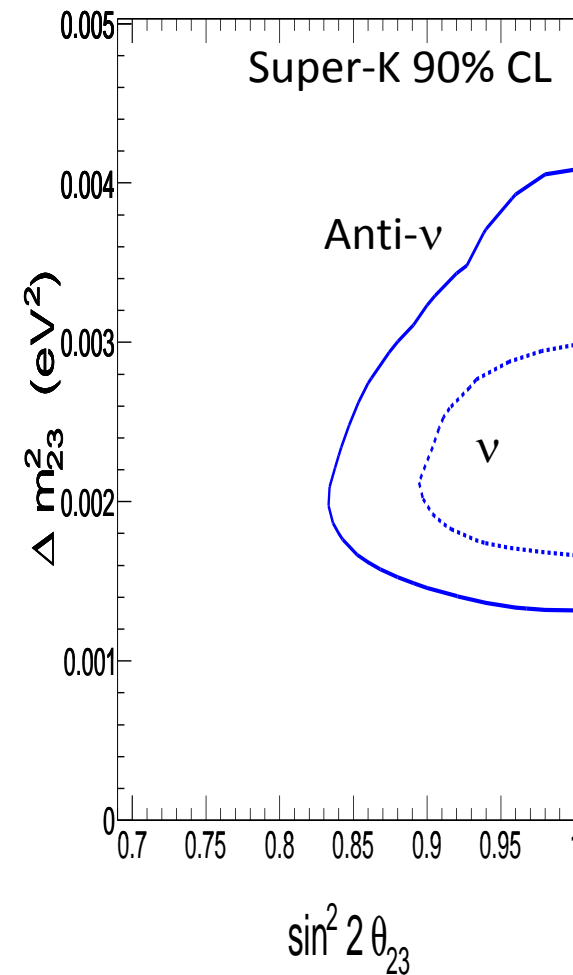
Accuracy:  
 $\Delta m^2$ : LBL,  
 $\sin^2 2\theta$ : still atm.

Consistent with  
maximal mixing!

# $(\Delta m_{23}^2, \sin^2 2\theta_{23})$ for $\nu$ 's and anti- $\nu$ 's ?



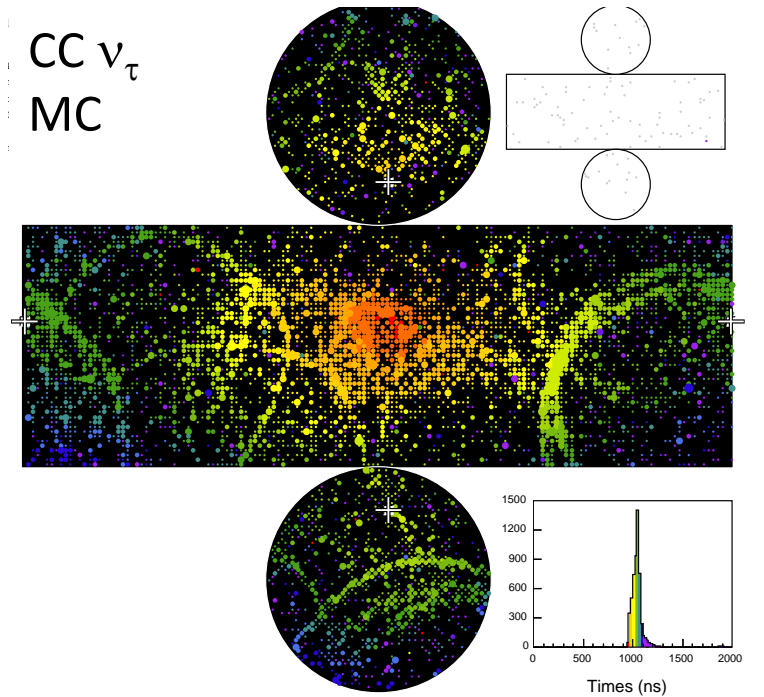
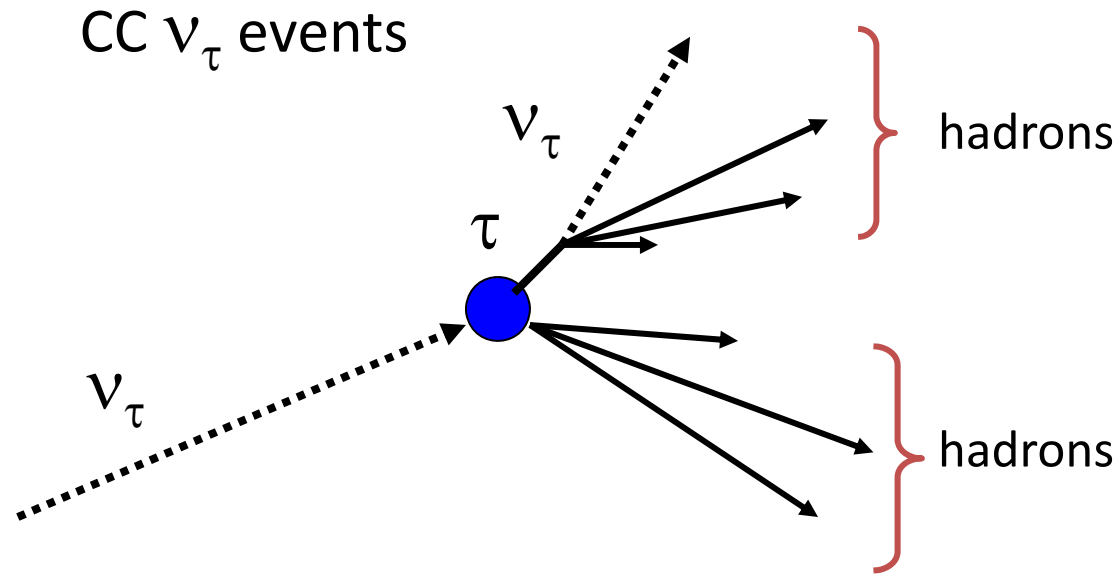
An oscillation analysis with  $(\Delta m_{23}^2, \sin^2 2\theta_{23}, \overline{\Delta m_{23}^2}, \overline{\sin^2 2\theta_{23}})$  with the zenith angle data.



# Search for CC $\nu_\tau$ events



# Search for CC $\nu_\tau$ events (SK-I)



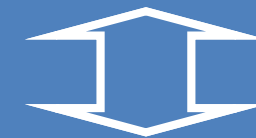
● Many hadrons . . . .  
 (But no big difference with other (NC) events. )

↳ BAD ⇒  $\tau$ -likelihood analysis

● Upward going only

↳ GOOD ⇒ Zenith angle

Only  $\sim 1.0$  CC  $\nu_\tau$   
 FC events/kton $\cdot$ yr



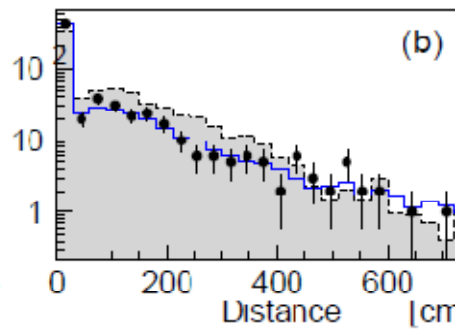
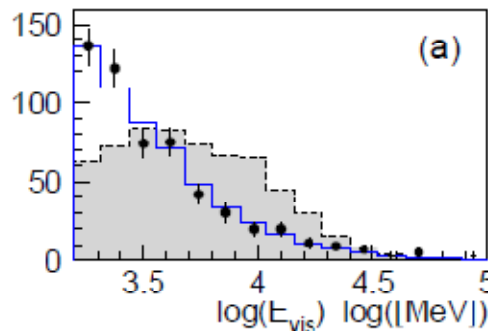
(BG (other  $\nu$  events)  
 $\sim 130$  ev./kton $\cdot$ yr)

# Selection of $\nu_\tau$ events

Pre-cuts:  $E(\text{visible}) > 1,33\text{GeV}$ , most-energetic ring = e-like

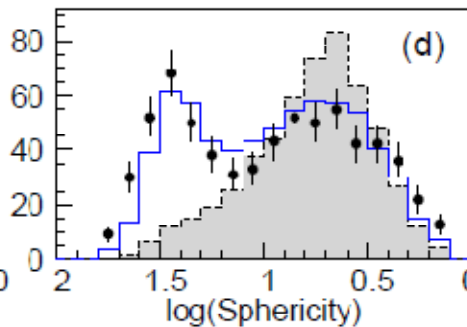
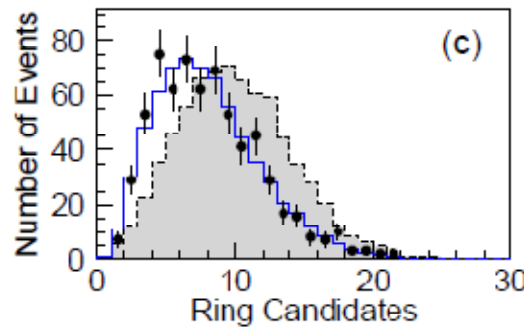


$E(\text{visible})$



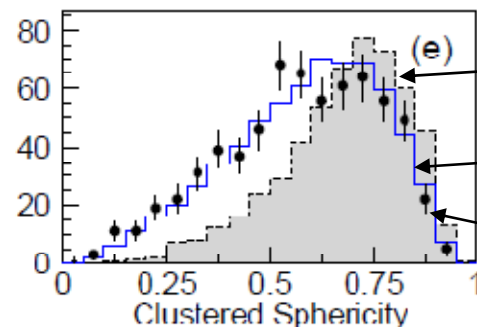
Max. distance between primary vertex and the decay-electron vertex

Number of ring candidates



Sphericity in the lab frame

Sphericity in the CM frame



$\nu_\tau$  MC

Atm. $\nu$  MC

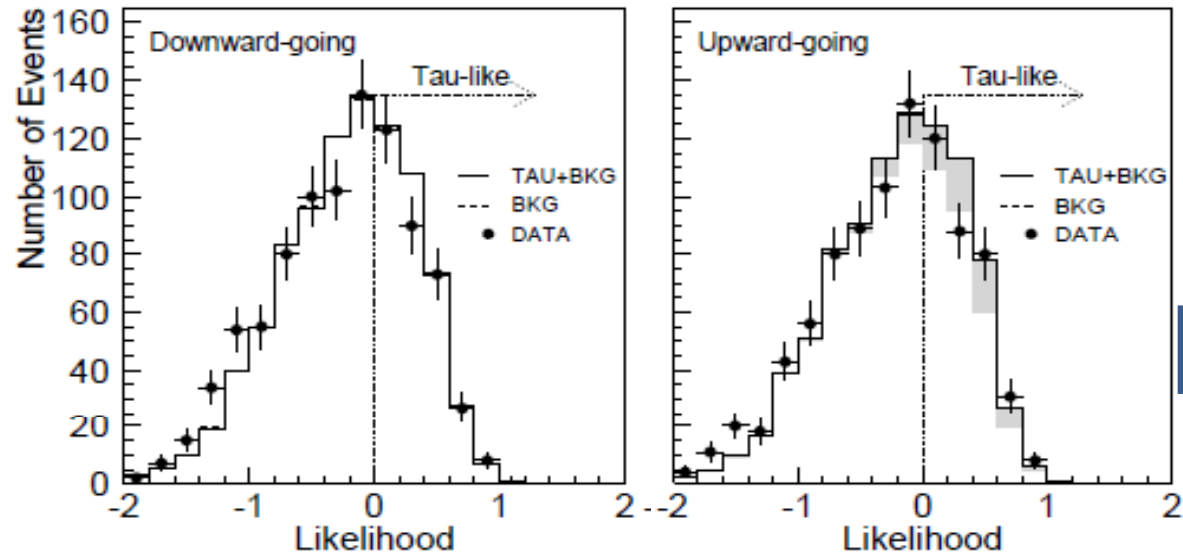
Data (downward-going)

# Likelihood / neural-net distributions

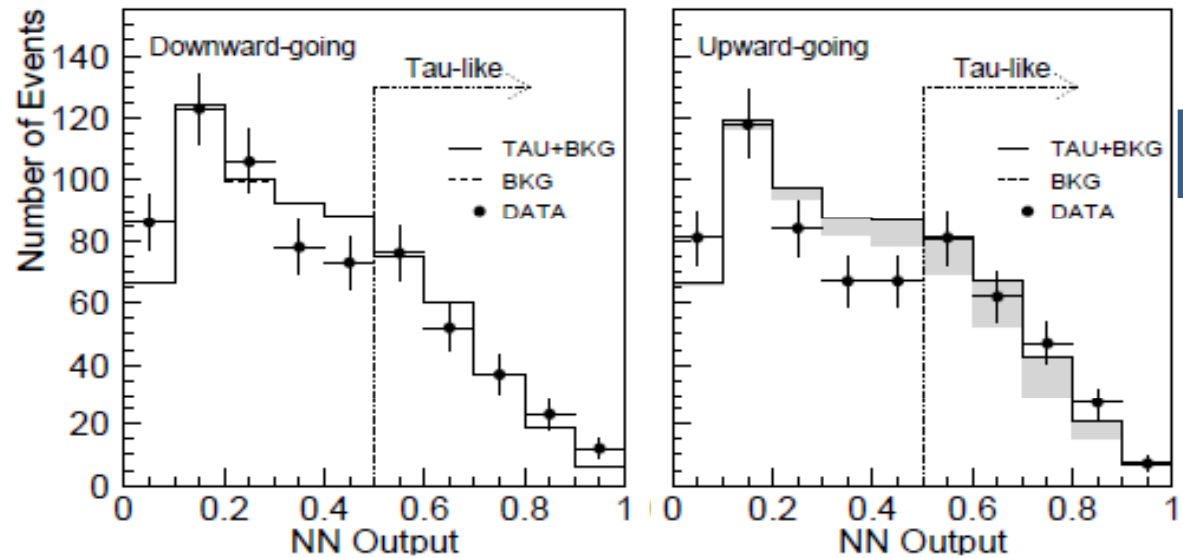
Likelihood

Down-going (no  $\nu_\tau$ )

Up-going



Neural-net



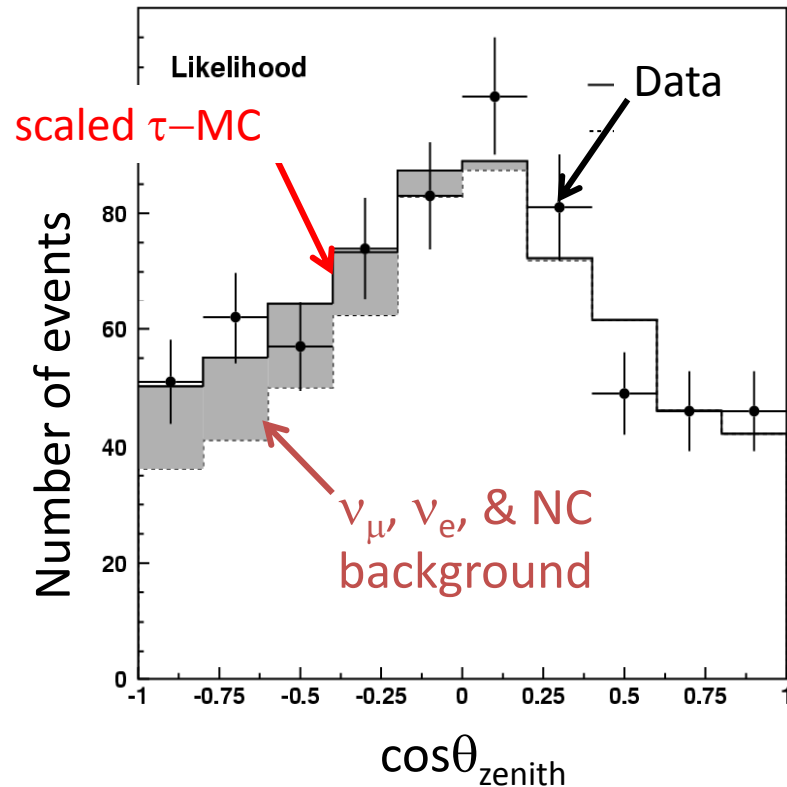
Zenith angle



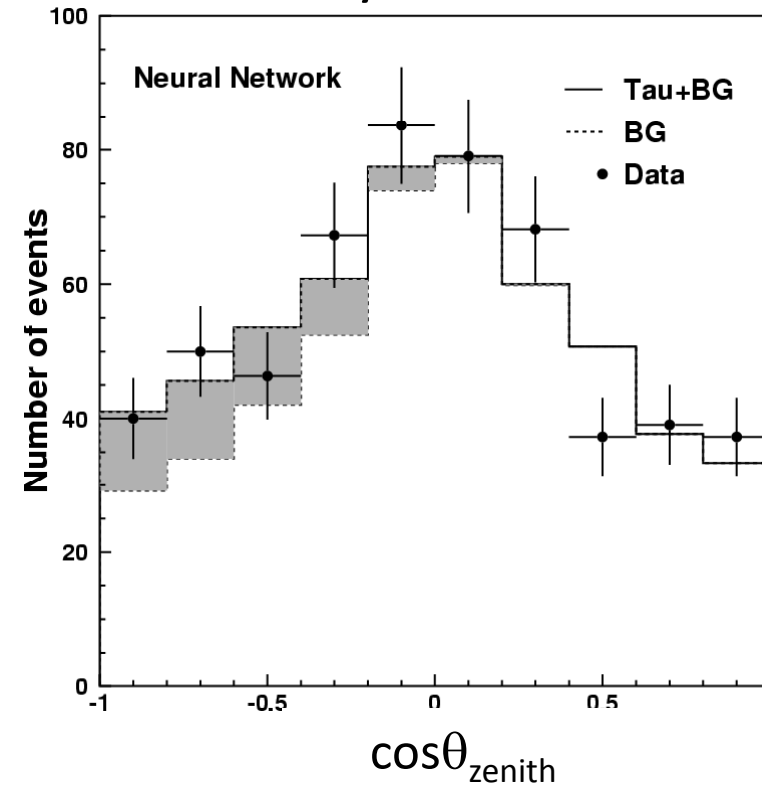
# Zenith angle distributions and fit results

Hep-ex/0607059

Likelihood analysis



NN analysis



Fitted # of  $\tau$  events

$138 \pm 48(\text{stat}) + 15 / -32(\text{syst})$

$134 \pm 48(\text{stat}) + 16 / -27(\text{syst})$

Expected # of  $\tau$  events

$78 \pm 26(\text{syst})$

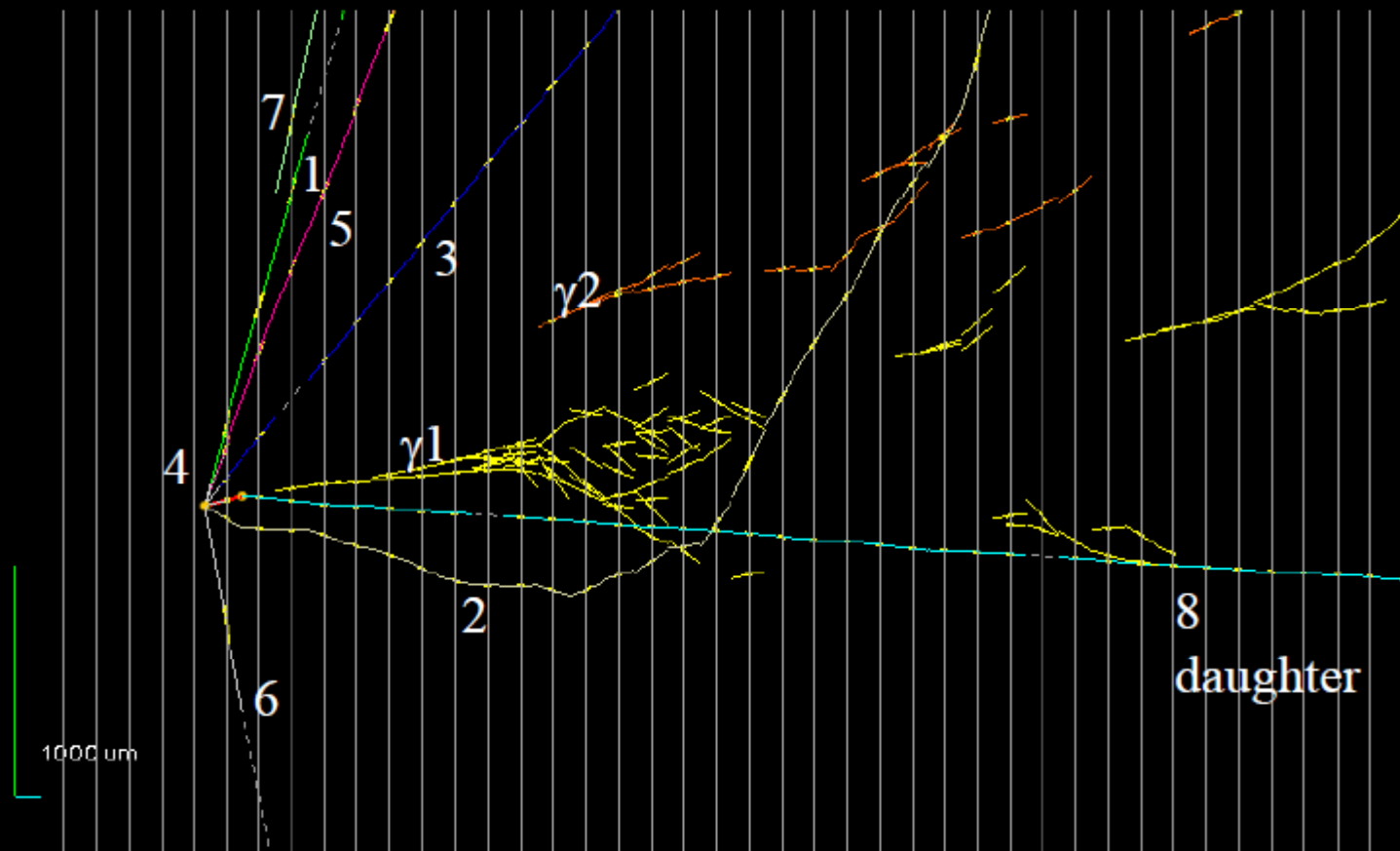
$78 \pm 27(\text{syst})$

Zero tau neutrino interaction is disfavored at  $2.4\sigma$ .

# OPERA first $\nu_\tau$ candidate

## Event topological features (side view)

Side view



Super-K is also trying to update the analysis

# *3 flavor oscillation analyses*

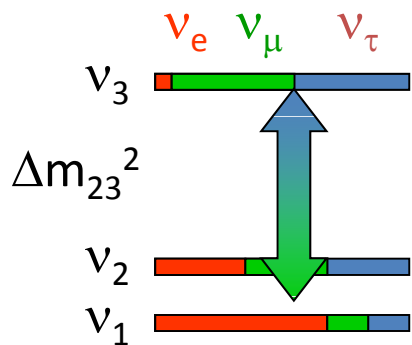


# 3 flavor oscillation: framework

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U \cdot \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

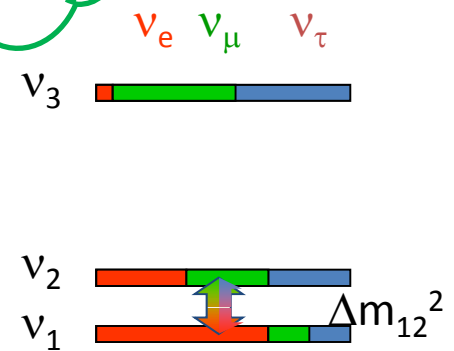
Can atmospheric neutrinos tell something?

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \times \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \times \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$



Atmospheric  
LBL

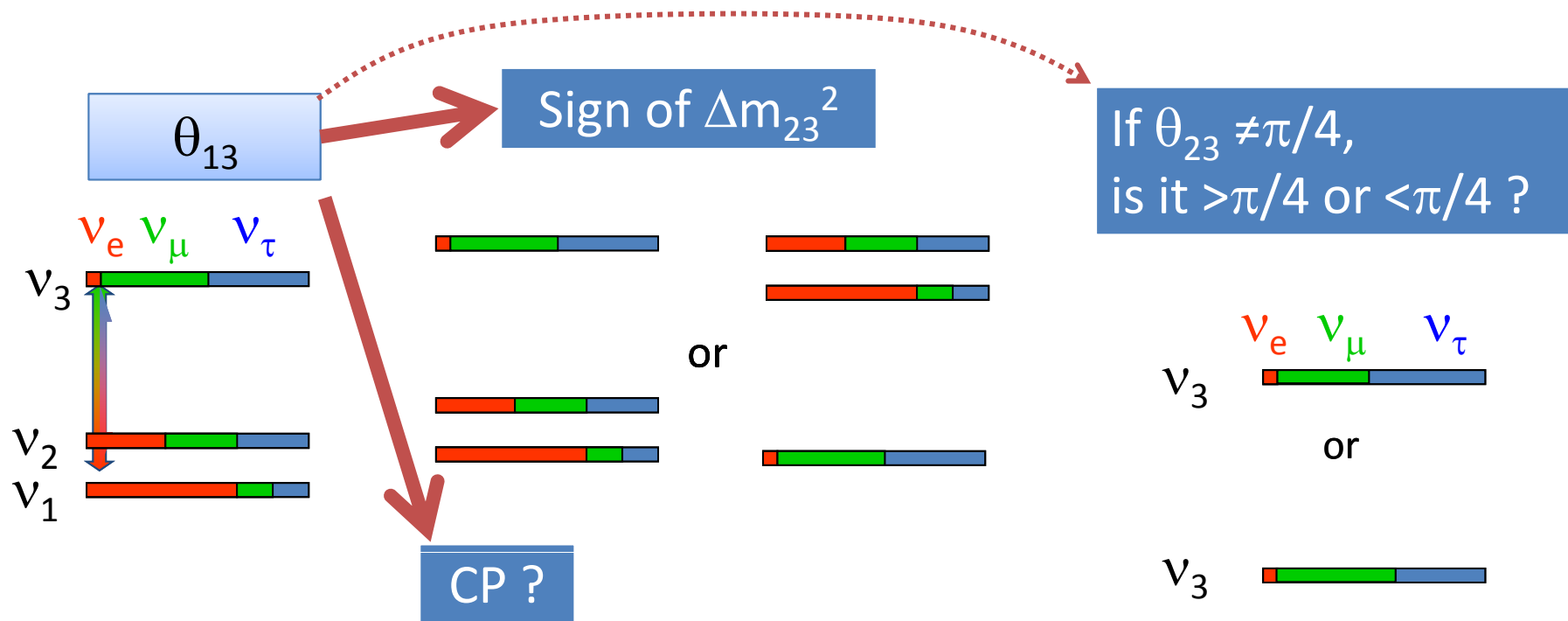
Solar  
KamLAND



# Sub-leading oscillations

$\sin^2\theta_{12}$ ,  $\sin^22\theta_{23}$ ,  $\Delta m_{12}^2$ ,  $|\Delta m_{23}^2|$  ... Already measured.

Next step: measure the unknown mixing angle  $\theta_{13}$



These are extremely important parameters to be measured.  
Question: How can we measure these parameters with  $\nu_{\text{atm}}$  ?

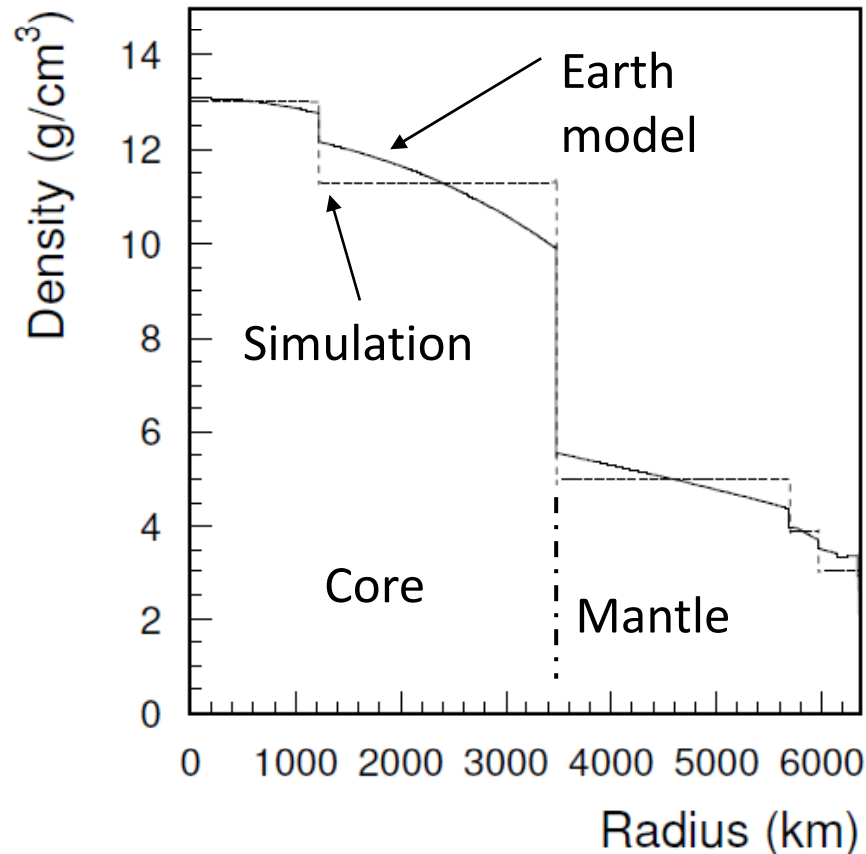
# *3 flavor oscillation analyses (1)*

*- Study of  $\theta_{13}$  -*

# Search for non-zero $\theta_{13}$ in atmospheric neutrino experiments

$$P(\nu_\mu \rightarrow \nu_e) = \sin^2 \theta_{23} \cdot \sin^2 2\theta_{13} \cdot \sin^2 \left( \frac{1.27 \Delta m_{23}^2 L}{E} \right) \quad (\Delta m_{12}^2=0 \text{ and vacuum oscillation assumed})$$

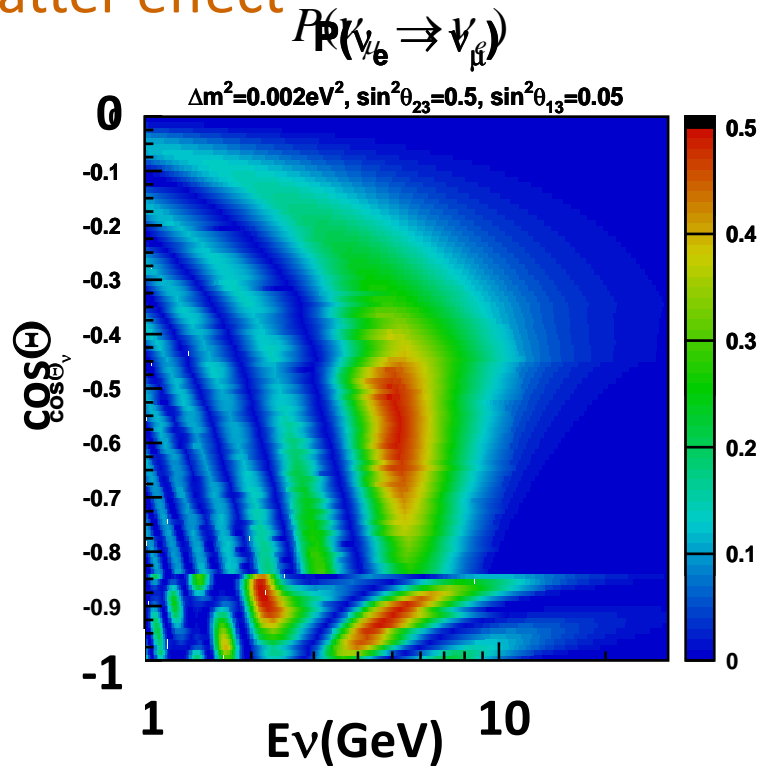
Since  $\nu_e$  is involved, the matter effect must be taken into account.



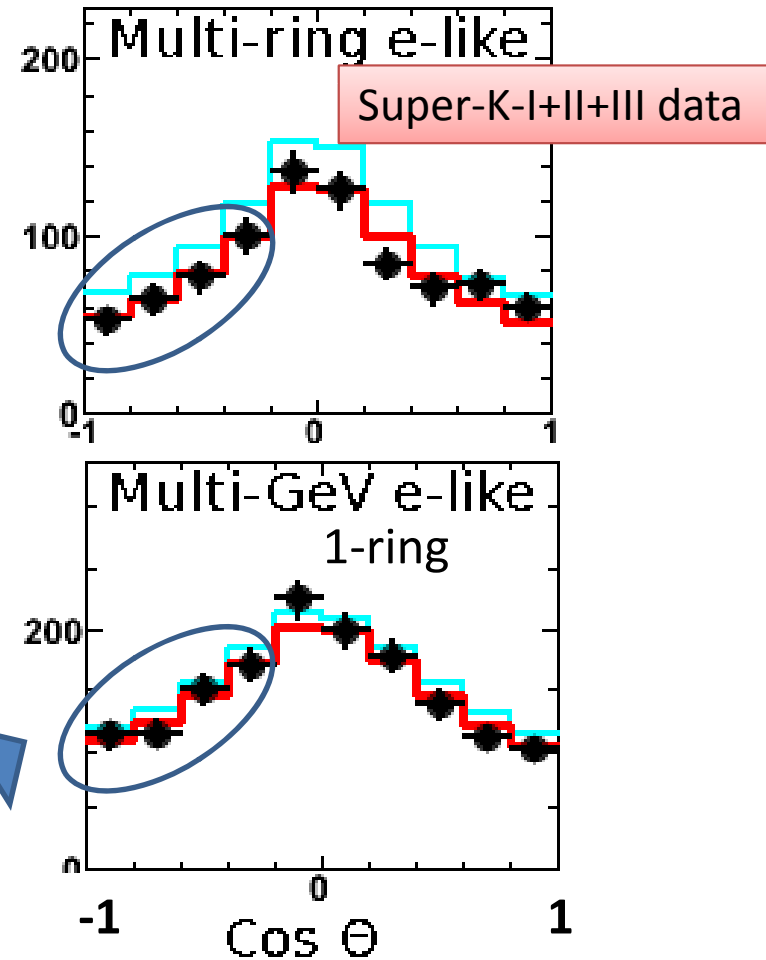
# Study of $\theta_{13}$

(One mass scale dominance ( $\Delta m_{12}^2=0$ ) assumed)

Matter effect



→ Electron appearance in the multi-GeV upward going events. (and some effects in  $\nu_\mu$  disappearance probability as well.)



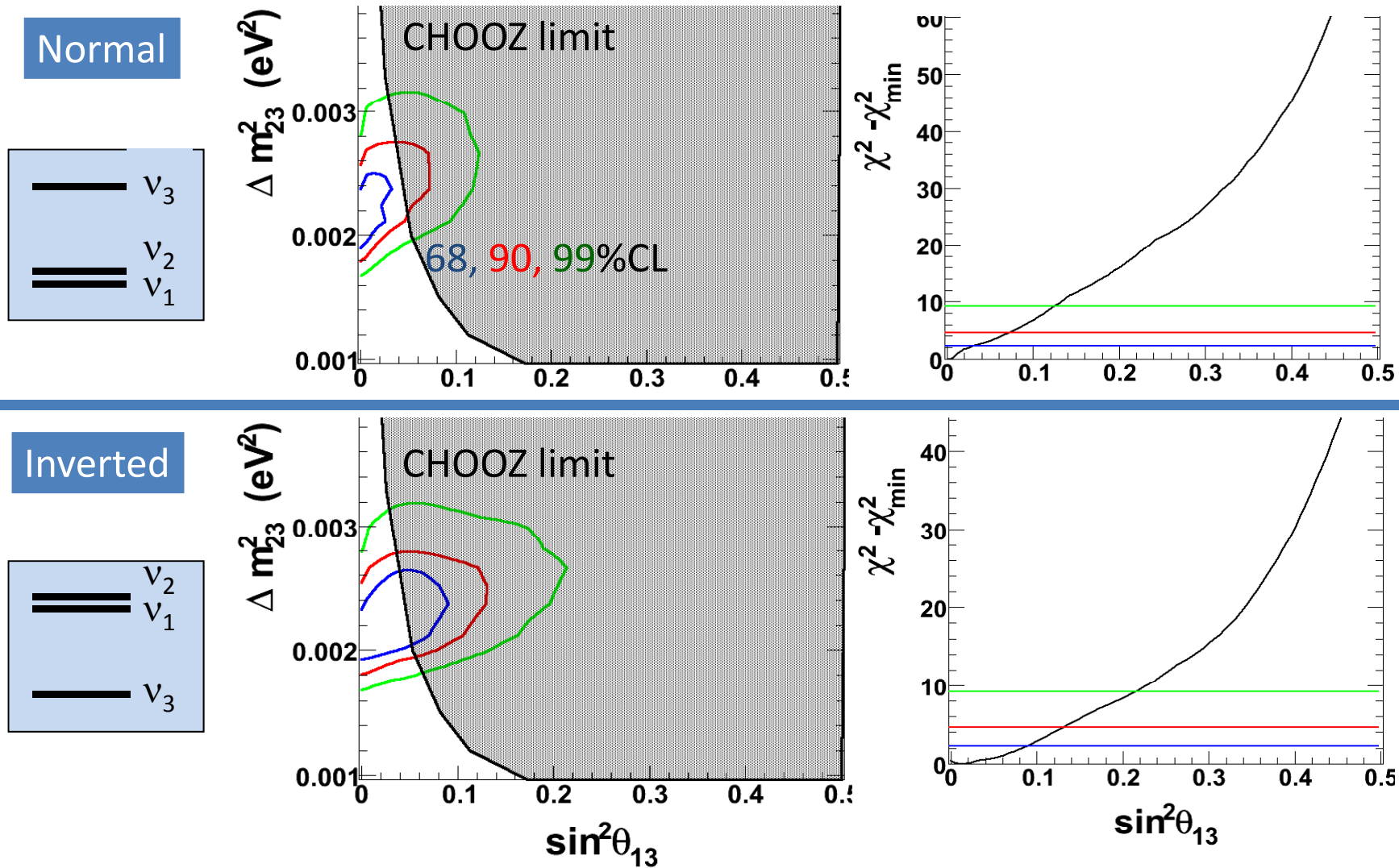
No evidence for electron appearance.

→ osci. analysis with all data.



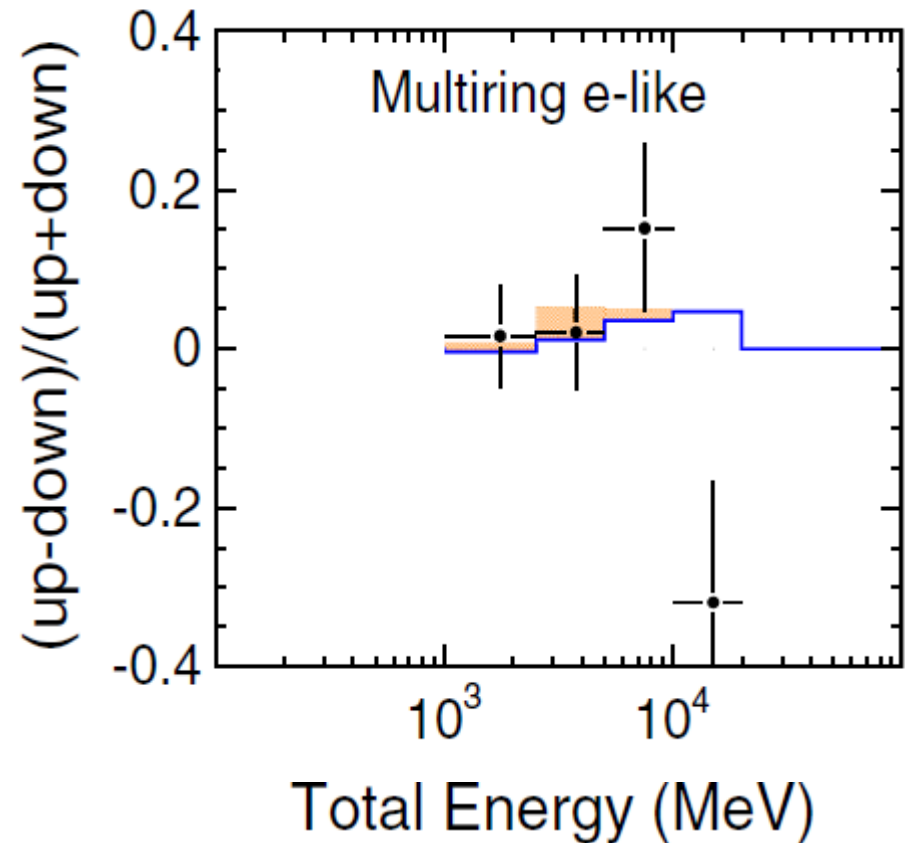
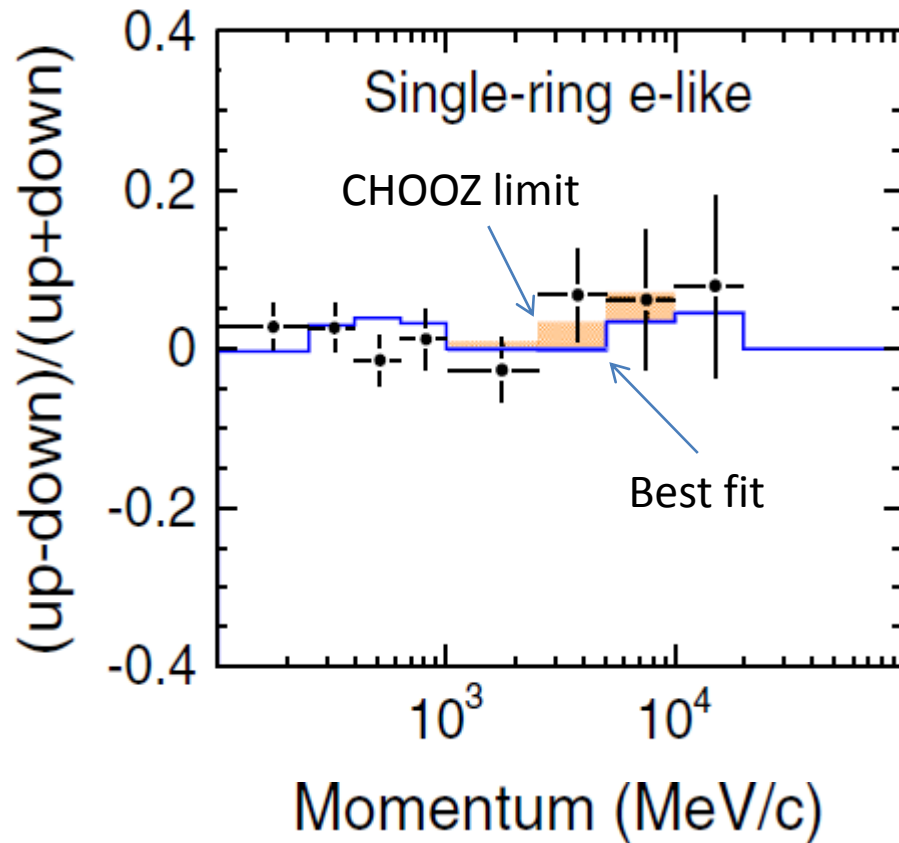
# Allowed $\theta_{13}$ region from SK atmospheric

SK PRD 81, 092004 (2010)



No evidence for non-zero  $\theta_{13}$  with an analysis that assumed  $\Delta m_{12}^2 = 0$ .

# Up-down asymmetry

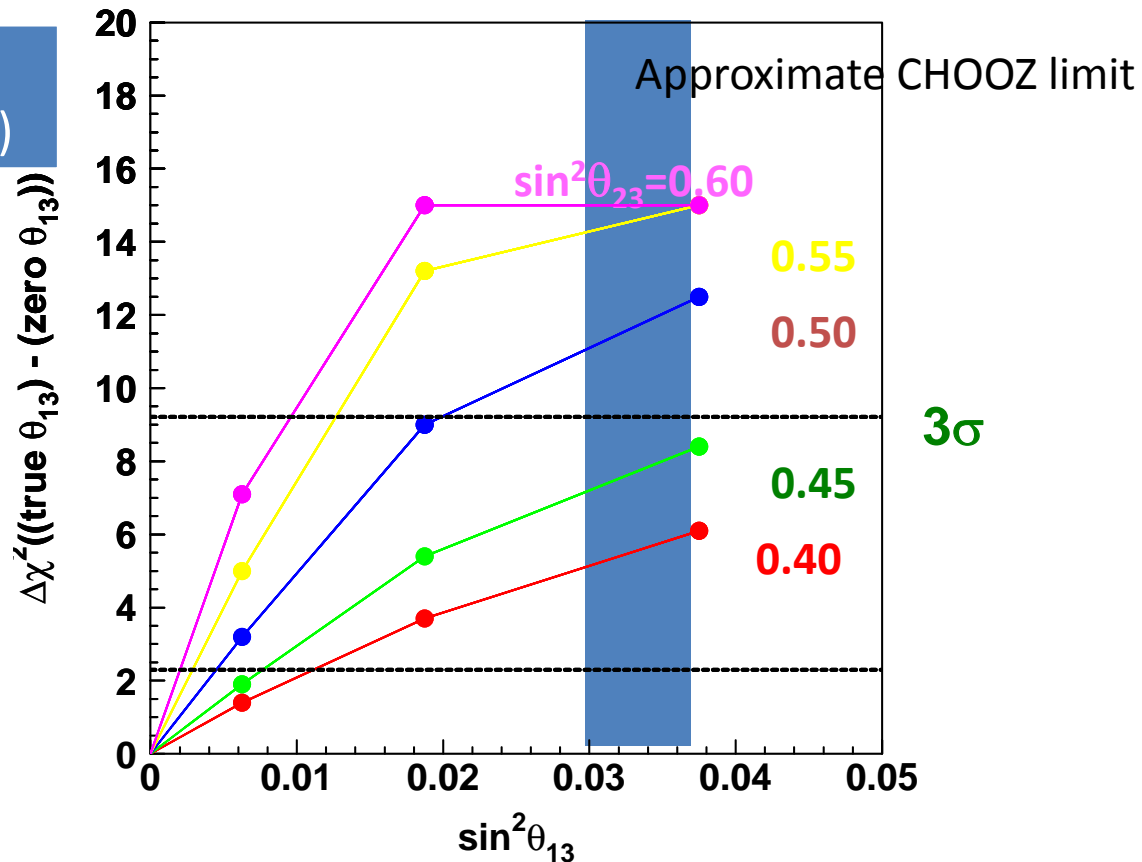


# Future sensitivity to non-zero $\theta_{13}$

M. Shiozawa et al., RCCN workshop (2004)

$$P(\nu_\mu \rightarrow \nu_e) = \sin^2 \theta_{23} \cdot \sin^2 2\theta_{13} \cdot \sin^2 \left( \frac{1.27 \Delta m_{23}^2 L}{E} \right) \quad (\text{vacuum})$$

20yrs SK  
(450kton·yr)



$s^2 2\theta_{12} = 0.825$   
 $s^2 \theta_{23} = 0.40 \sim 0.60$   
 $s^2 \theta_{13} = 0.00 \sim 0.04$   
 $\delta_{cp} = 45^\circ$   
 $\Delta m_{12}^2 = 8.3 \times 10^{-5}$   
 $\Delta m_{23}^2 = +2.5 \times 10^{-3}$

Positive signal for nonzero  $\theta_{13}$  can be seen if  $\theta_{13}$  is near the CHOOZ limit and  $\sin^2 \theta_{23} > 0.5$

But probably  
after  
T2K/Nova/  
reactor...

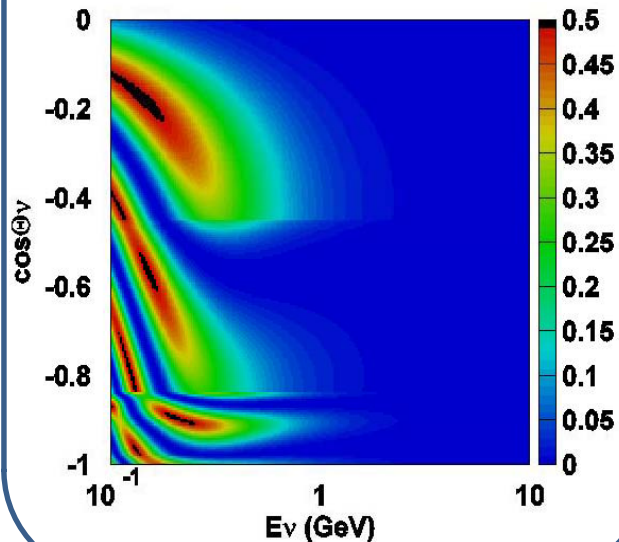
## ***3 flavor oscillation analyses (2)***

***- Solar term effect and octant of  $\theta_{23}$  -***

# Solar term effect and octant of $\theta_{23}$

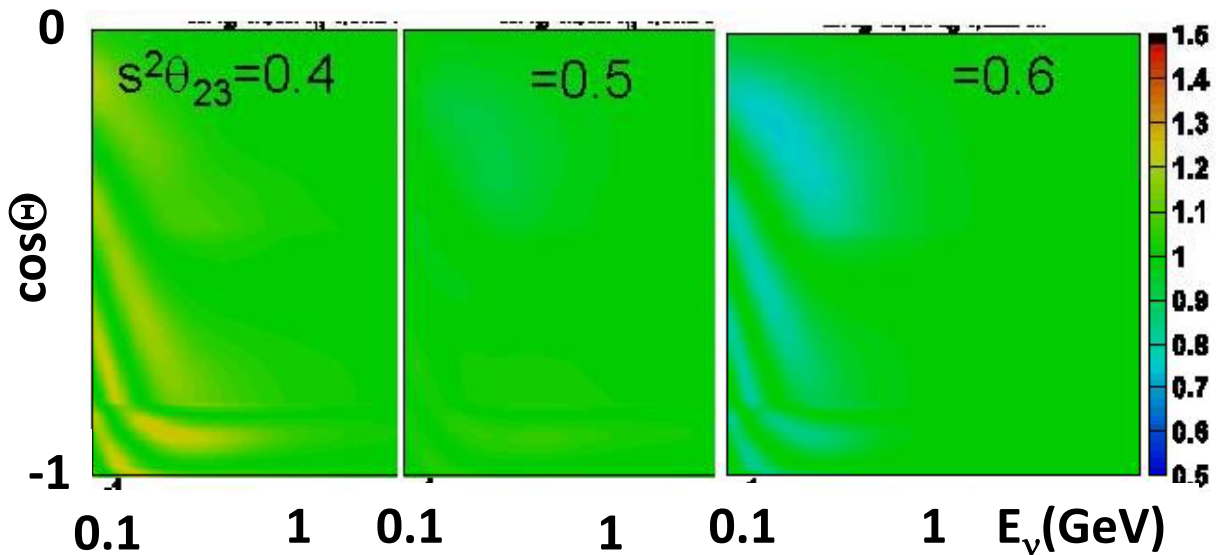
( $\theta_{13}=0$  assumed)

$P(\nu_\mu \rightarrow \nu_e)$  by solar oscillation parameters



However, due to the cancellation between  $\nu_\mu \rightarrow \nu_e$  and  $\nu_e \rightarrow \nu_x$ , the change in the  $\nu_e$  flux is small.

$$\frac{\nu_e \text{ flux}(osc)}{\nu_e \text{ flux}(no \text{ osc})}$$

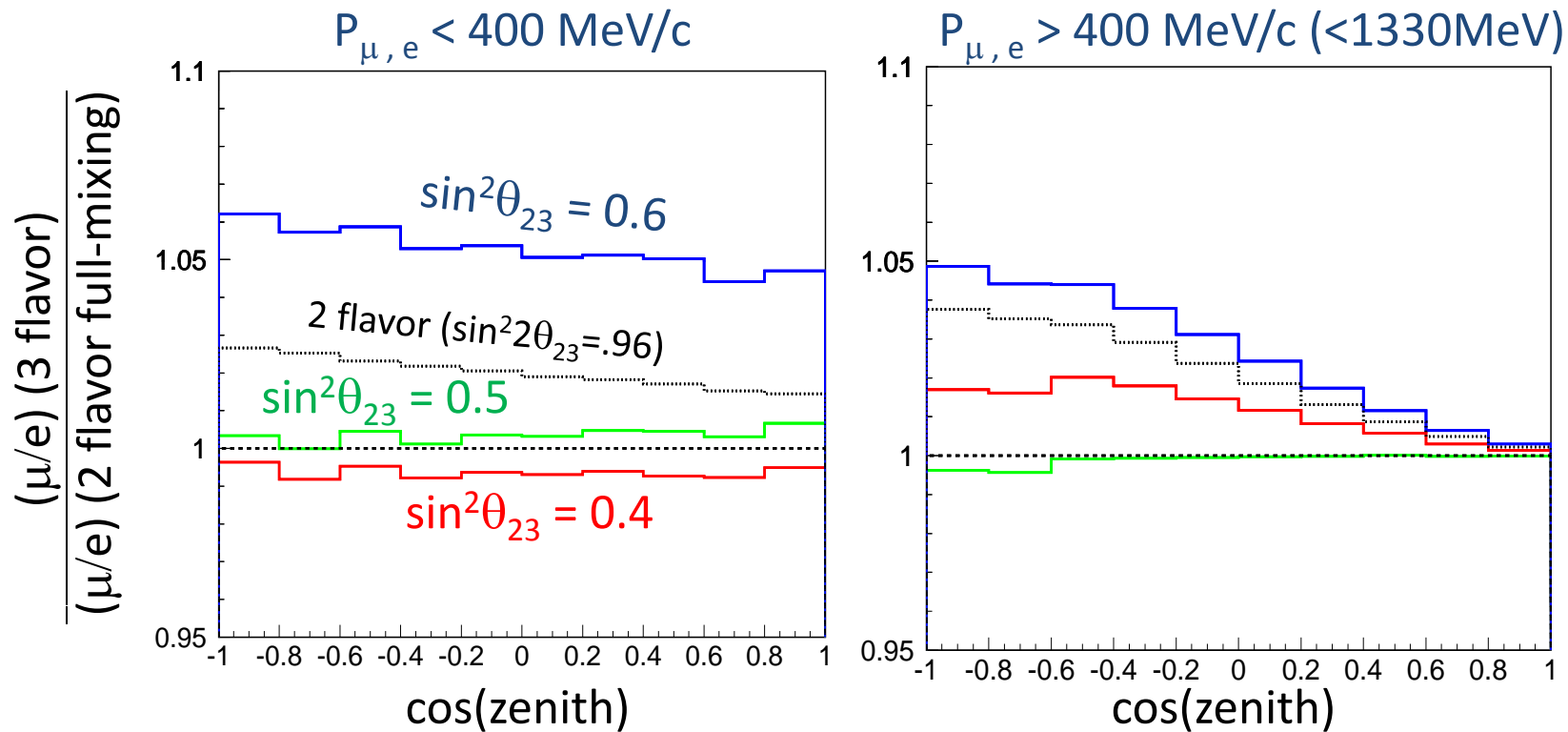


Oscillation probability is different between  $s^2\theta_{23}=0.4$  and  $0.6$

→ discrimination between  $\theta_{23} > \pi/4$  and  $< \pi/4$  might be possible by studying sub-GeV atmospheric  $\nu_e$  and  $\nu_\mu$  events.

# Effect of the solar terms to the sub-GeV $\mu/e$ ratio (zenith angle dependence)

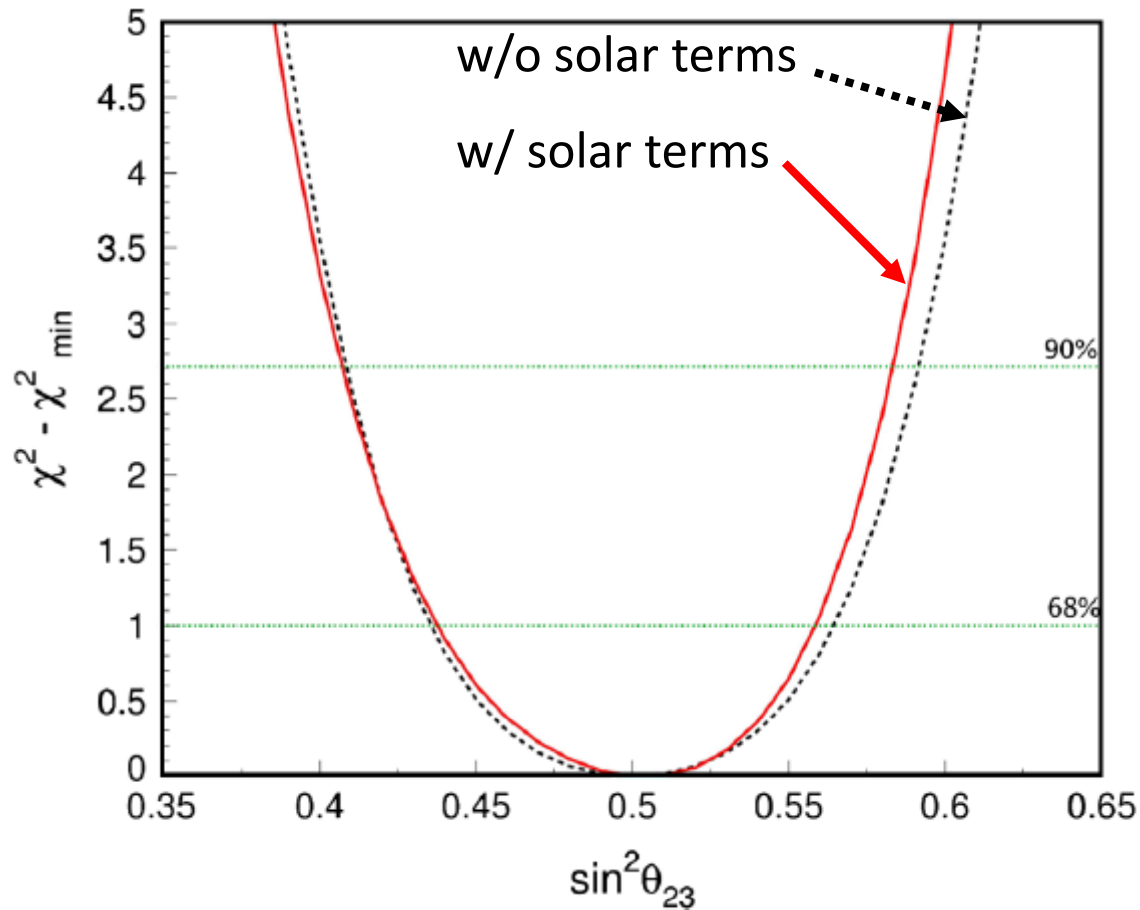
$$\begin{aligned} \Delta m_{12}^2 &= 8.3 \times 10^{-5} \text{ eV}^2 \\ \Delta m_{23}^2 &= 2.5 \times 10^{-3} \text{ eV}^2 \\ \sin^2 2\theta_{12} &= 0.82 \\ \sin^2 \theta_{13} &= 0 \end{aligned}$$



It could be possible to discriminate the octant of  $\theta_{23}$ , if  $\sin^2 \theta_{23}$  is significantly away from 0.5.

# Constraint on $\sin^2 \theta_{23}$ with and without the solar terms

SK PRD 81, 092004 (2010)



Solar terms off :

best-fit :  $\sin^2 \theta_{23} = 0.50$

Solar terms on :

best-fit :  $\sin^2 \theta_{23} = 0.50$

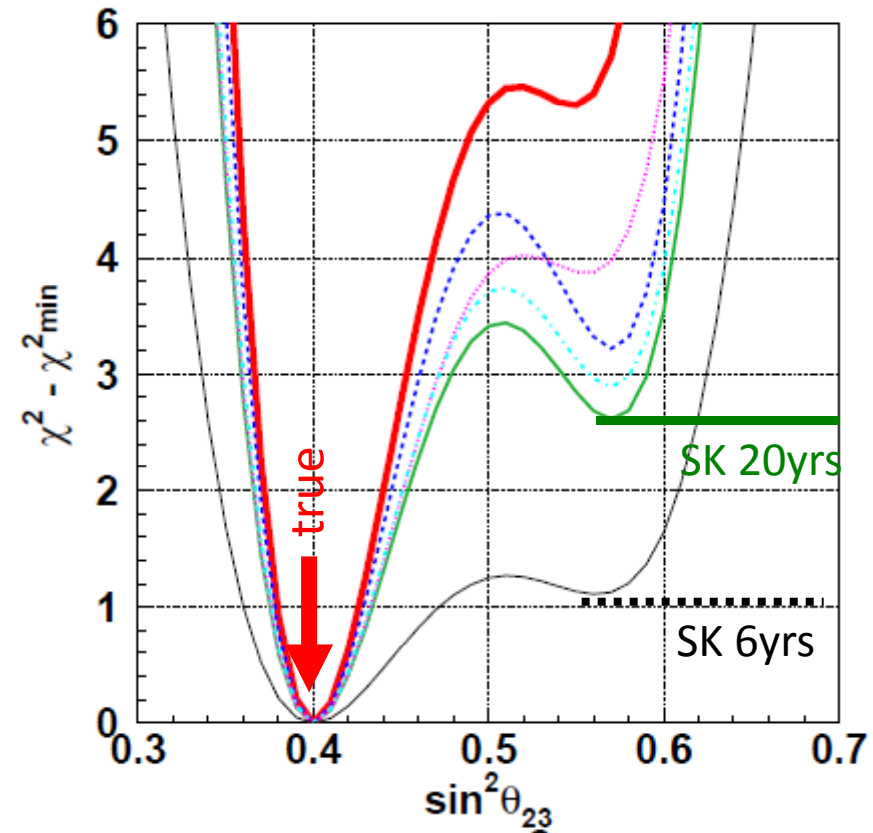
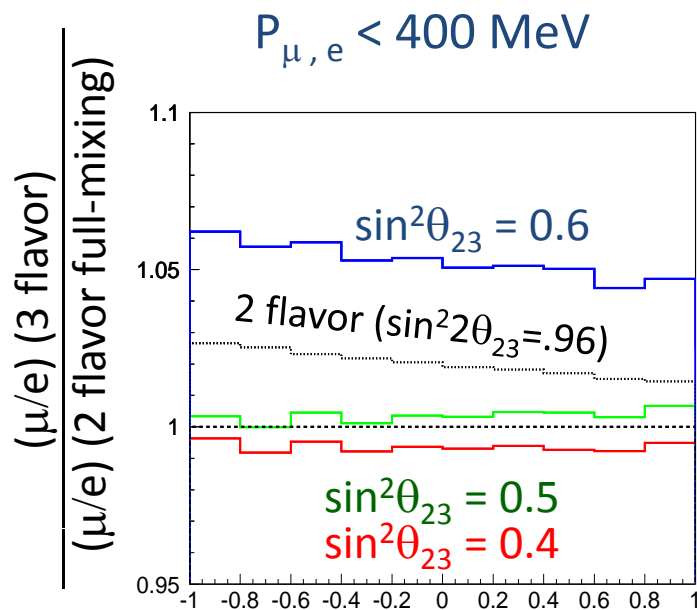
Still the maximum  
mixing is most  
favored.

# Future $\theta_{23}$ octant sensitivity and syst. errors

Y. Takenaga, PhD thesis (2008)

$$\begin{aligned} \Delta m_{12}^2 &= 8.3 \times 10^{-5} \text{ eV}^2 \\ \Delta m_{23}^2 &= 2.5 \times 10^{-3} \text{ eV}^2 \\ \sin^2 2\theta_{12} &= 0.82 \\ \sin^2 \theta_{13} &= 0 \end{aligned}$$

0.45 Mtonyr = SK 20yr



- 20yrs, all syst =  $\times 0.25$
- - - syst (v int) =  $\times 0.25$
- - - syst (flux) =  $\times 0.25$
- - - syst (detector) =  $\times 0.25$

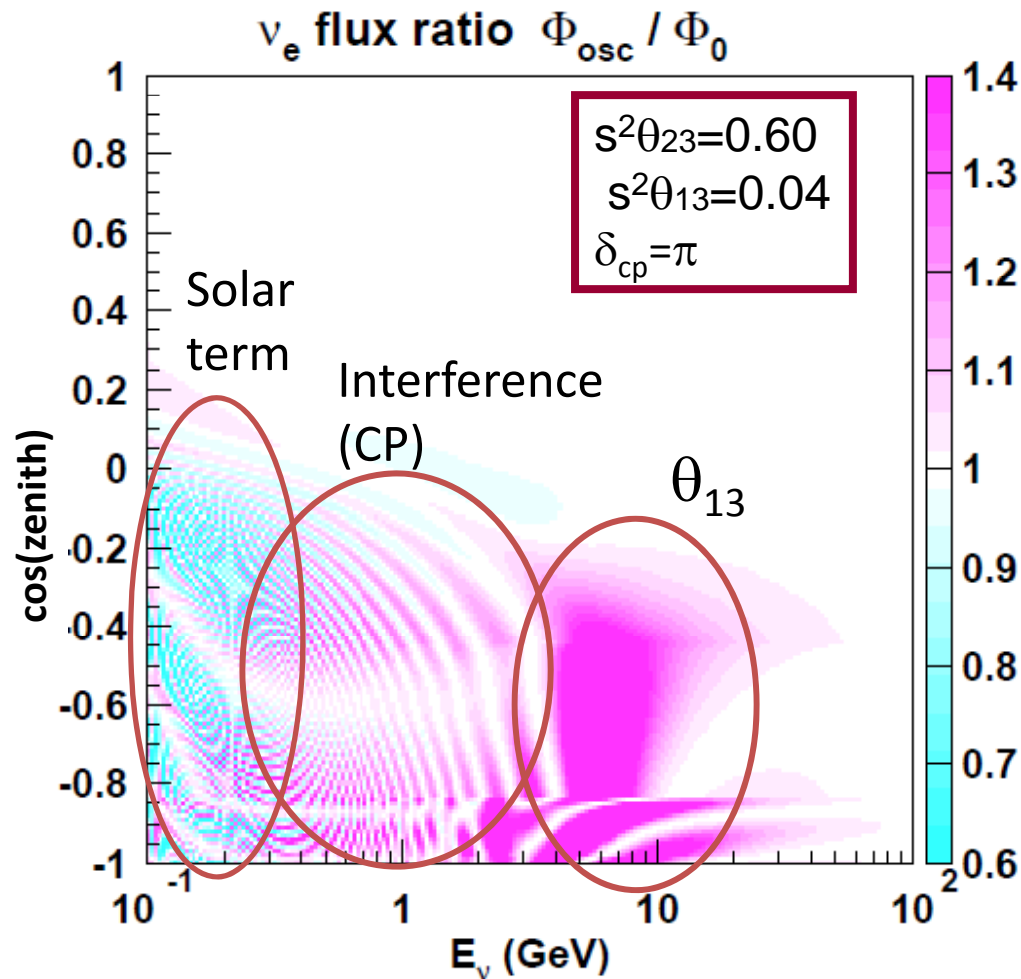


# ***3 flavor oscillation analyses (3)***

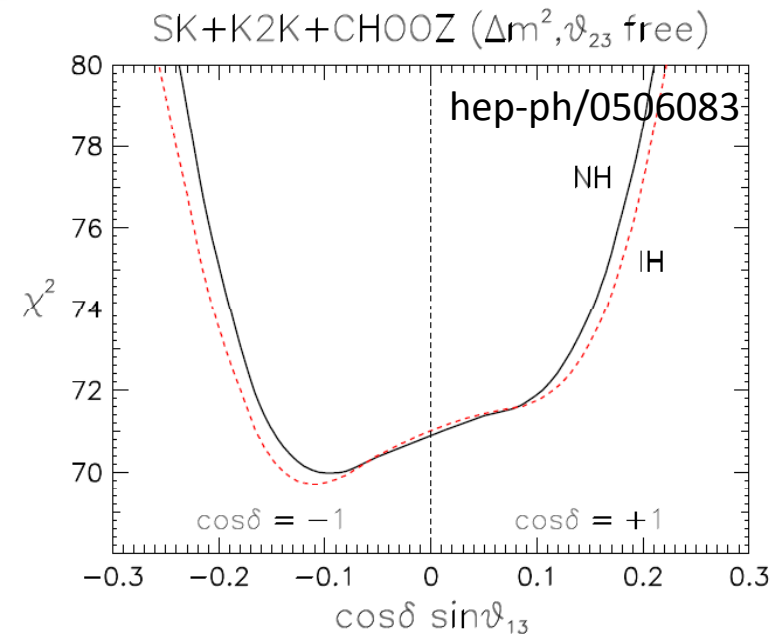
***- Full 3 flavor analysis -***

# Full 3 flavor analysis of the atmospheric $\nu$ data

- ◆ Super-K-I+II+III searched for non-zero  $\theta_{13}$  based on the 1 mass scale dominance model. No evidence for non-zero  $\theta_{13}$  has been found.
- ◆ However, the solar term effects are relevant in atmospheric neutrino exp's.



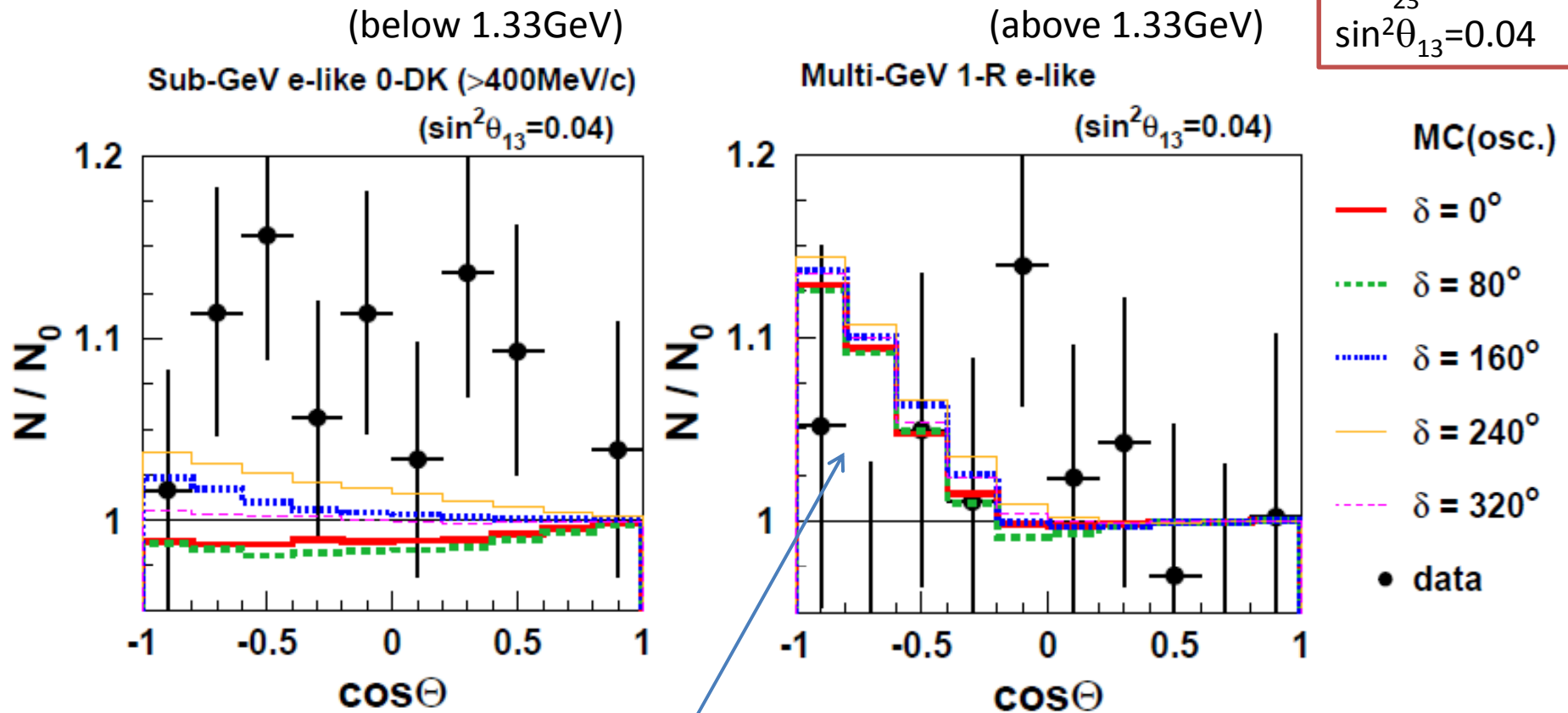
- ◆ Therefore, the interference term (CP term) may play an important role.
- ◆ In fact, analyses in hep-ph/0506083 and others indicate the potential importance of the full 3 flavor analysis.



# Expected $\delta_{CP}$ effect on zenith angle dist.

C.Ishihara, PhD thesis (2010)

$\sin^2\theta_{23}=0.55$   
 $\Delta m_{23}^2=0.0021$   
 $\sin^2\theta_{13}=0.04$

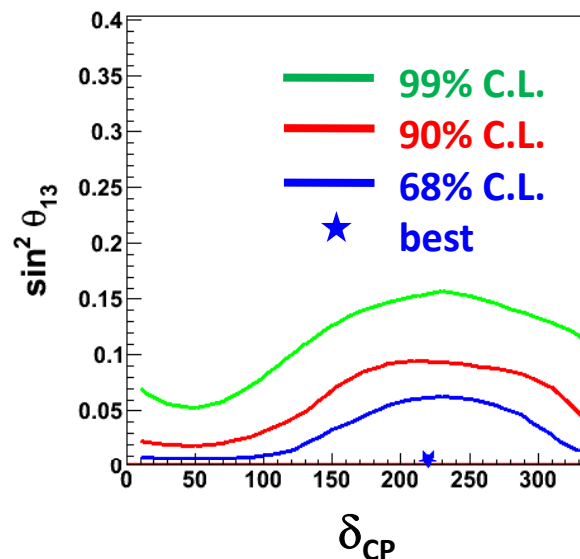
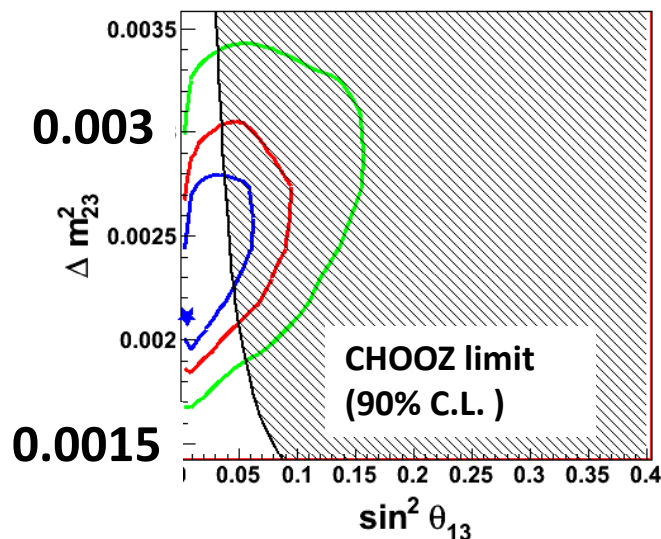
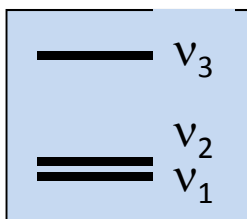


Overall excess:  $\theta_{13}$  effect

# Full 3-flavor oscillation results

Fitted:  $\Delta m_{23}^2$ ,  $\sin^2 \theta_{23}$ ,  $\sin^2 \theta_{13}$ ,  $\delta_{CP}$  and sign of  $(\Delta m_{23}^2)$

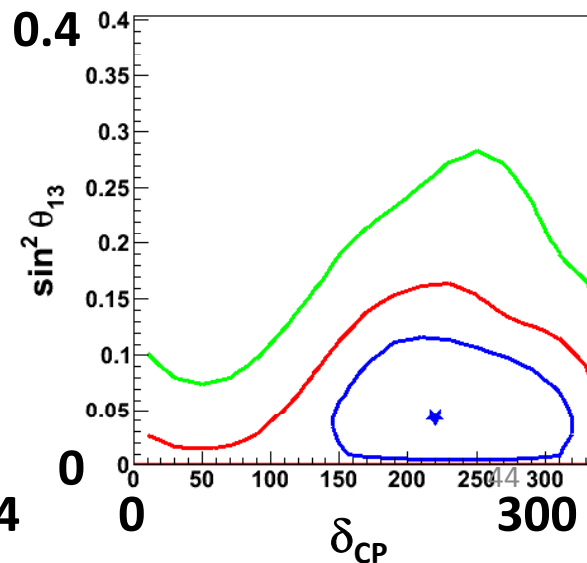
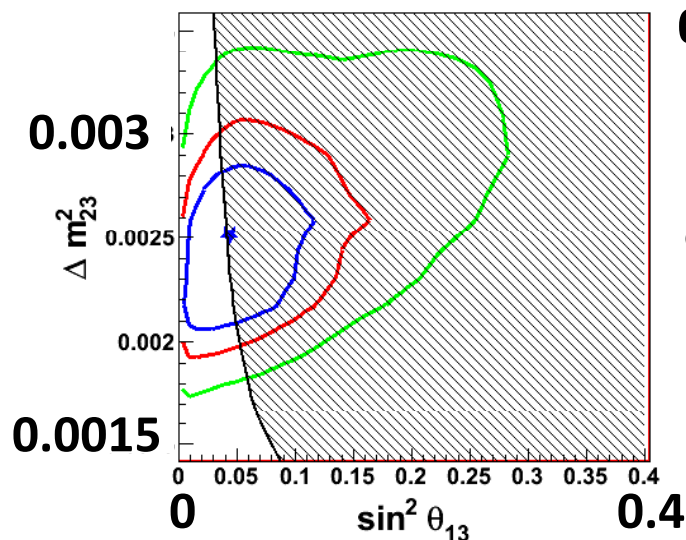
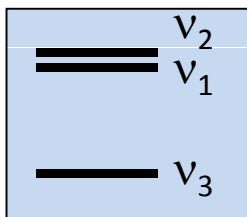
Normal



Super-K-I+II+III  
Y. Takeuchi Nu2010

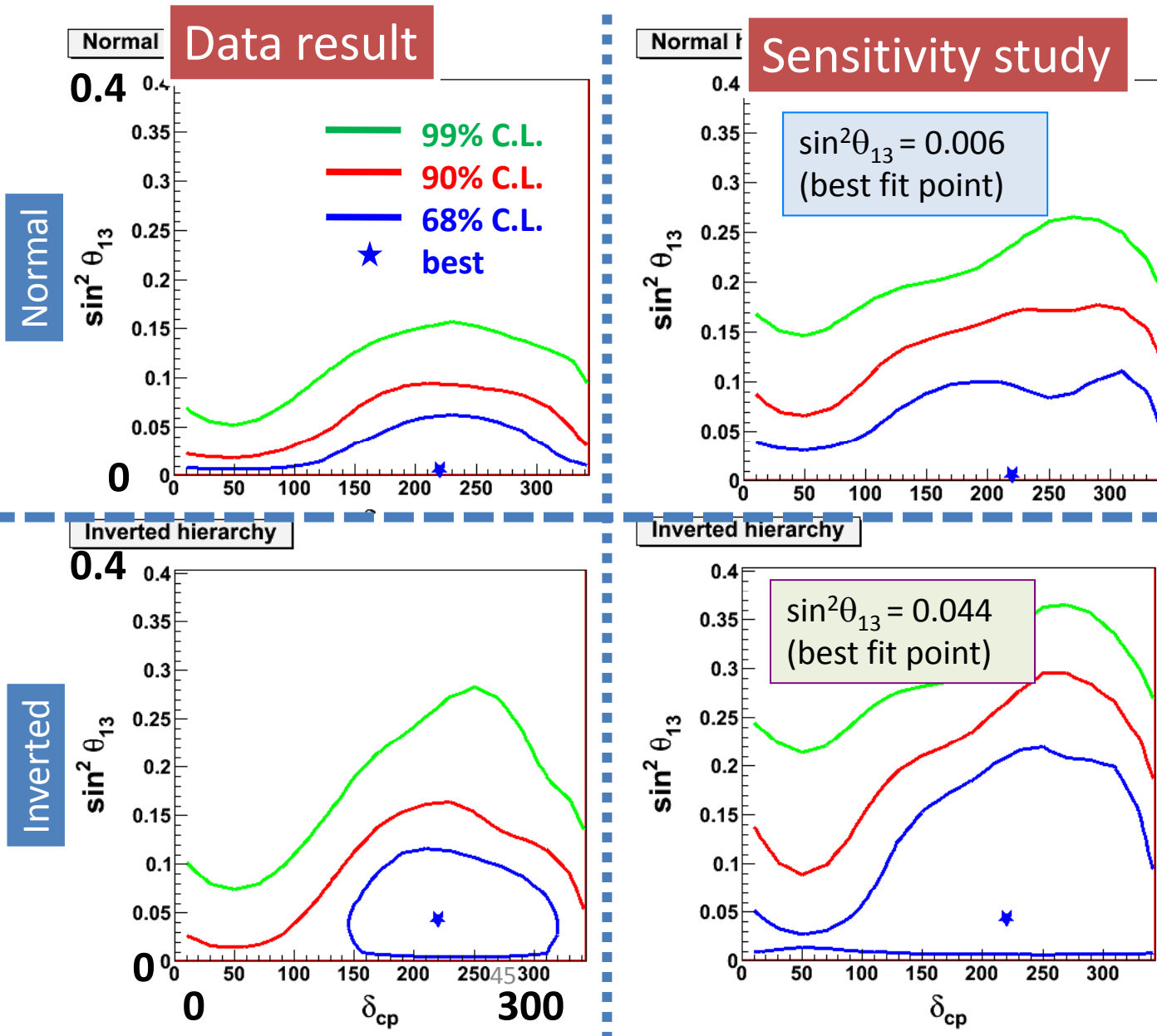
Preliminary

Inverted



indicating  
some CP  
sensitivity

# Results versus sensitivity

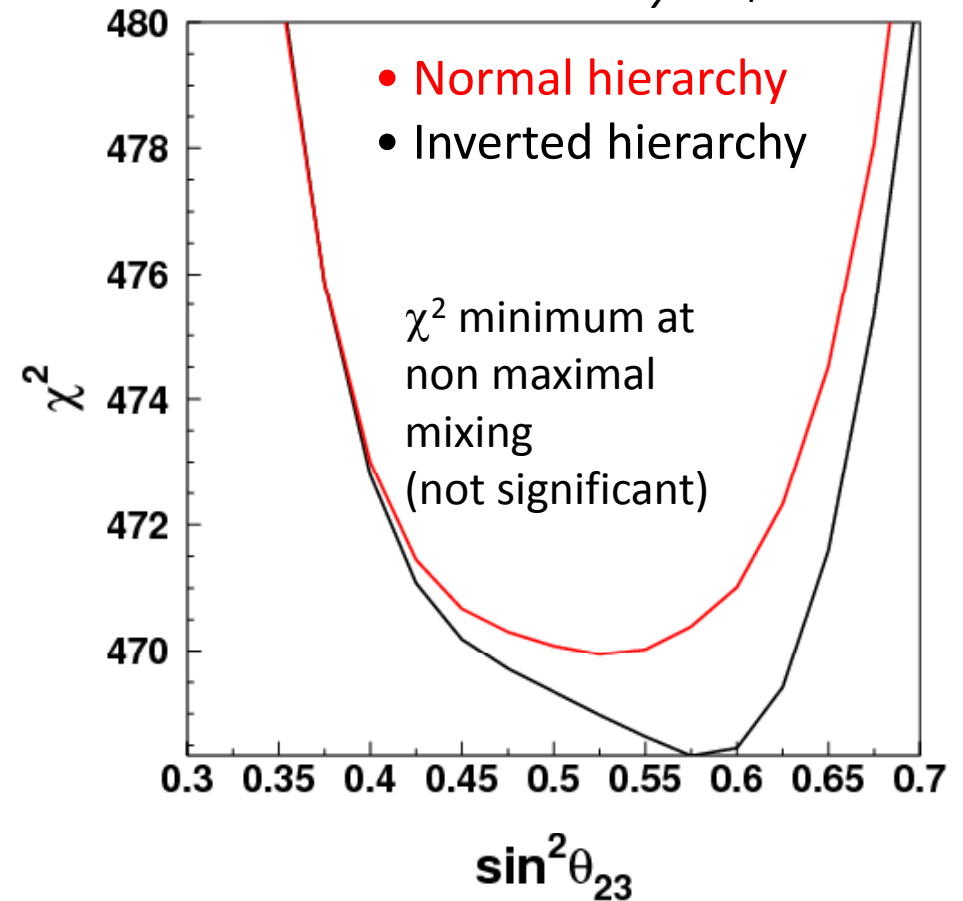
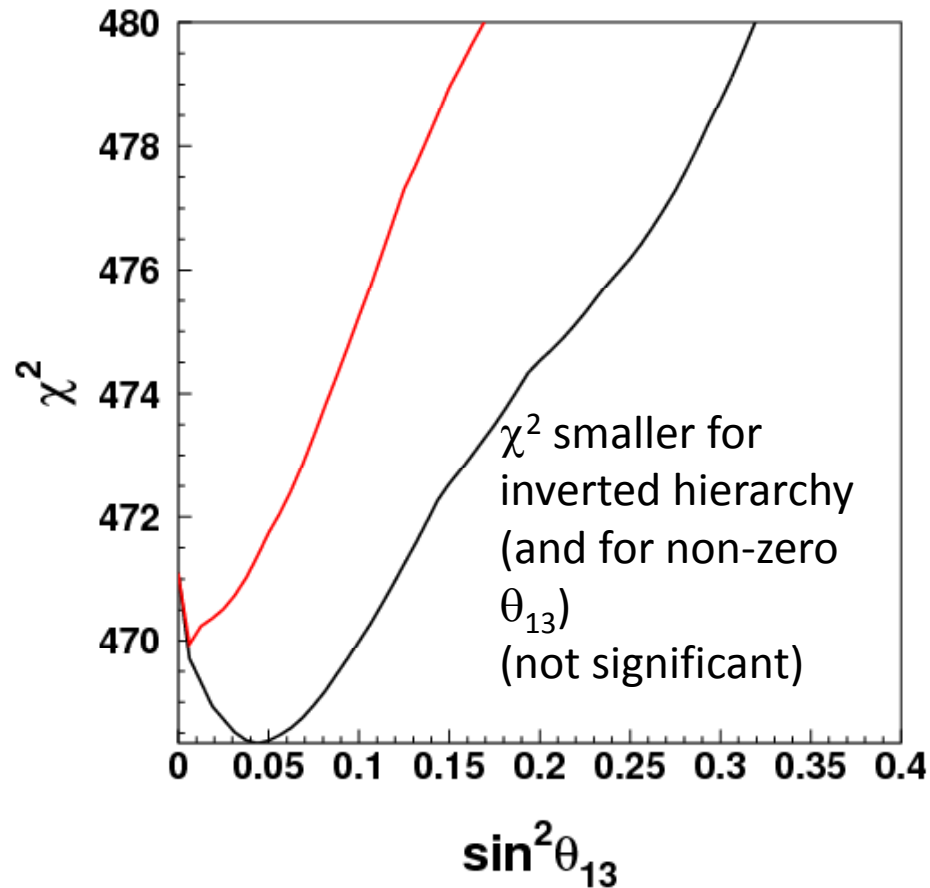


For the assumed oscillation parameters, the results from the data are slightly better than those by the sensitivity study (based on MC).

The results suggest that atmospheric neutrino experiments have some sensitivity to CP violation.

# $\chi^2$ distributions

Preliminary Super-K-I+II+III

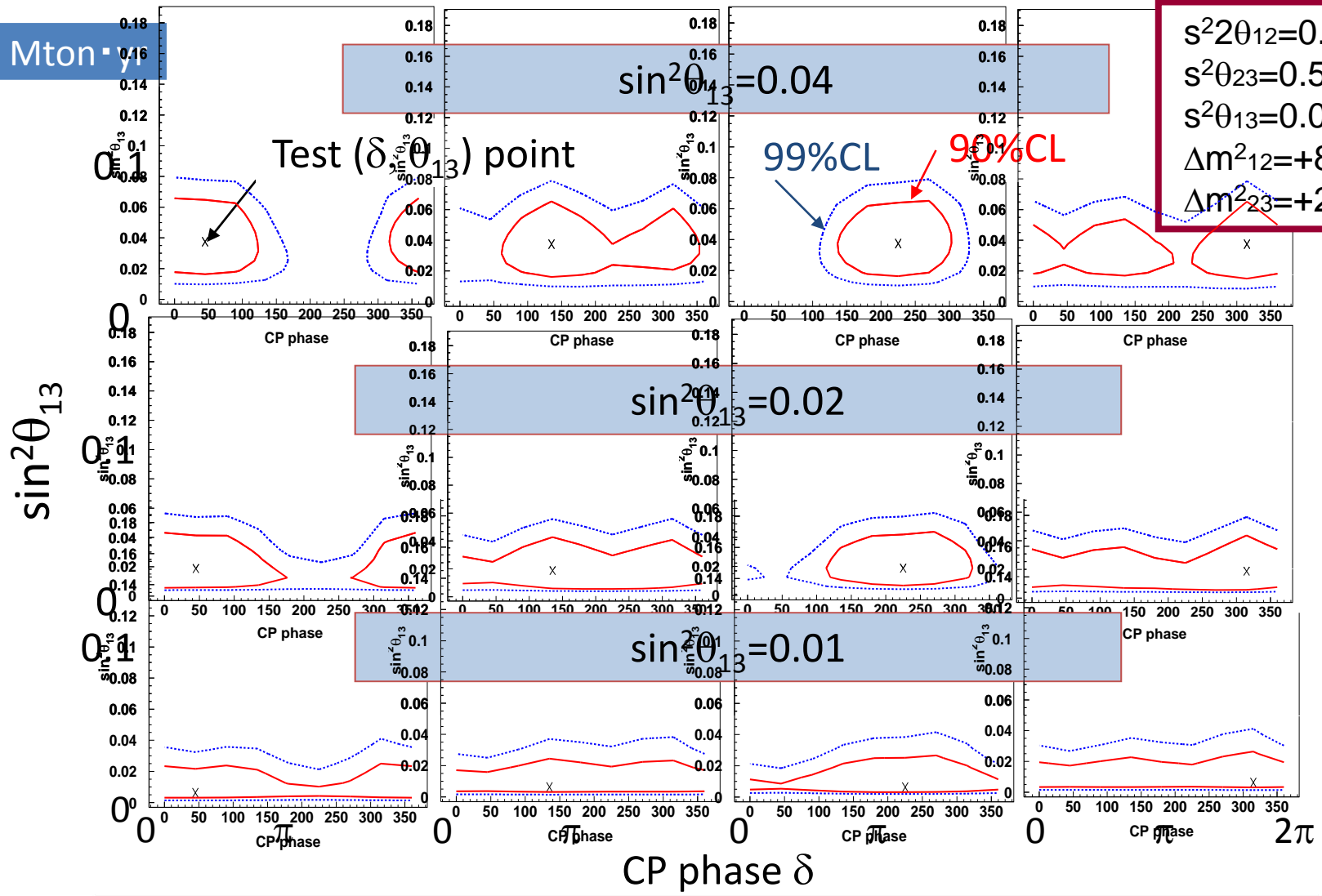


There is no clear evidence for the sub-leading effects. However, the data indicate that future atmospheric neutrino experiments might be a powerful tool for studying sub-leading effects.

# Sensitivity: a future $\nu_{atm}$ experiment

M. Shiozawa et al., RCCN workshop (2004)

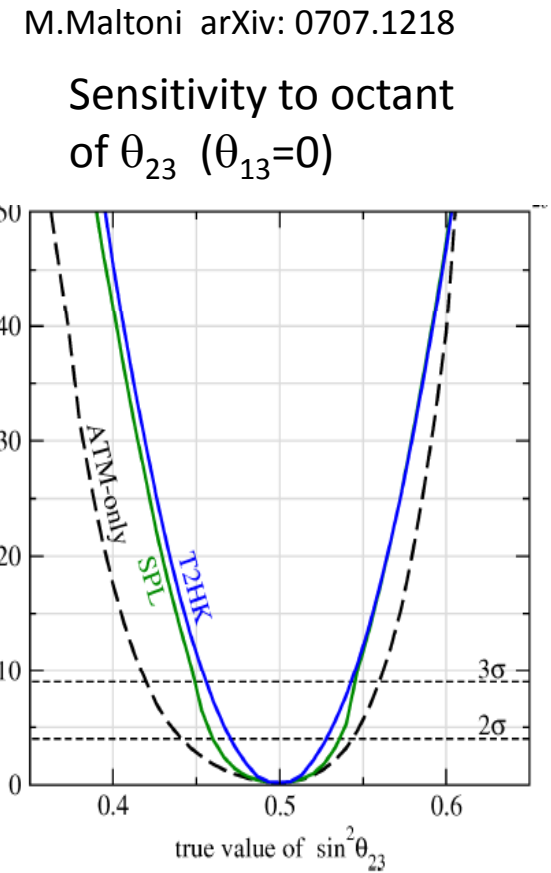
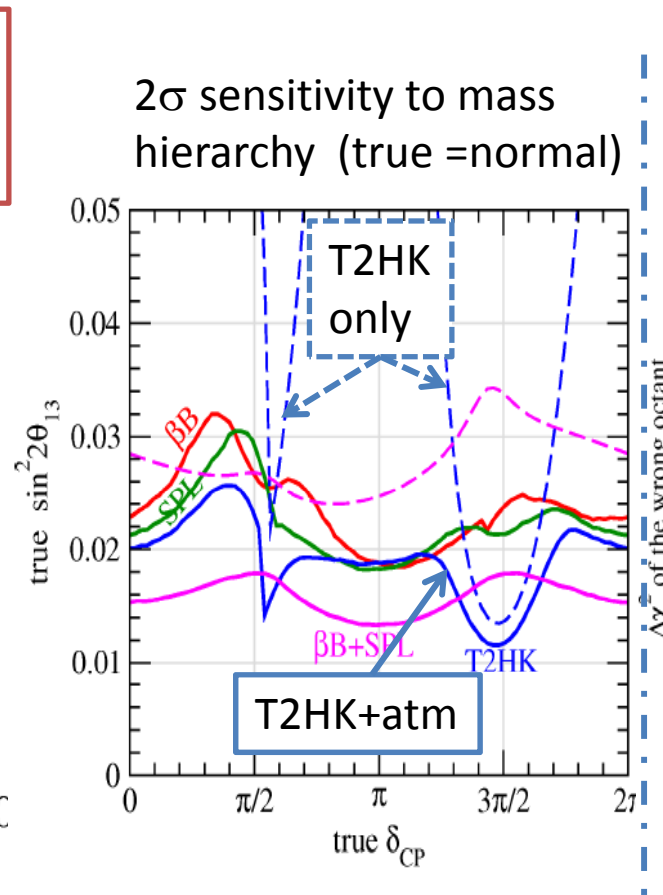
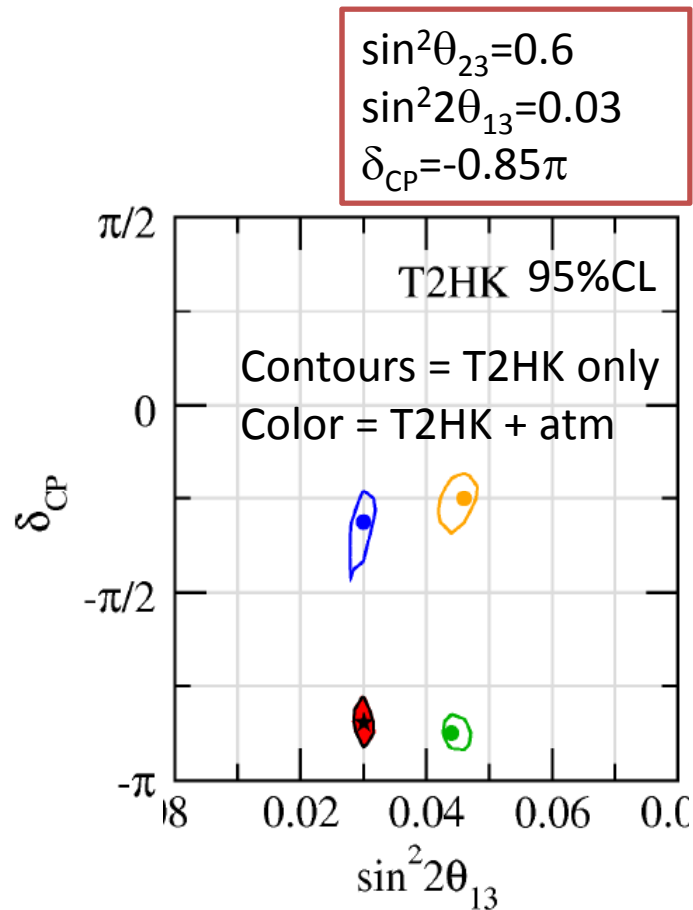
1.8 Mton  $\cdot$  y



CP phase could be studied if  $\theta_{13}$  is close to the CHOOZ limit.

# Synergies with long baseline experiments

Future long baseline experiments have high sensitivities to  $\delta_{CP}$  ....  
 However, in some experiments (especially with relatively short baseline ( $\sim 300\text{km}$ )),  
 a problem of parameter degeneracy is expected.



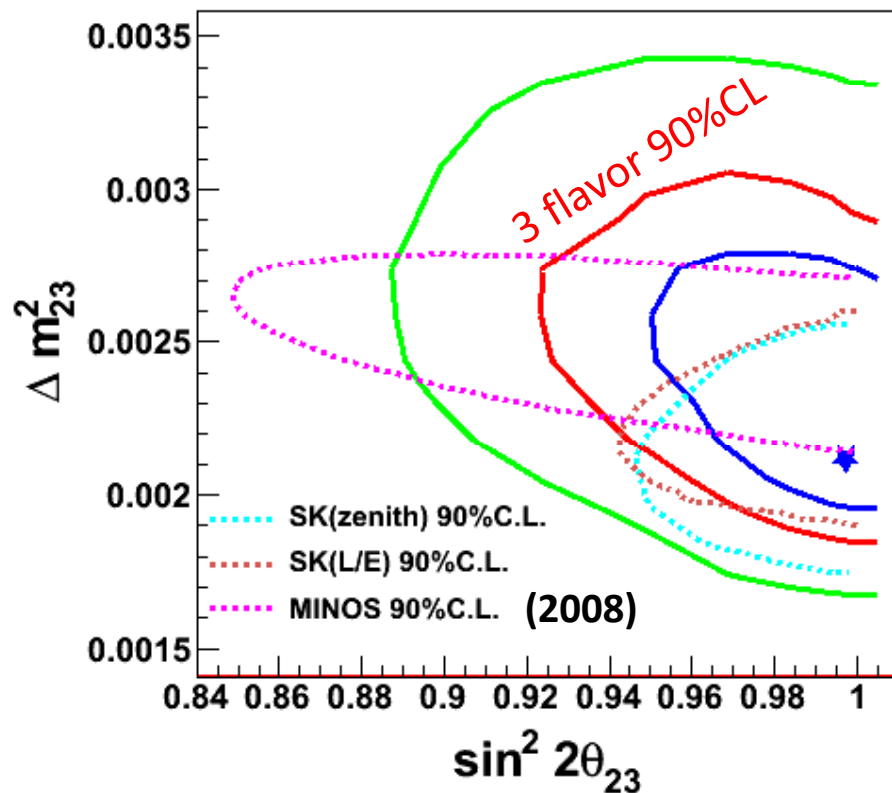
Atmospheric neutrinos (which are available freely) will help future LBL experiments!



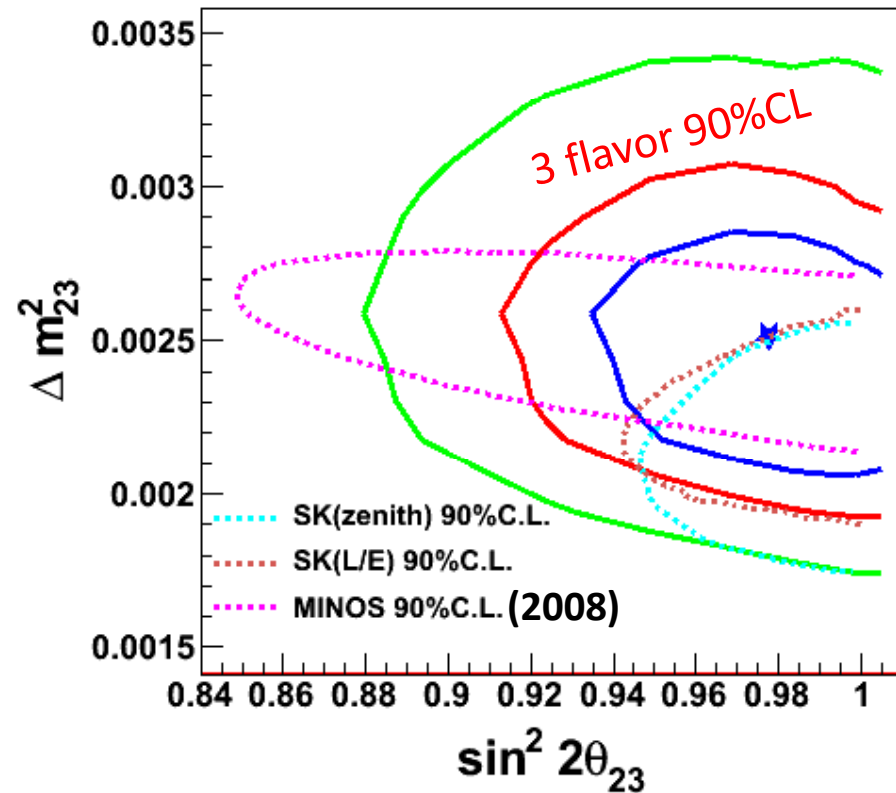
# Possible importance of the full 3-flavor oscillation analysis (1)

Preliminary Super-K-I+II+III

Normal hierarchy

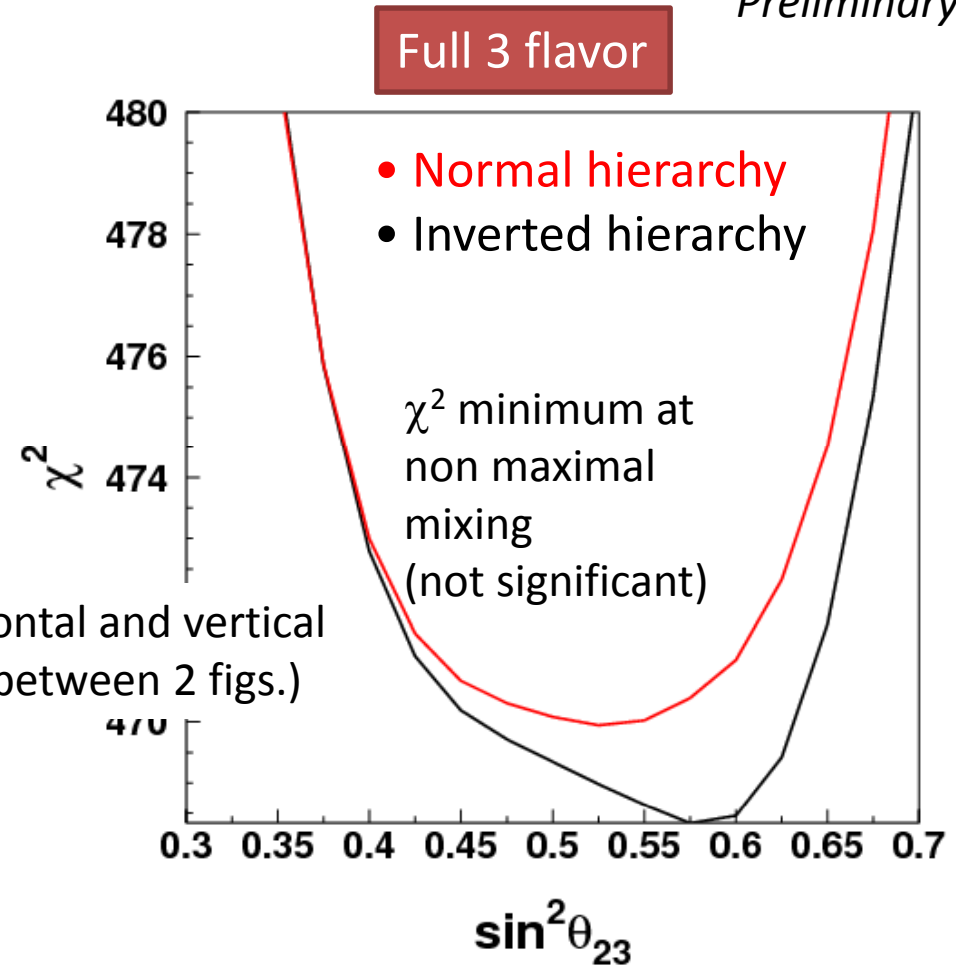
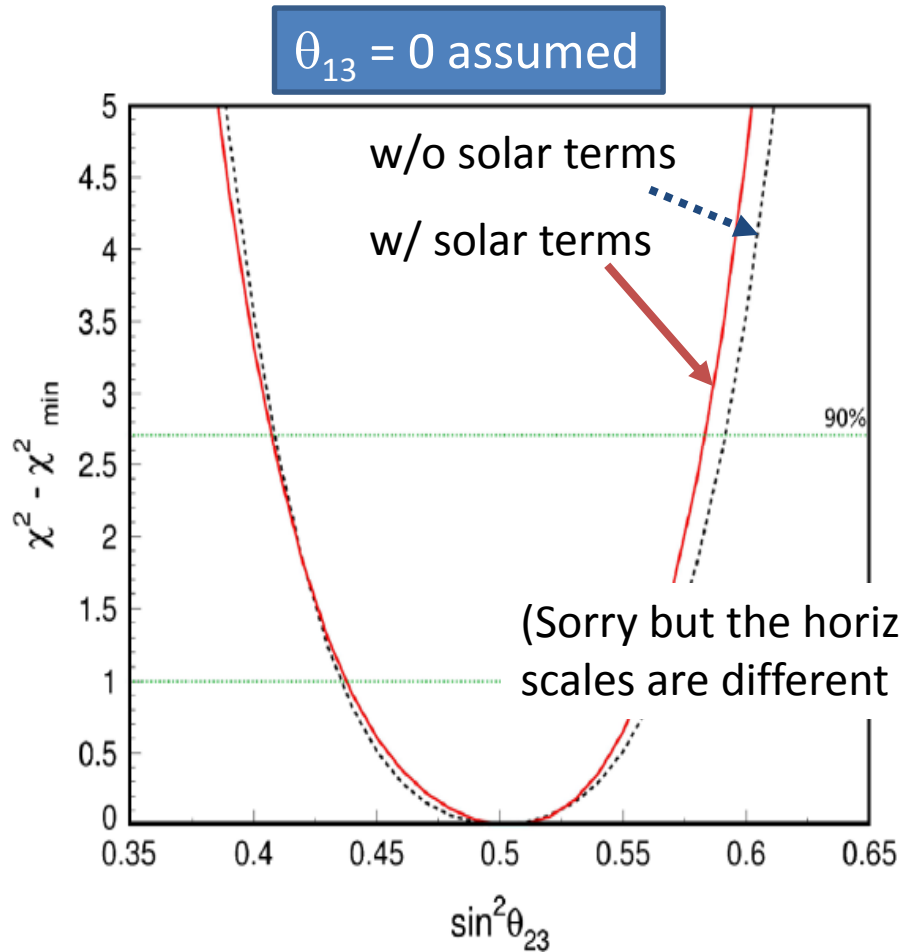


Inverted hierarchy



# Possible importance of the full 3-flavor oscillation analysis (2)

Preliminary



These distributions suggest that “full 3 flavor oscillation analysis” is important in estimating the oscillation parameters accurately.

# Summary

- With the improved atmospheric neutrino data, the calculation of the neutrino flux is also improving.
- The present data are consistent with  $\nu_{\mu} \rightarrow \nu_{\tau}$  oscillation with the maximal mixing.
- The full 3 flavor oscillation analysis has been carried out, suggesting that atmospheric neutrino experiments are sensitive to sub-leading effects. In particular, future atmospheric neutrino experiments with high statistics are sensitive to CP violation, if  $\theta_{13}$  is large.
- Even for estimating  $(\Delta m_{23}^2, \sin^2\theta_{23})$ , a full 3 flavor oscillation analysis might be required to accurately estimate the allowed parameter regions.
- Atmospheric neutrinos could help future LBL experiments in resolving the parameter degeneracy problems.